



# MCRT in galaxies with SKIRT

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# Peter Camps



## **Academic (Ghent University)**

- 1980: Master Engineering
- 2011: Bachelor Physics & Astronomy
- 2012-current: PhD student (Maarten Baes)

## **Commercial (30 years in between)**

- commercial software development
- international management
- technical software (e.g. PDF editing)
- small teams (1 to 20)

# Overview

## **MCRT in galaxies with SKIRT**

- Dust in galaxies
- SKIRT features and code design
- Energy balance in galaxies
- Automated galaxy modeling

## **MCRT post-processing of hydrodynamic snapshots**

- Stochastic heating of dust grains
- Dust grids: regular, hierarchical, unstructured
- Importing hydro snapshots: AMR, SPH
- FIR properties of galaxies in a cosmological simulation

# Dust in galaxies

Section A-1













# Interstellar dust

## Minor fraction of the interstellar medium

- Dust-to-gas ratio is usually less than 1%

## But a crucial constituent

- Extinction: up to 50% of the radiation emitted by stars is absorbed or scattered by interstellar dust
- Infrared emission: absorbed energy is released as thermal radiation
- Regulates the physical and chemical conditions of the interstellar gas (e.g. formation of molecules)
- Plays a key role in the formation of stars and planetary systems

# Interstellar dust

## Origin

- Birth in evolved stars with extended shells; possibly also in novae and supernovae
- Accretion of gas atoms and coagulation of grains in cold clouds

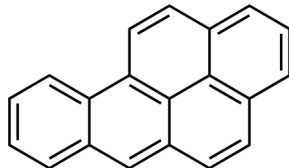
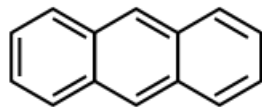
## Destruction

- Star formation, hot gas, shocks
- Sputtering by high energy radiation
- Evaporation at high temperature
- Shattering in grain-grain collisions

# Interstellar dust

## Composition

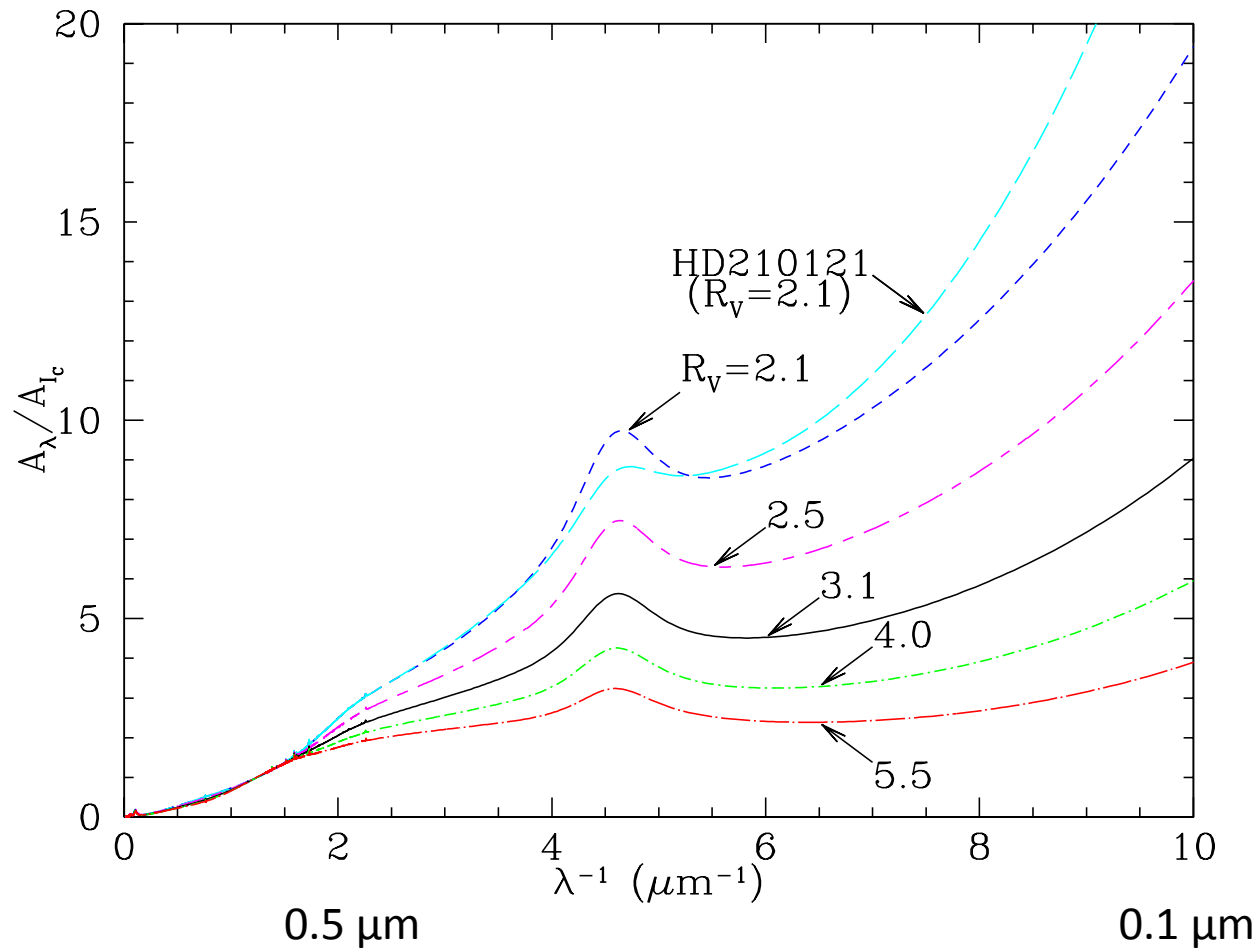
- Graphite (amorphous carbon)
- Silicates: amorphous or crystalline
  - » e.g. Enstatite ( $\text{MgSiO}_3$ ), Forsterite ( $\text{Mg}_2\text{SiO}_4$ )
- PAH molecules (polycyclic aromatic hydrocarbon)



## Grain size

- 1/3 nm (a few atoms) up to 1/3 micron
- “Logarithmic” size distribution
- Irregular shapes

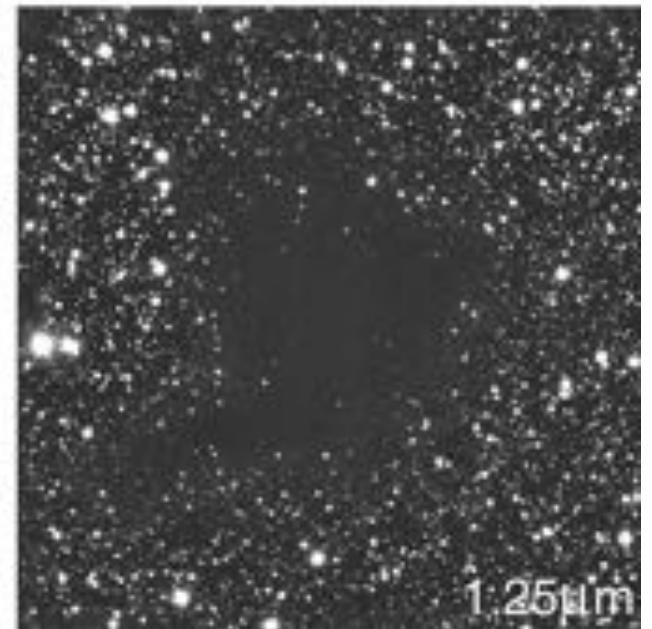
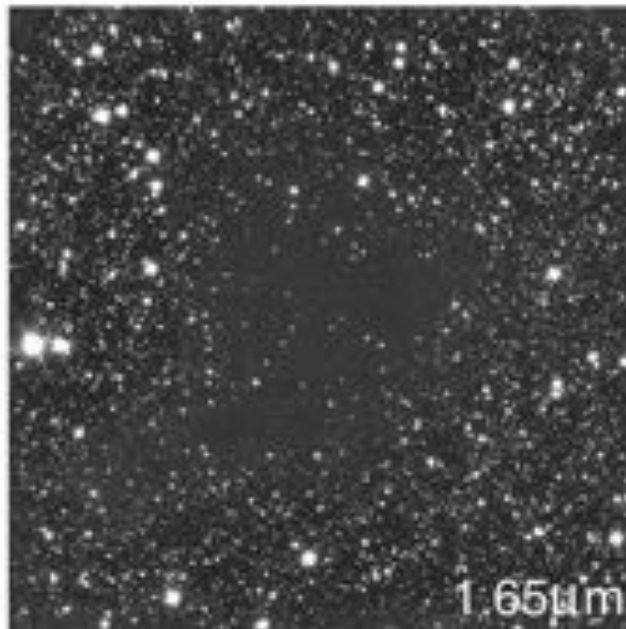
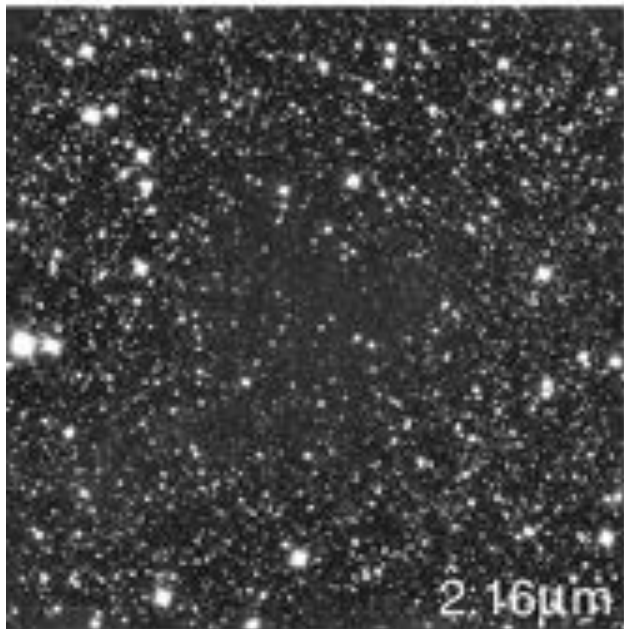
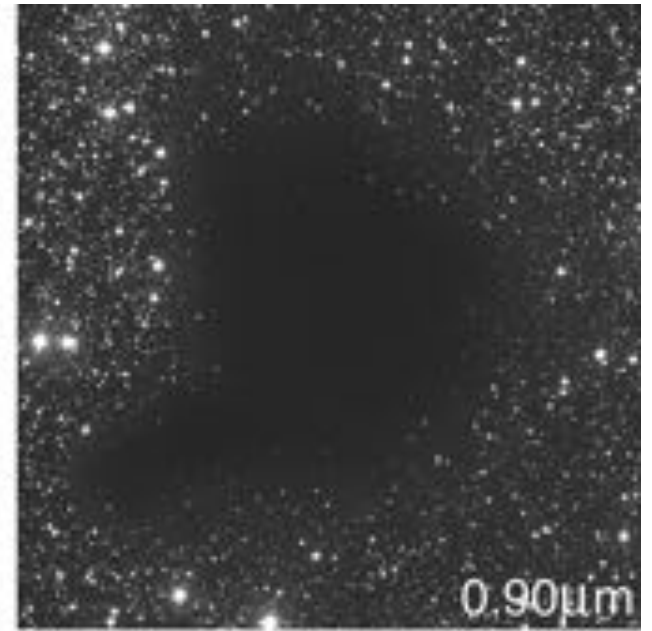
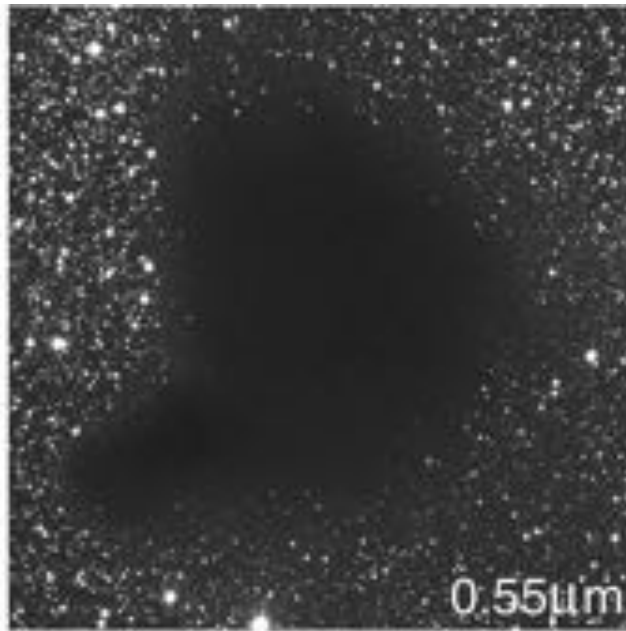
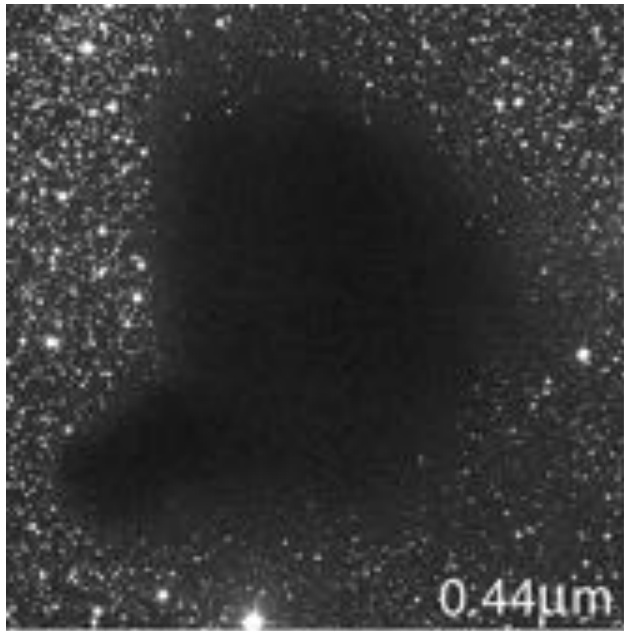
# Extinction curve



- Extinction rapidly decreases with wavelength
- Dependency is highly nonlinear

*Draine 2003*

# Reddening



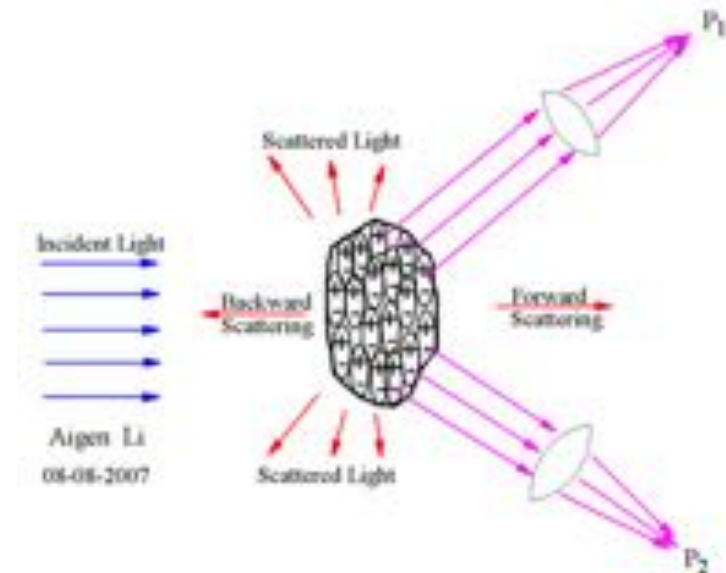
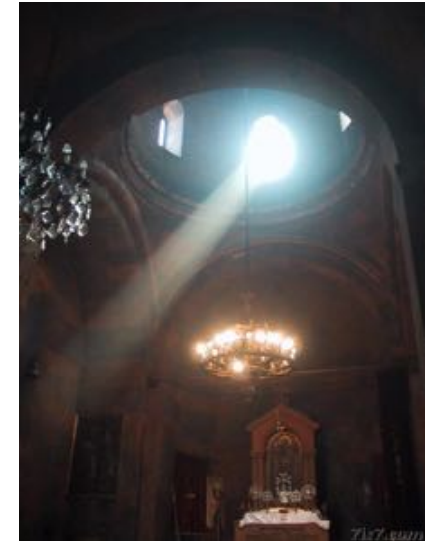
# Absorption and scattering

Two sink terms (extinction processes) to be considered in dust RT:

- **absorption:** dust grain absorbs the radiative energy (the photon) and converts it to internal energy
- **scattering:** dust grain changes the propagation direction of a photon

Absorption and scattering can be characterized by the absorption and scattering coefficients (depend on the size, shape and chemical composition of the dust grains)

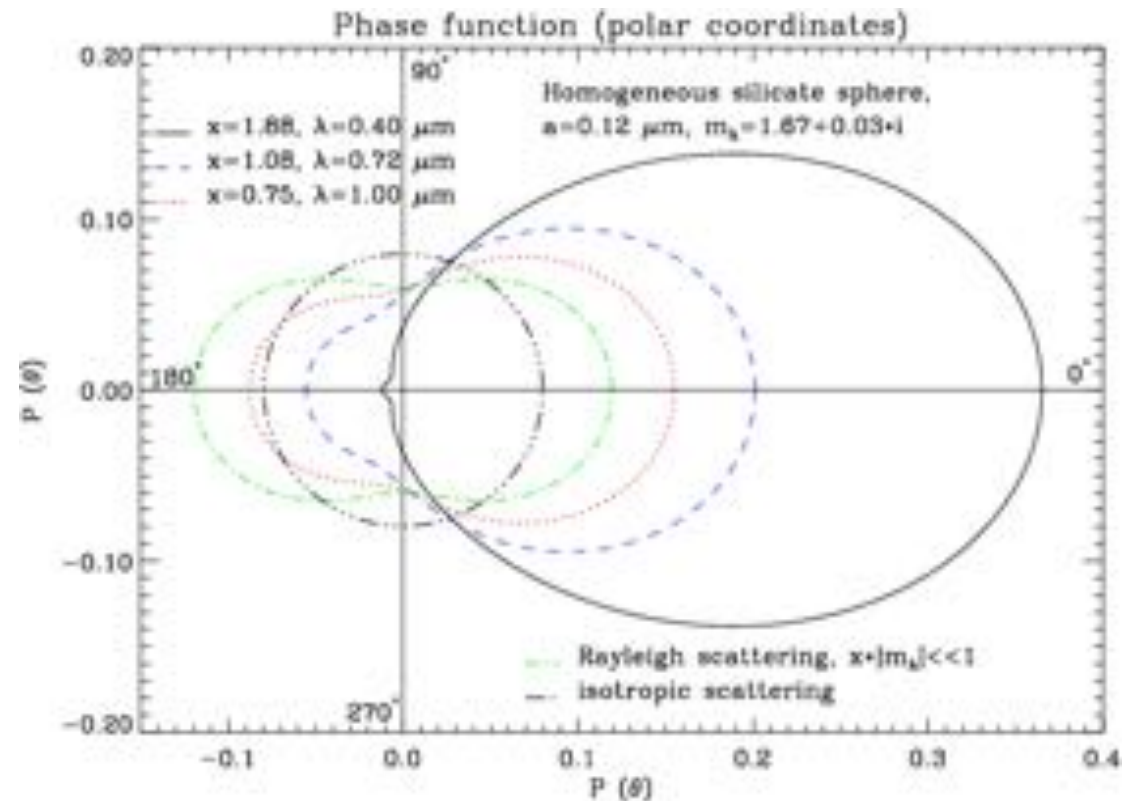
$$\kappa_{\lambda} = \kappa_{\lambda}^{\text{abs}} + \kappa_{\lambda}^{\text{sca}}$$



# Scattering phase function

Scattering redirects photons into another direction, so it is both a sink and a source term.

The phase function  $\Phi_\lambda(\mathbf{k}, \mathbf{k}')$  describes the probability that a photon coming from direction  $\mathbf{k}'$  will have  $\mathbf{k}$  as its new propagation direction.



Scattering off dust grains is anisotropic and generally forward. The scattering function typically depends only on the angle between incoming and outgoing direction.



# Henyey-Greenstein phase function

The most widely used phase function =  
Henyey-Greenstein phase function

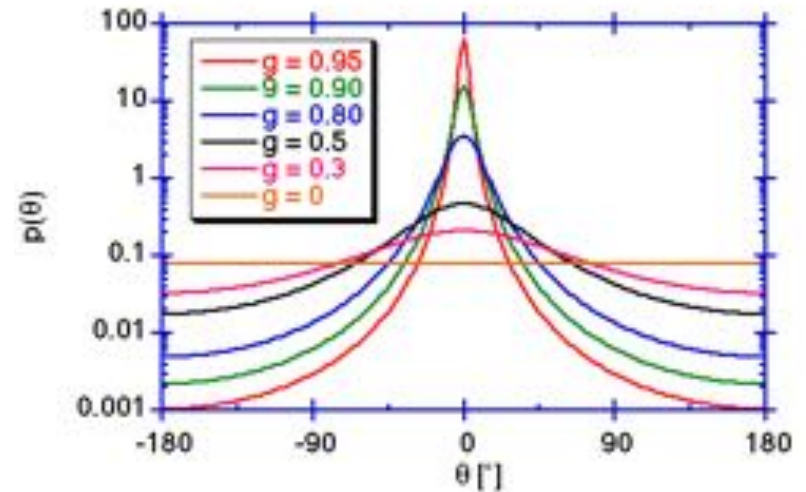
$$\Phi_\lambda(\cos \alpha) = \frac{1}{4\pi} \frac{1 - g_\lambda^2}{(1 + g_\lambda^2 - 2g_\lambda \cos \alpha)^{3/2}}$$

Contains one free parameter: the  
asymmetry parameter  $g_\lambda$ ,

$$g_\lambda = \int \Phi_\lambda(\cos \alpha) \cos \alpha \, d\Omega$$

The asymmetry parameter  $g_\lambda$ , can be defined for any phase function, but the HG phase function contains it as an explicit parameter.

- $g_\lambda = 0$ : isotropic scattering
- $g_\lambda = 1$ : completely forward scattering
- $g_\lambda = -1$ : completely backward scattering



# How to trace interstellar dust (1)

## Model the extinction

- Stellar emission
- Absorption and multiple anisotropic scattering by dust

## Issues

- 6 dimensions (3 position, 2 direction, 1 wavelength) even when assuming time-independence
- Non-local
- Non-linear
- Complicated geometry (3D, inhomogeneous...)
- Optical properties of the dust are poorly known

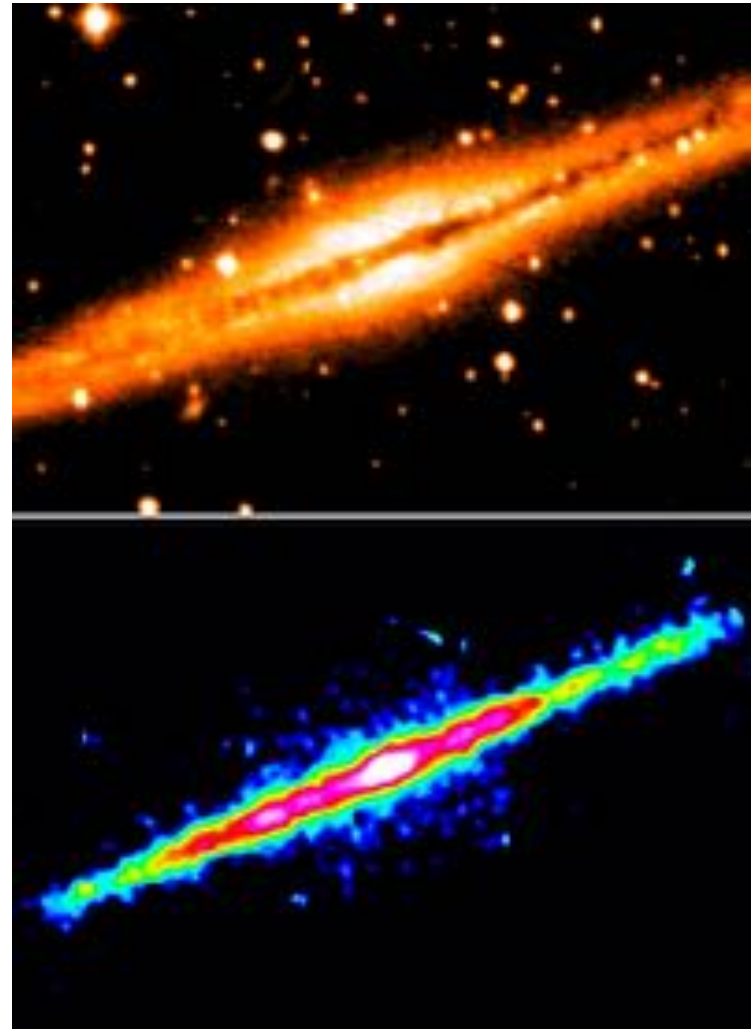
## How to trace interstellar dust (2)

Energy balance: dust grains emit the energy they absorb

$$\int_0^{\infty} \kappa_{\lambda}^{\text{abs}} J_{\lambda} d\lambda = \int_0^{\infty} \kappa_{\lambda}^{\text{abs}} B_{\lambda}(T_d) d\lambda$$

Realistic values in the interstellar medium yield temperatures of 15-30 K. The corresponding emission peaks in the far-infrared or submm range (on the order of 100  $\mu\text{m}$ ).

**Interstellar dust effectively converts optical/UV starlight to FIR/submm emission.**



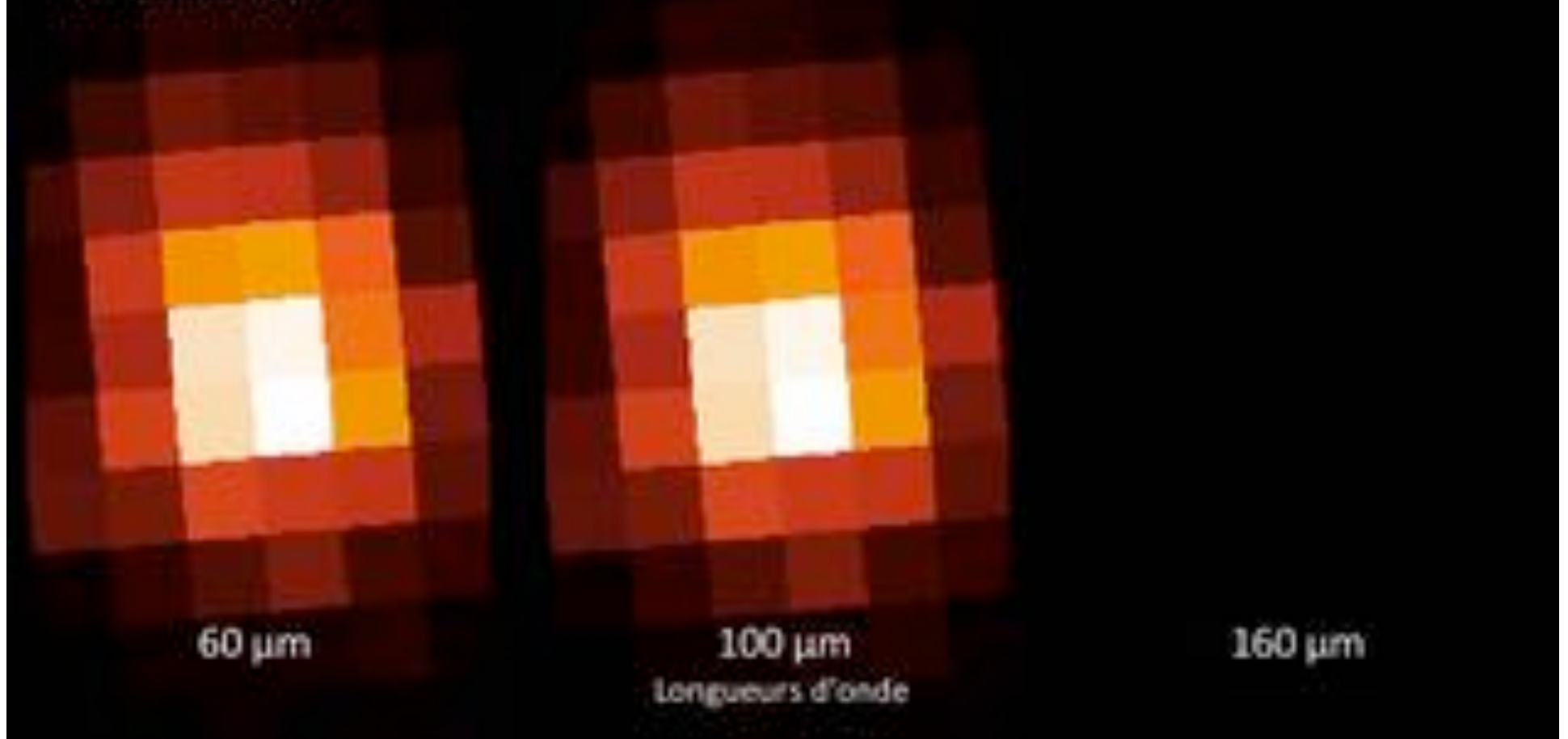


*Fritz et al. 2012*

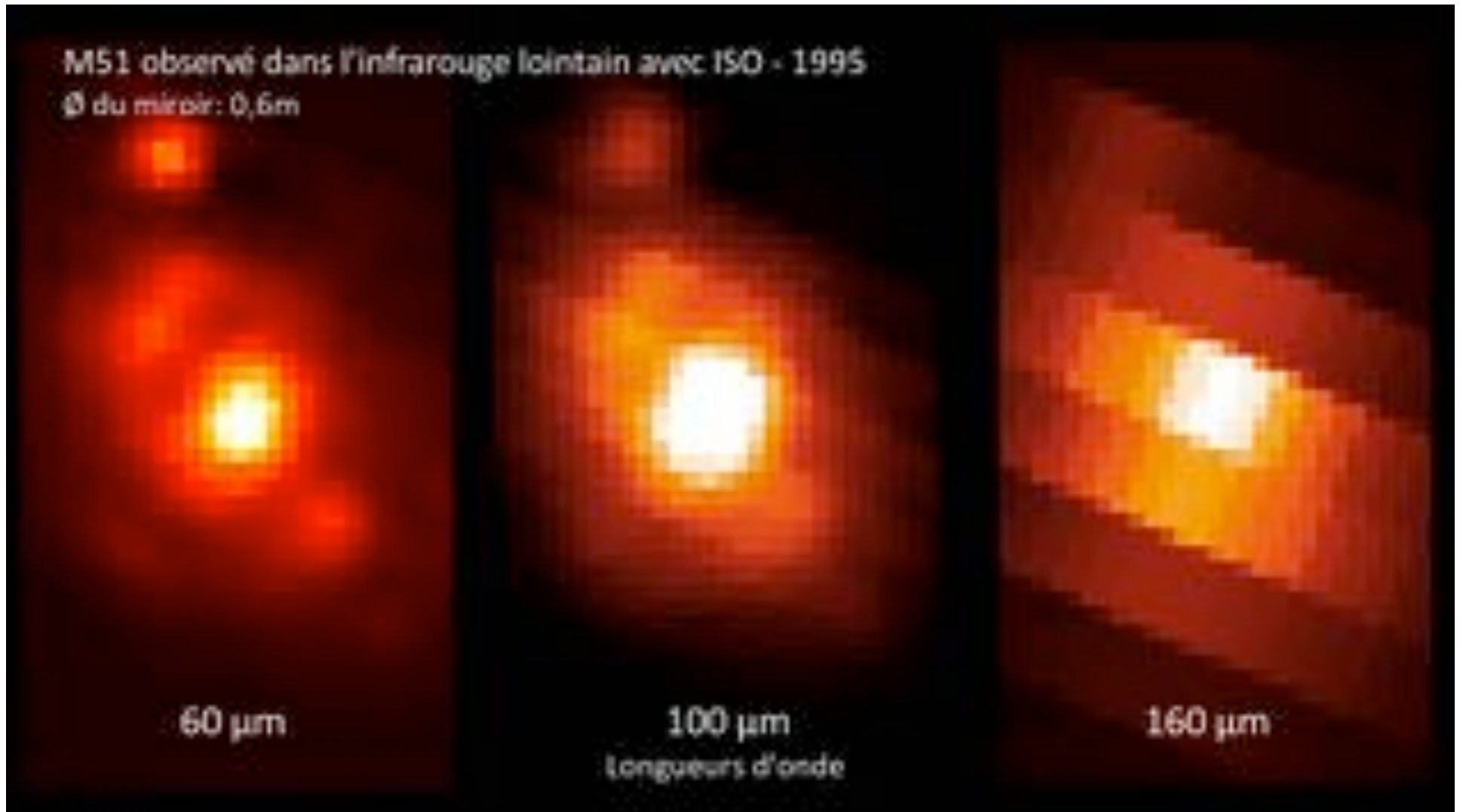
# M51 with IRAS

M51 observé dans l'infrarouge lointain avec IRAS - 1983

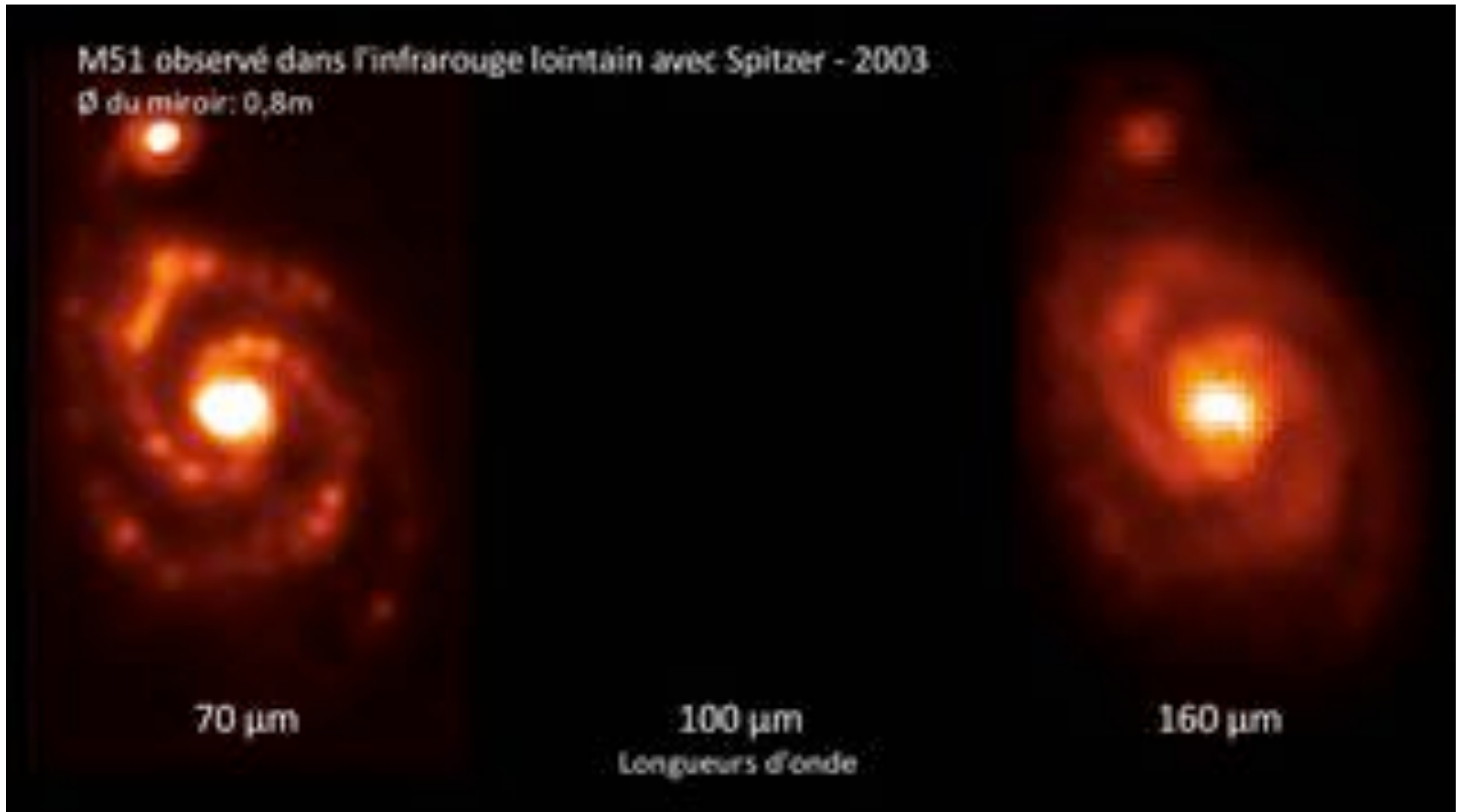
Ø du miroir: 0,5m



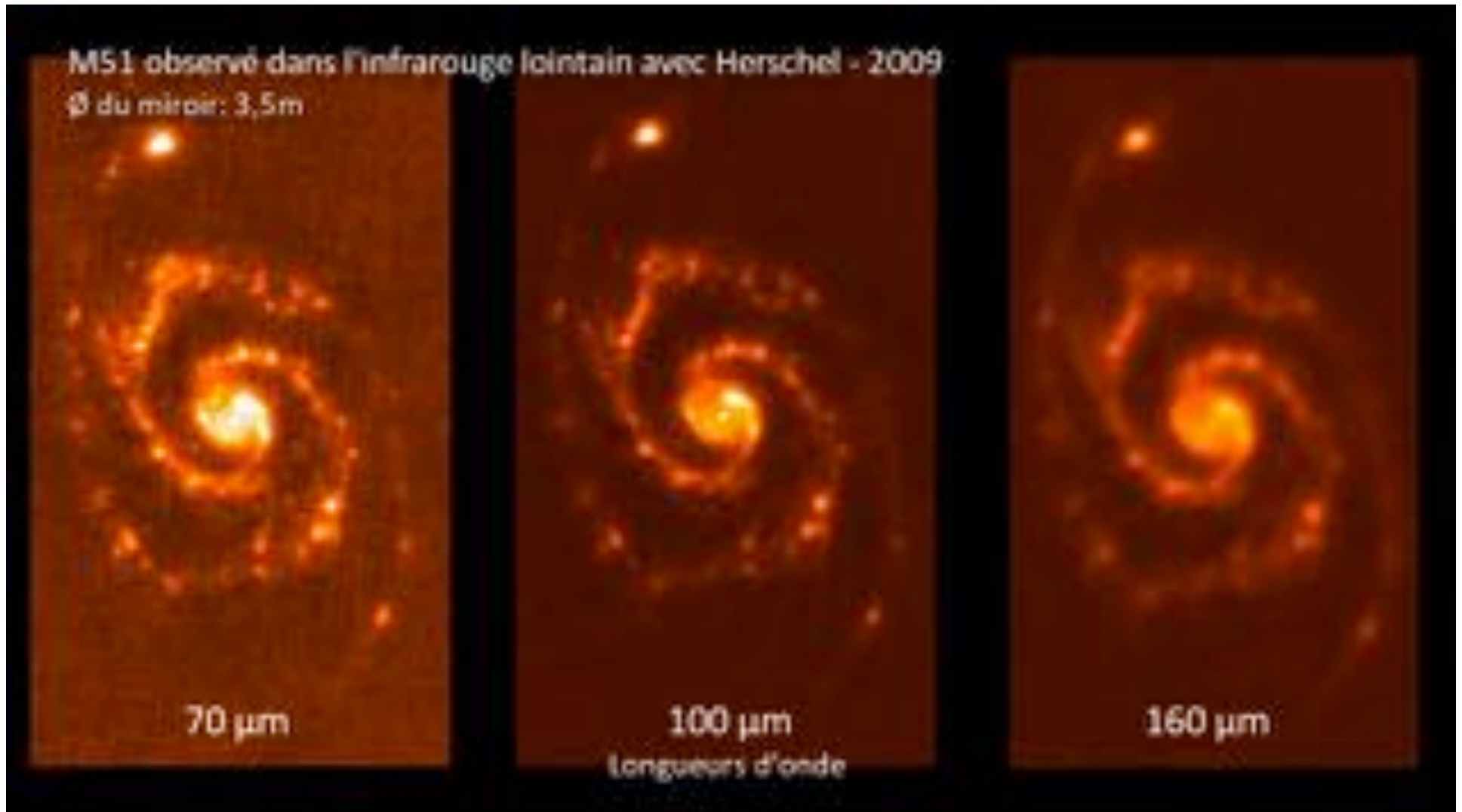
# M51 with ISO



# M51 with Spitzer

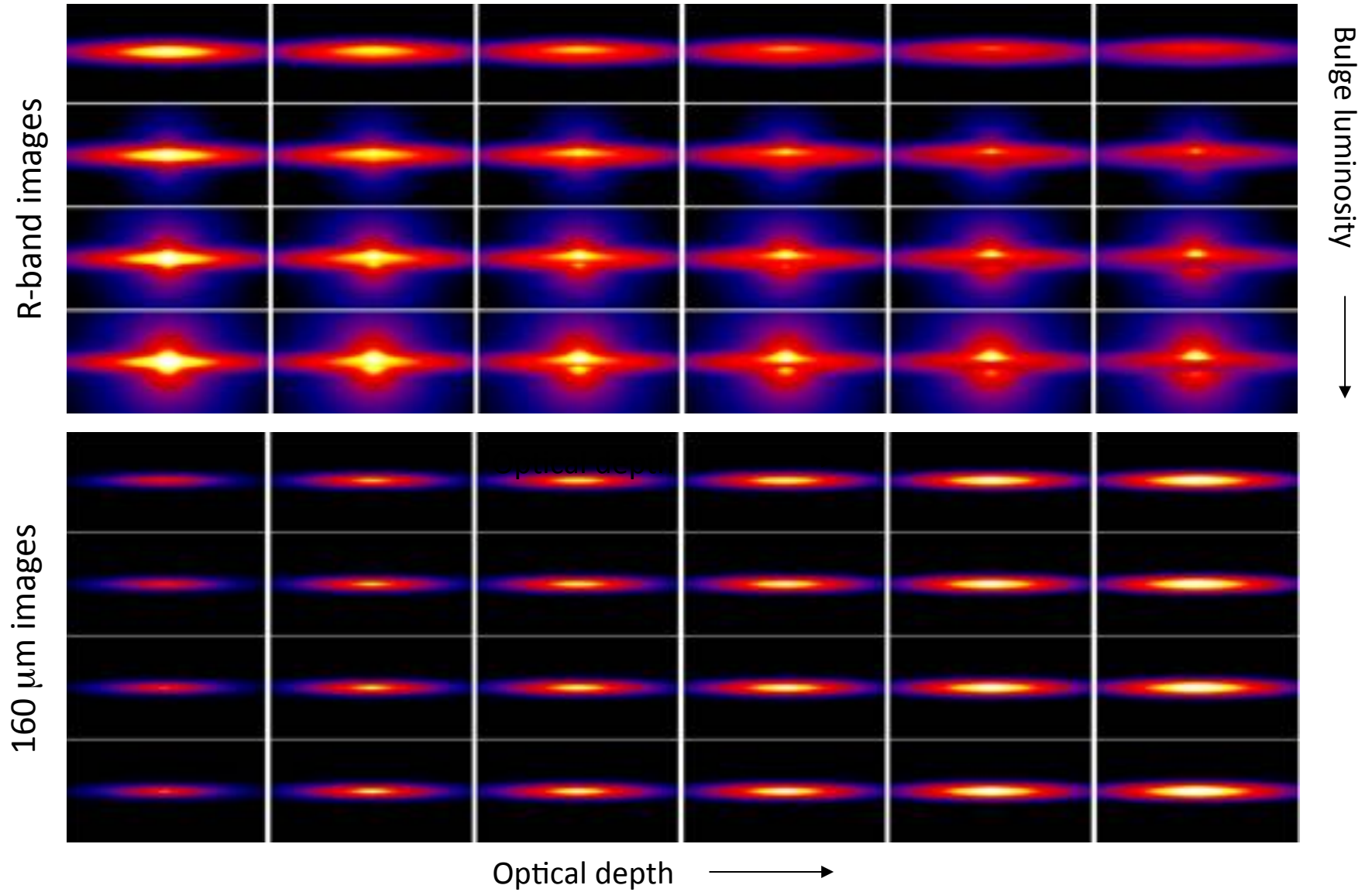


# M51 with Herschel

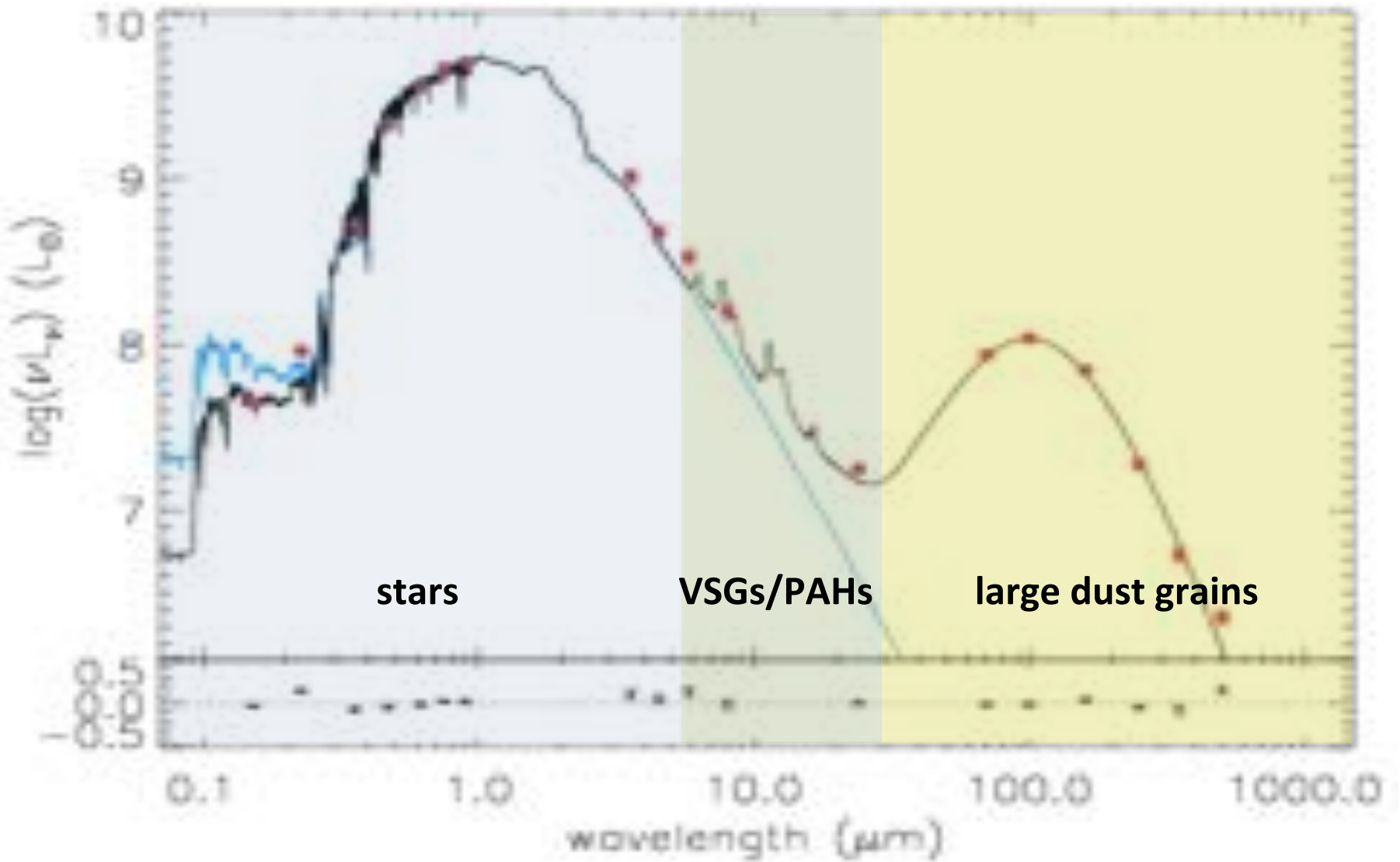




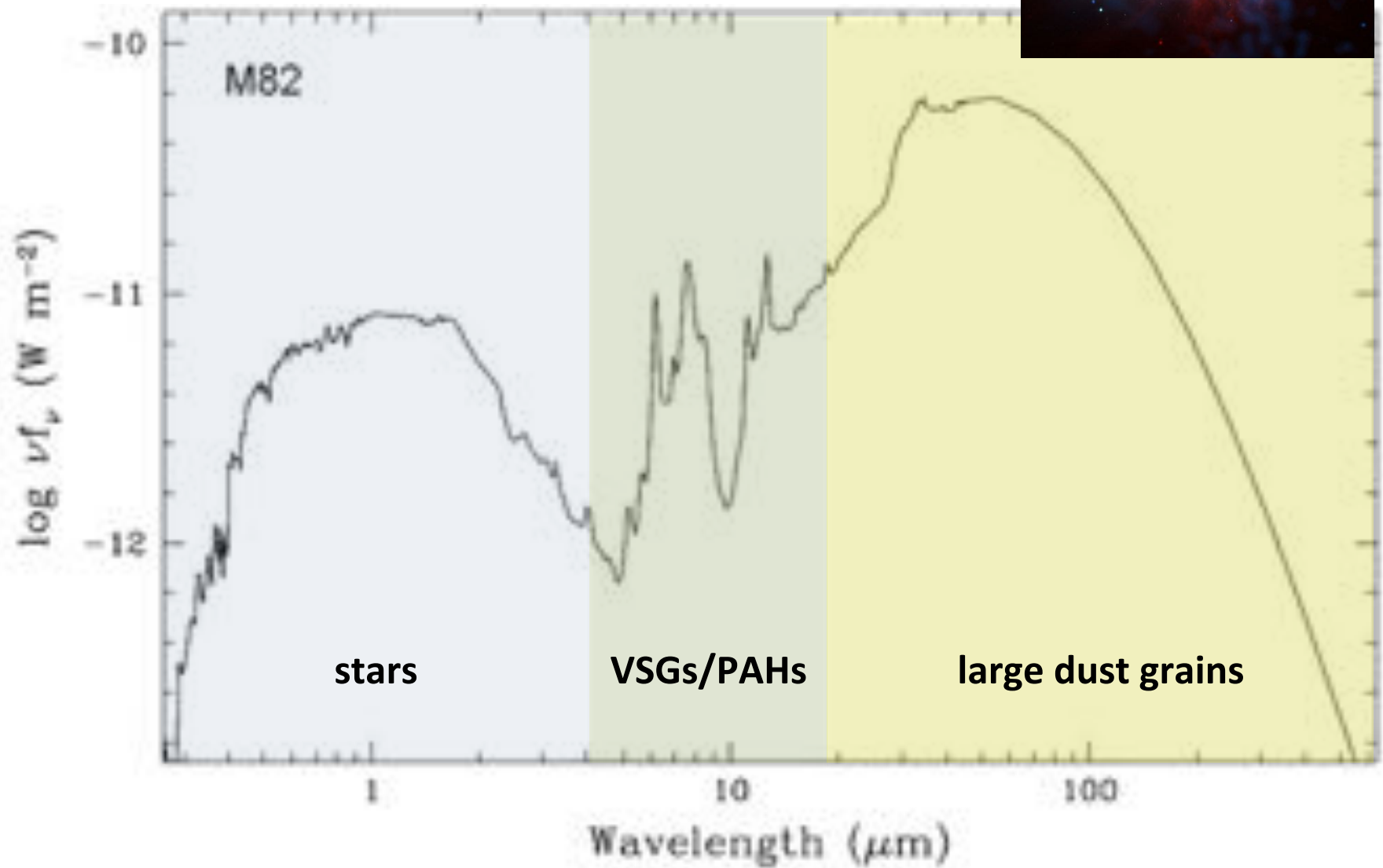
# Dust heating in spiral galaxies



# M31 SED



# M82 SED

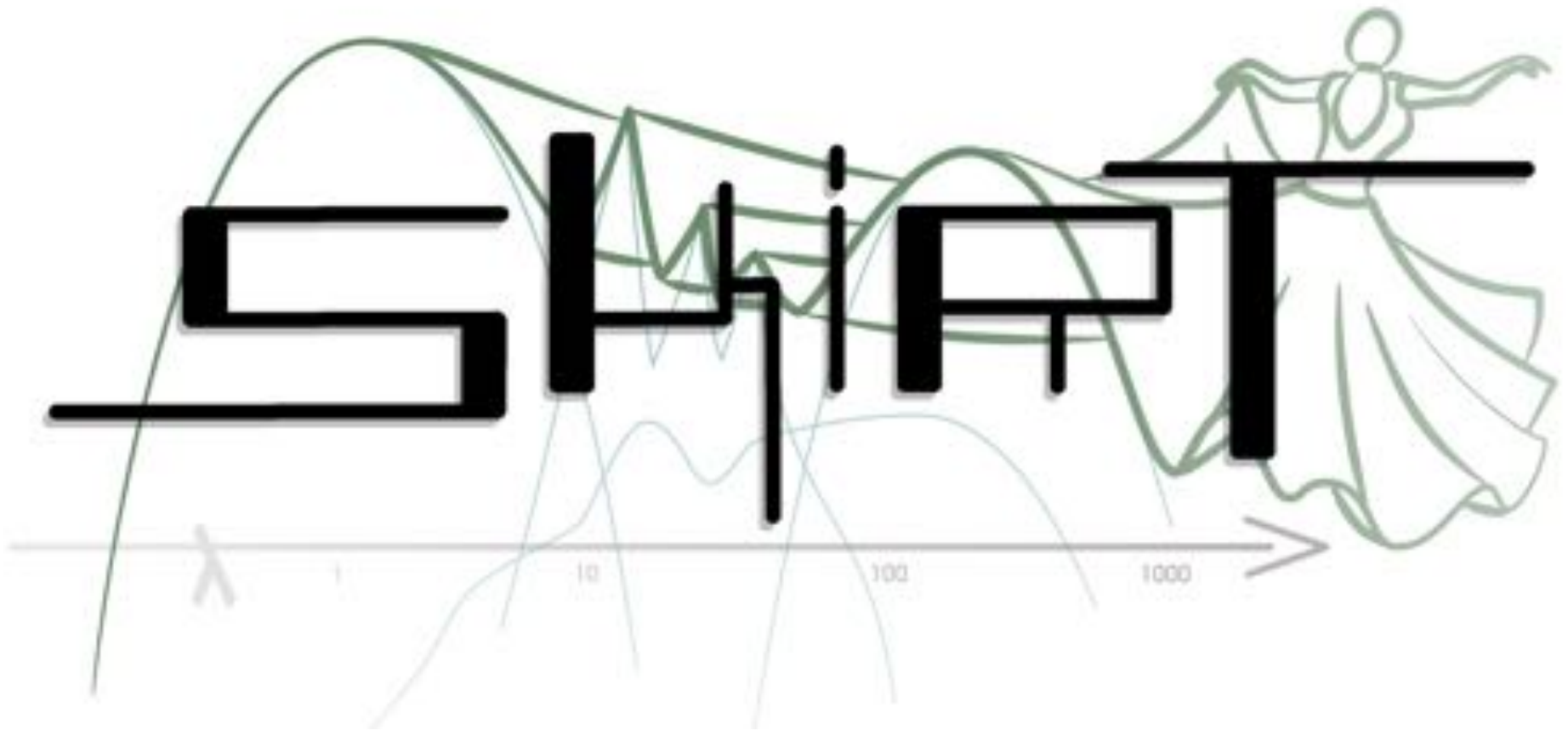


Questions ?



# SKIRT features and code design

Section A-2



[www.skirt.ugent.be](http://www.skirt.ugent.be)  
[github.com/skirt](https://github.com/skirt)

# Key features



## **Monte Carlo continuum radiative transfer**

- Absorption, scattering, and re-emission by dust
- Self-consistent calculation of dust temperature
- Stochastic heating of dust grains

## **Acceleration techniques**

- Biased emission, forced scattering, continuous absorption, peel-off towards instruments
- Hybrid parallelization (shared & distributed memory)

## **Arbitrary geometries & properties for stars and dust**

- Many built-in components, configured at run-time
- Import snapshot from hydrodynamic simulation

# Application focus

## *Compare models to observations*

- Images and emission spectrum

## **Dust in spiral galaxies**

- Geometry and structure
- Energy balance
- Scaling relations

## **Other applications**

- Dust torus in active galactic nuclei
- Molecular clouds
- Dusty outflows from (binary) stars





# Infrastructure



open source



- Open source
- Published on GitHub ([github.com/skirt](https://github.com/skirt))
- Fully documented ([www.skirt.ugent.be](http://www.skirt.ugent.be))
- Written in C++11 (75000 lines in 300 classes)
- Uses Qt 5.x libraries and tools
- Optional use of MPI (multi-node parallelization)
- No other dependencies
- Well tested (200+ regression test cases)

# Configurable built-in options

skirt

skirt <ski-filename>

```
Welcome to SKIRT v7 (git 525-a714d03 built on Aug 5 2015)
Running on obiwan.ugent.be for pcamps
Interactively constructing a simulation...
? Enter the name of the ski file to be created: test
Possible choices for the simulation:
  1. An oligochromatic Monte Carlo simulation
  2. A panchromatic Monte Carlo simulation
? Enter one of these numbers [1,2] (1): 2
```

<PanDustSystem

writeDensity="true"

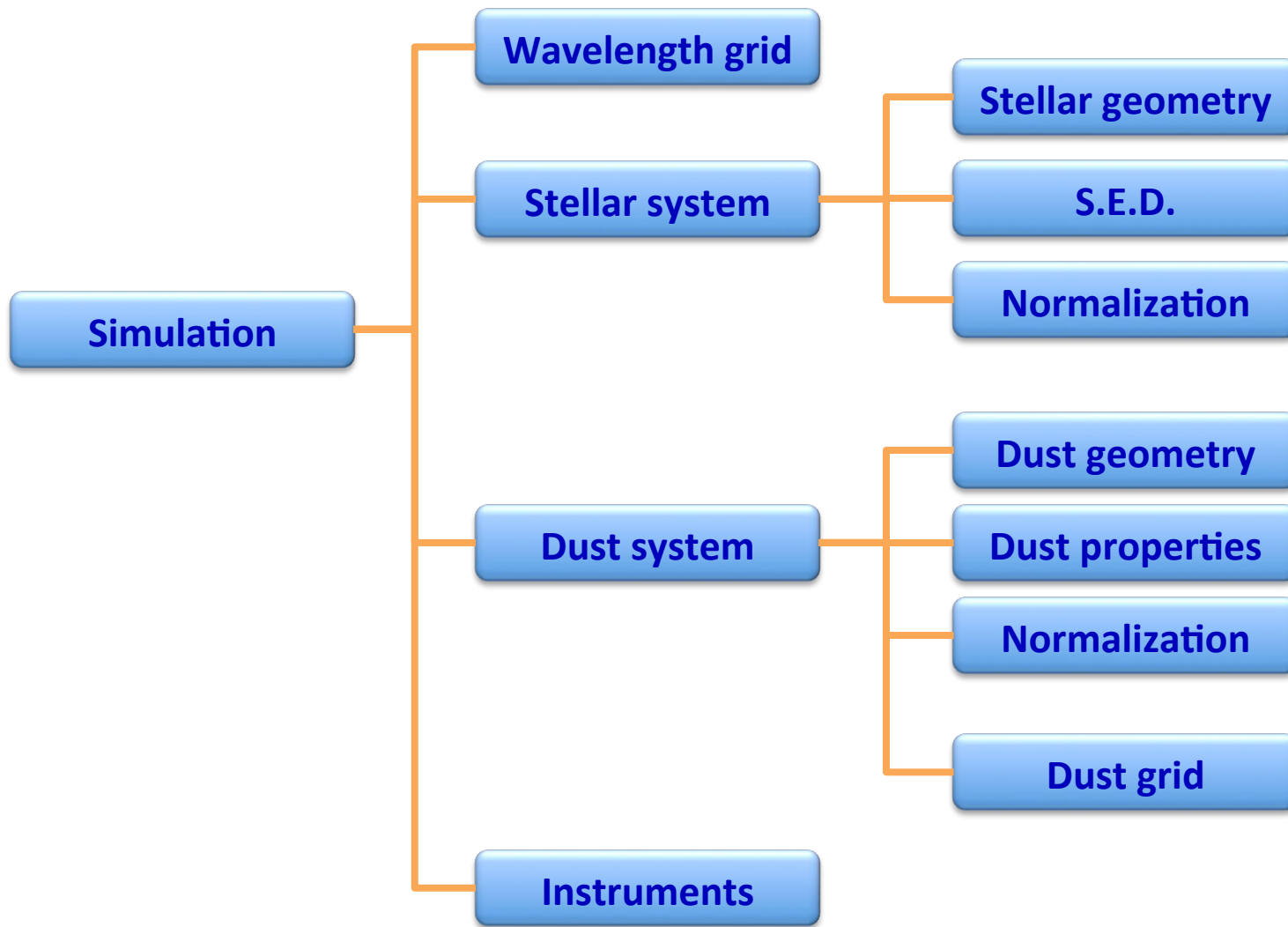
dustEmission="true"

transient="false"

selfAbsorption="false">

- Command-line interface
- Q&A session to **create** configuration file
- XML-based configuration file
  - Easy to **adjust** in editor
  - **Upgradable** by automatic process

# Simulation structure



# Instruments



Instrument name	SED	Frame	Sources Separated
<i>DistantInstrument</i>			
SEDInstrument	✓	--	--
FrameInstrument	--	✓	--
SimpleInstrument	✓	✓	--
FullInstrument	✓	✓	✓
PerspectiveInstrument	--	✓	--

# Geometries

## Basic (often symmetric)

Point

Plummer

Gamma

Sersic

Einasto

Shell

Ring

Torus

Exponential disk

Cuboid

Multi-Gaussian expansion

## Hydro snapshots

AMR (adaptive mesh)

SPH (smoothed particles)

## Decorators

Offset

Rotation

Spheroidal distortion

Triaxial distortion

Spherical cavity

Cylindrical cavity

Crop

Add spiral arms

Make clumpy

Combine

## Anisotropic sources

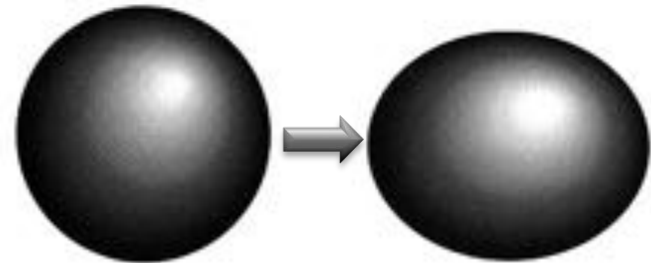
Laser

Netzer accretion disk

Spherical surface

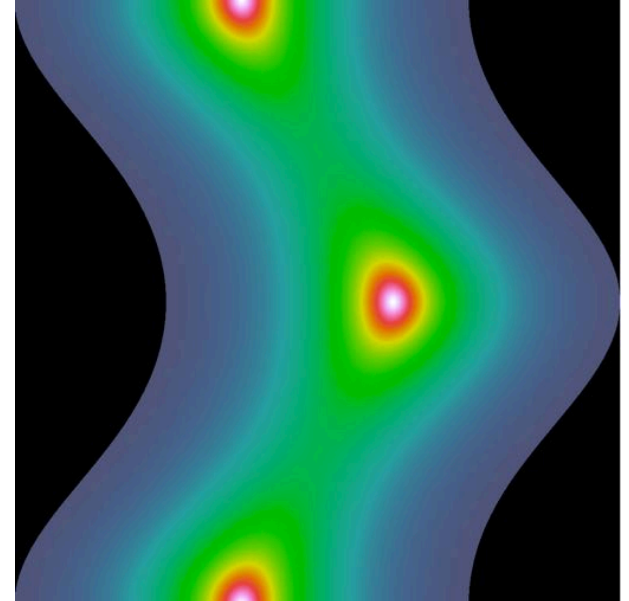
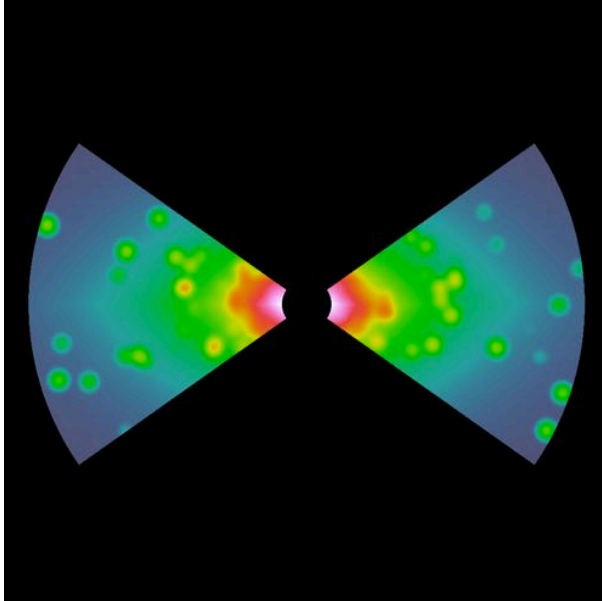
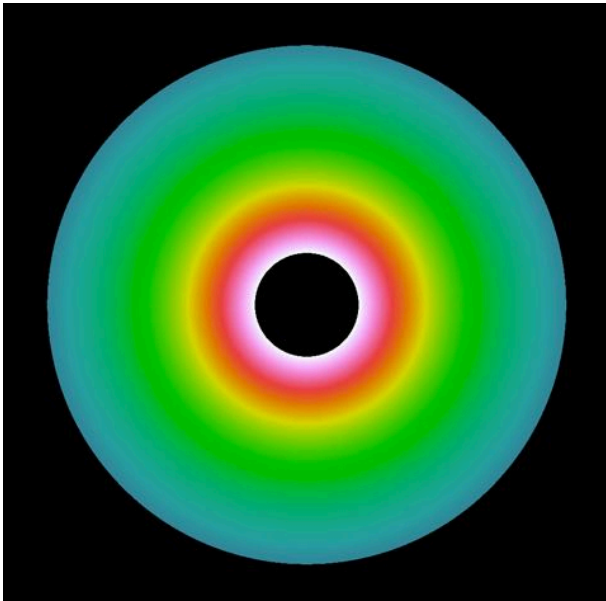
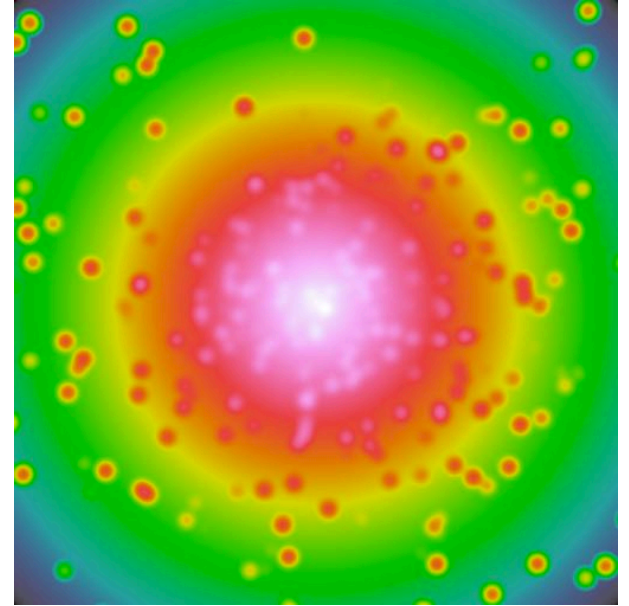
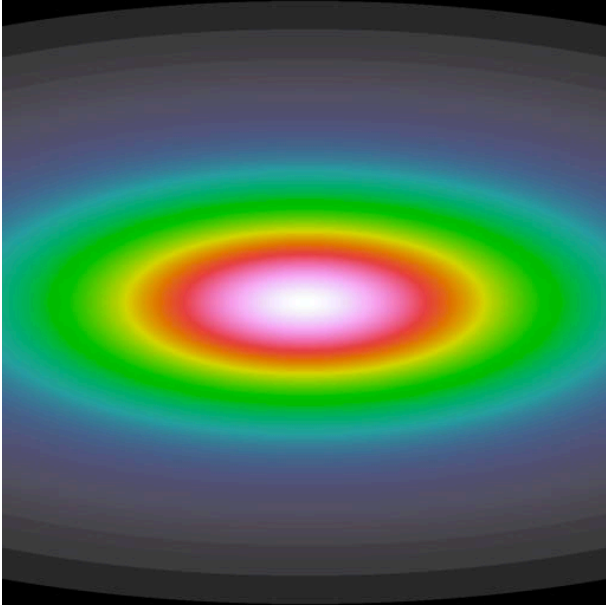
Spherical background

- A geometry defines a spatial density distribution
- All geometries can be used for both **stellar** and **dust** distributions
- **Decorators** serve to adjust and combine other geometries



- Decorators can be **nested** to arbitrary levels

# Geometries

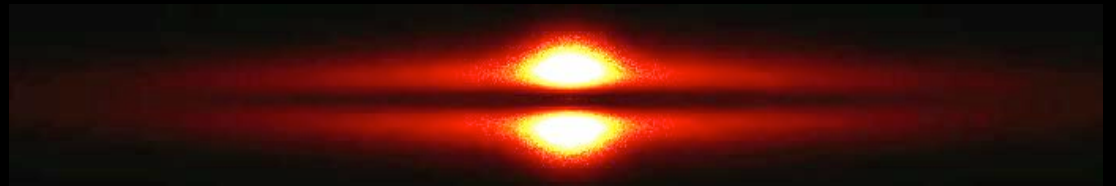


# Geometries

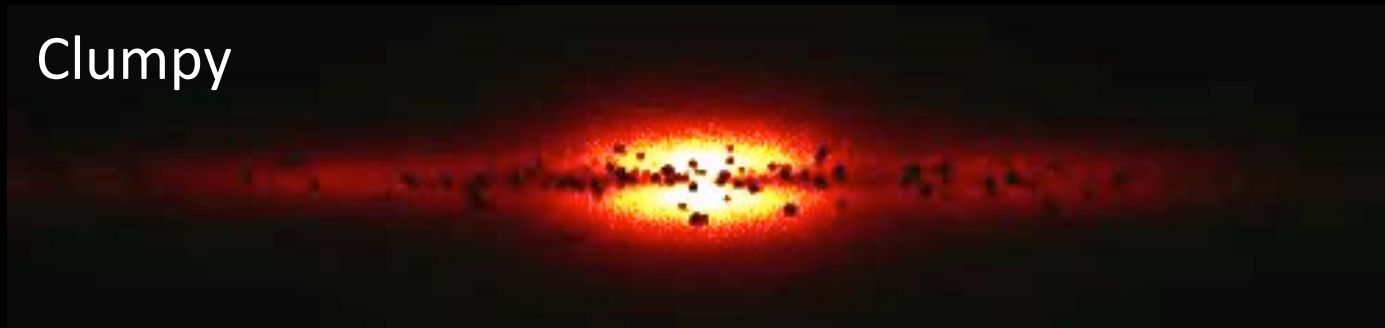
Spiral arms



Peanut bulge



Clumpy



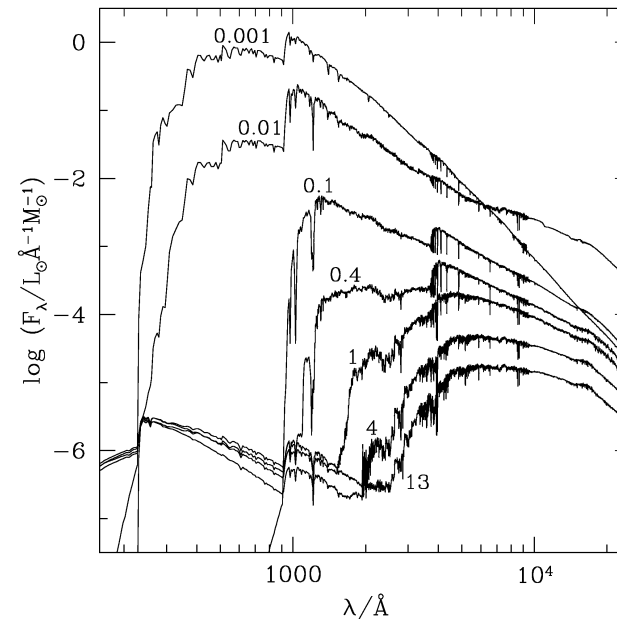
*De Geyter 2015*

# Stellar SEDs

SED
Black Body
Sun
Pegase
Quasar
Maraston
Kurucz
Bruzual-Charlot
Starburst (Mappings)
File

SED family
Bruzual-Charlot
Starburst (Mappings)

- An SED is assigned to each stellar geometry



*Bruzual & Charlot 2003*

- An SED family allows each particle/cell in an imported hydro **snapshot** to be assigned its own spectrum based on its properties (e.g. metallicity, age)



# Dust properties

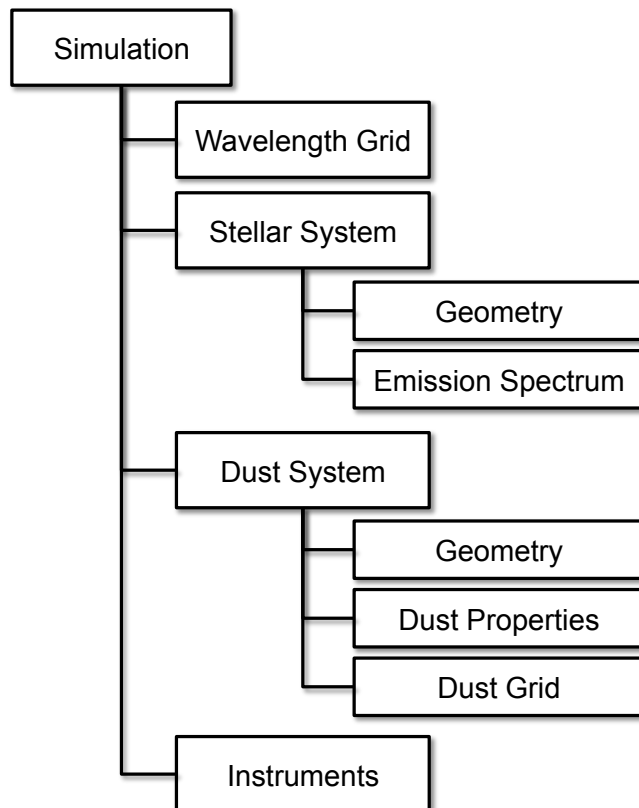
Turn-key dust mixture	Configurable dust mixture	
Draine & Li 2007	<b>Grain composition</b>	<b>Grain size distribution</b>
MRN	Graphite	LogNormal
Weingartner & Draine	Silicate	PowerLaw
Zubko et al.	Ionized PAH	ModifiedPowerLaw
	Neutral PAH	SingleGrain
	Enstatite	Zubko
	Forsterite	

- A dust system can have **multiple** dust components, each with its own geometry and dust mixture
- Turn-key dust mixtures include **pre-configured** properties
- The configurable dust mix allows specifying grain **composition** and **size distribution** in detail

# Software architecture

## Complex configuration

- » Many built-in options
- » Nontrivial structure (iteration, nesting)



How to deal with this?

**Scientific codes can benefit from careful object-oriented design**

**A non-graphical user interface can be friendly**

# Design goals

## Single point of definition

- Define user interface properties with the program logic

## Data-driven user interface

- Have the user interface adjust automatically as new features are added

## Structured parameter file

- Use human-readable self-documenting format that supports iteration and nesting

## Modularity

- Minimize dependencies through appropriate interfaces and data encapsulation

# Single point of definition in the code

```
class ClumpyGeometry : public Geometry
{
    Q_OBJECT
    Q_CLASSINFO("Title", "a geometry that adds clumpiness to any geometry")

    Q_CLASSINFO("Property", "geometry")
    Q_CLASSINFO("Title", "the geometry to which clumpiness is added")

    Q_CLASSINFO("Property", "clumpFraction")
    Q_CLASSINFO("Title", "the fraction of the mass locked up in clumps")
    Q_CLASSINFO("MinValue", "0")
    Q_CLASSINFO("MaxValue", "1")

public:
    Q_INVOKABLE void setGeometry(Geometry* value);
    Q_INVOKABLE Geometry* geometry() const;

    Q_INVOKABLE void setClumpFraction(double value);
    Q_INVOKABLE double clumpFraction() const;

    ...
};
```

Property  
name

Human readable  
title

Value  
restrictions

Data type

# Data-driven “Q&A” user interface

```
$ skirt
? Enter the name of the ski file to be created: spiralgalaxy
Possible choices for the simulation:
  1. An oligochromatic Monte Carlo simulation
  2. A panchromatic Monte Carlo simulation
? Enter one of these numbers [1,2] (1): 1
Possible choices for the units system:
  1. SI units
  2. Stellar units (length in AU, distance in pc)
  3. Extragalactic units (length in pc, distance in Mpc)
? Enter one of these numbers [1,3] (3):
? Enter the number of photon packages per wavelength [0,2e13] (1e6): 1e7
Possible choices for the wavelength grid:
  1. A list of one or more distinct wavelengths
Automatically selected the only choice: 1
? Enter the wavelengths [0.0001 micron,1e6 micron]: 0.55
Possible choices for the stellar system:
  1. A stellar system composed of various stellar components
  2. A stellar system derived from an SPH output file
  ...
? Enter one of these numbers [1,4] (1): 1
  ...
Possible choices for the geometry of the dust component:
  1. A point source geometry
  2. A Plummer geometry
  ...
  9. An exponential disk geometry
  ...
? Enter one of these numbers [1,26] (9): 9
```

Allowed range  
and default units

Choices derived from  
source code data

Default value

# XML-based parameter file

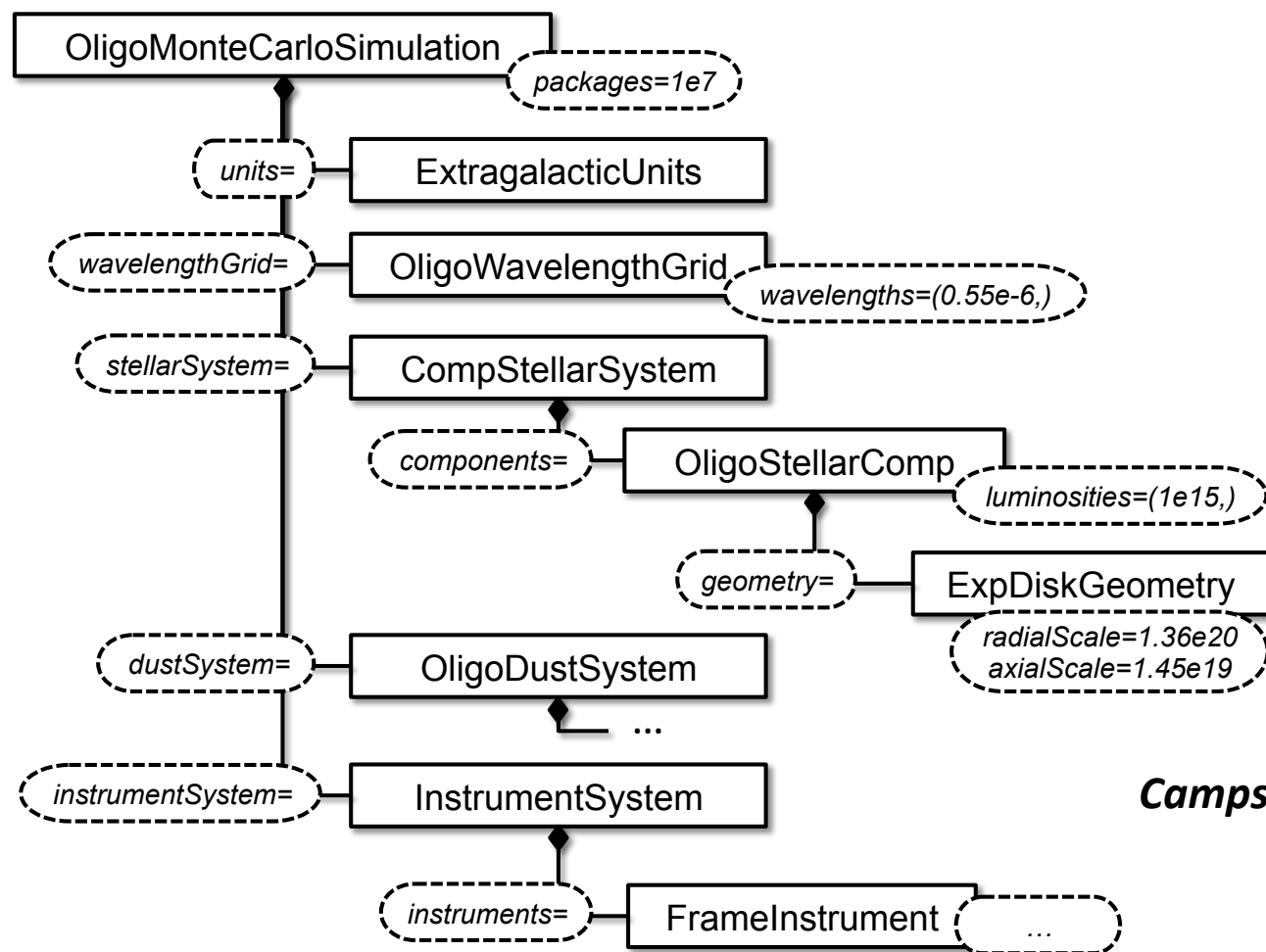
```
<?xml version="1.0" encoding="UTF-8"?>
<skirt-simulation-hierarchy type="MonteCarloSimulation" format="6.1">
  <OligoMonteCarloSimulation packages="1e7">
    <units type="Units">
      <ExtragalacticUnits/>
    </units>
    <wavelengthGrid type="OligoWavelengthGrid">
      <OligoWavelengthGrid wavelengths="0.55 micron"/>
    </wavelengthGrid>
    <stellarSystem type="StellarSystem">
      <CompStellarSystem>
        <components type="StellarComp">
          <OligoStellarComp luminosities="1e11">
            <geometry type="Geometry">
              <ExpDiskGeometry radialScale="4400 pc" axialScale="500 pc"
                radialTrunc="0 pc" axialTrunc="0 pc"/>
            </geometry>
          </OligoStellarComp>
        </components>
      </CompStellarSystem>
    </stellarSystem>
    <dustSystem type="OligoDustSystem">
      <OligoDustSystem>
        <dustDistribution type="DustDistribution">
          <CompDustDistribution>
            <components type="DustComp">
```

Supports iteration and nesting to any depth

Property names are documented

Values include units

# Run-time structure of simulation

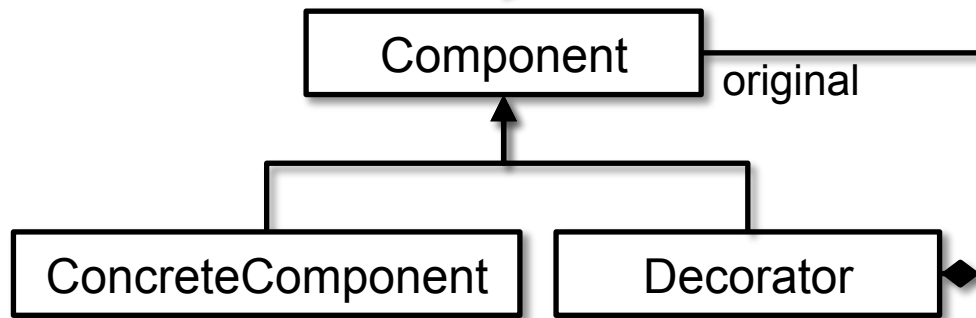


*Camps & Baes 2015*

Run-time hierarchy and parameter file have identical structure

# Geometry decorators

```
class Geometry {  
public:  
    Geometry();  
    virtual ~Geometry();  
    virtual double density(Position x) const = 0;  
    virtual Position generatePosition() const = 0;  
}
```



```
class ConcreteGeometry : public Geometry {  
public:  
    ConcreteGeometry(double p) {_p=p}  
    double density(Position x) const;  
    Position generatePosition() const;  
private:  
    double _p;  
}
```

```
class OffsetGeometryDecorator : public Geometry {  
public:  
    OffsetGeometryDecorator(Geometry* g, Position a)  
        {_g = g; _a = a;}  
    double density(Position x) const  
        {return _g->density(x-a);}  
    Position generatePosition() const  
        {return _g->generatePosition()+a;}  
private:  
    Geometry* _g;  
    Position _a;  
}
```



# Conclusion

## SKIRT

- Is a state-of-the art dust continuum RT code
- Offers a large suite of built-in components
- Includes a flexible configuration mechanism
- Allows easily adding new components

## All (scientific) codes

- Can benefit from careful object-oriented design
- Can offer a friendly user interface (even if not graphical)

Questions ?



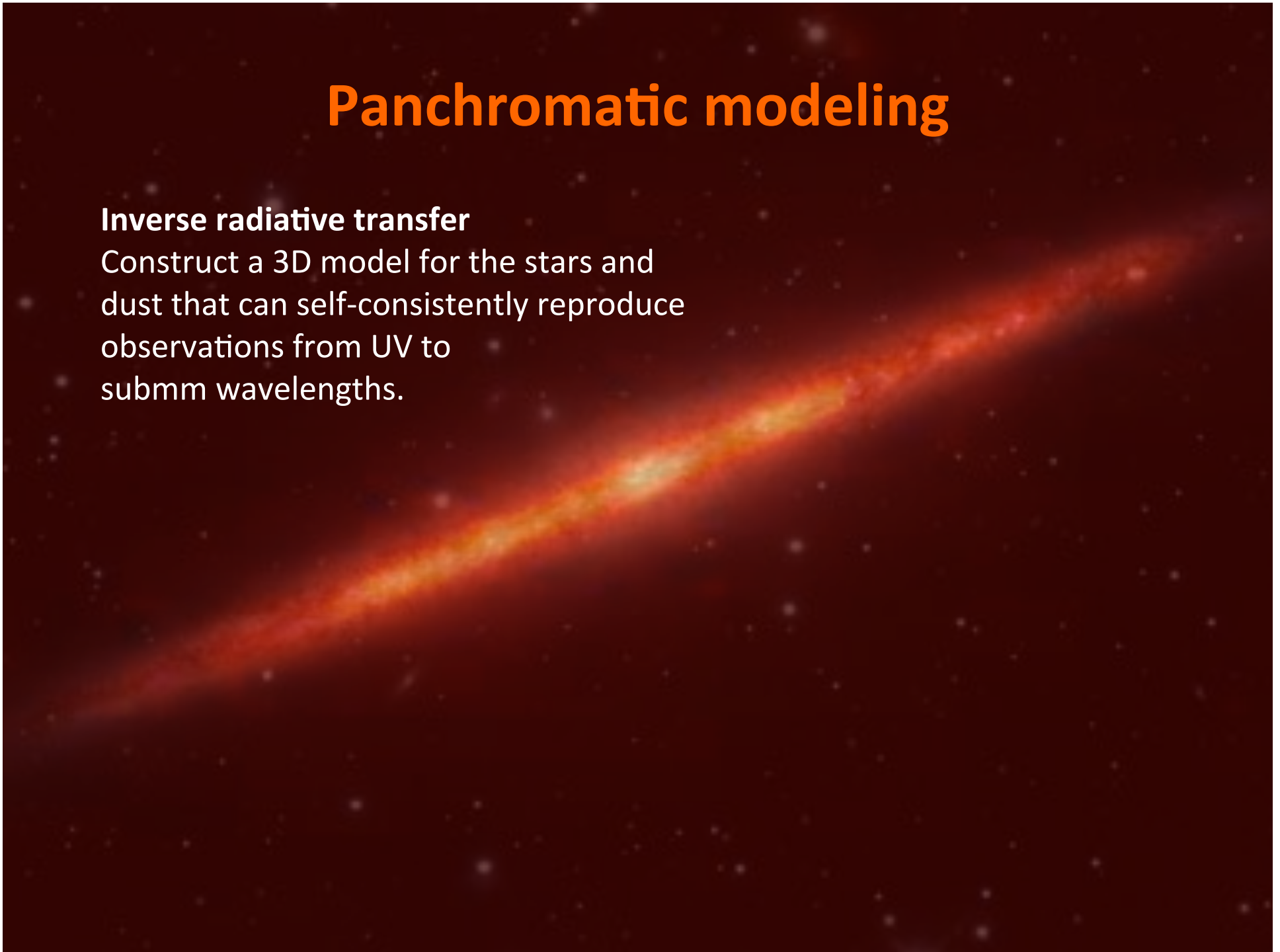
# Energy balance in galaxies

Section A-3

# Panchromatic modeling

## **Inverse radiative transfer**

Construct a 3D model for the stars and dust that can self-consistently reproduce observations from UV to submm wavelengths.



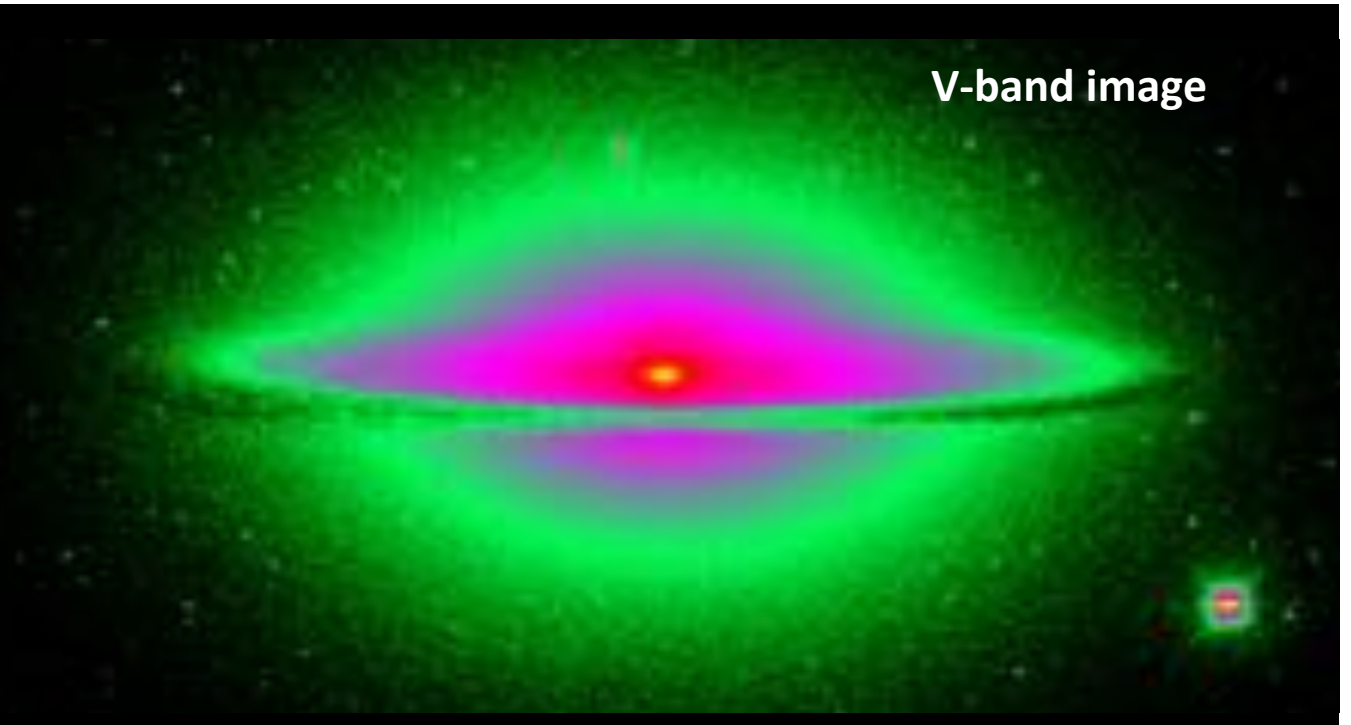
## Case study: Sombrero galaxy (NGC 4594)



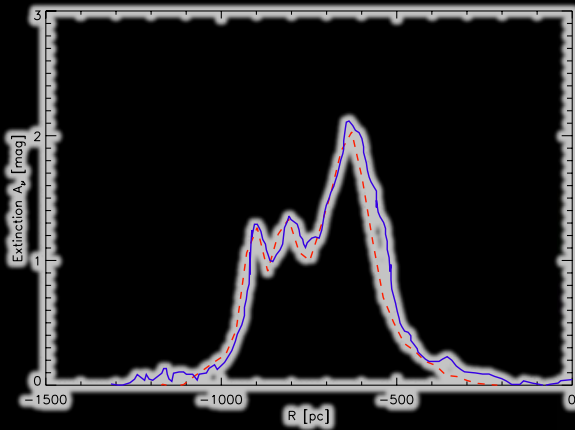
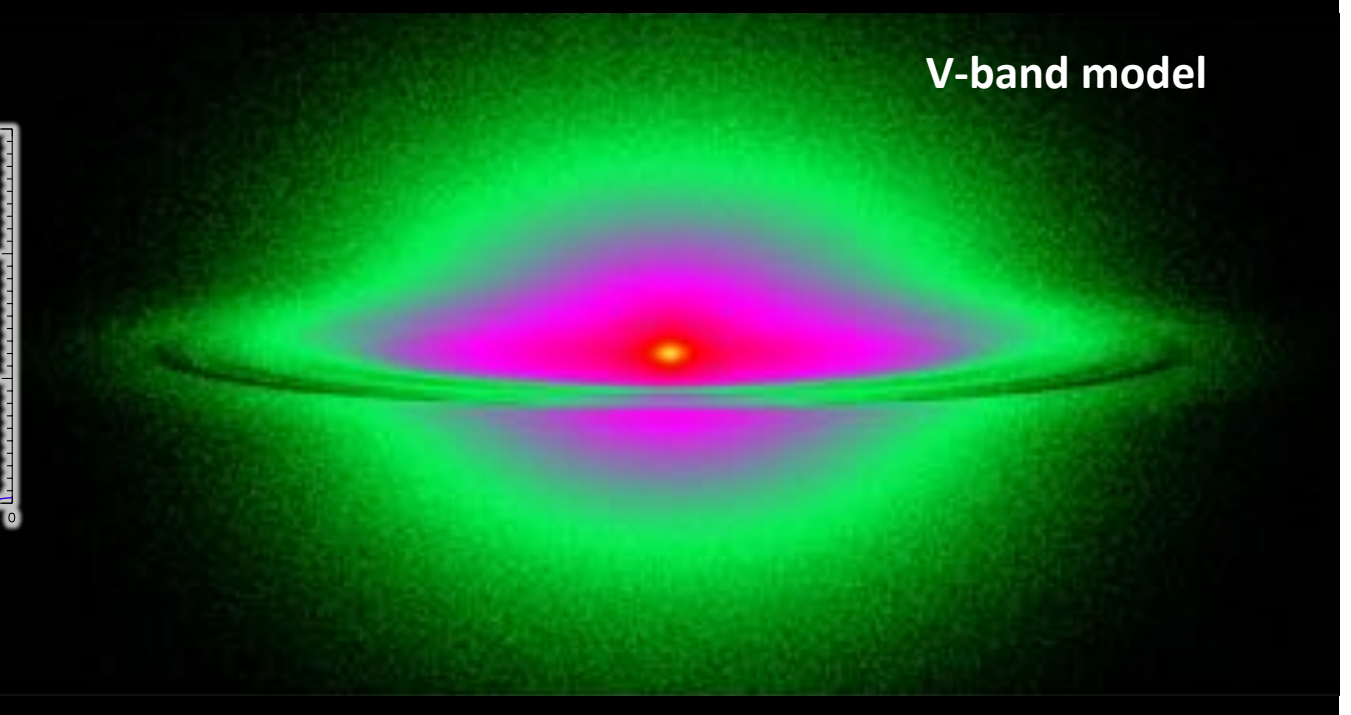
# NGC 4594

Construct a model reproducing the optical image; in particular the minor axis intensity profile

V-band image

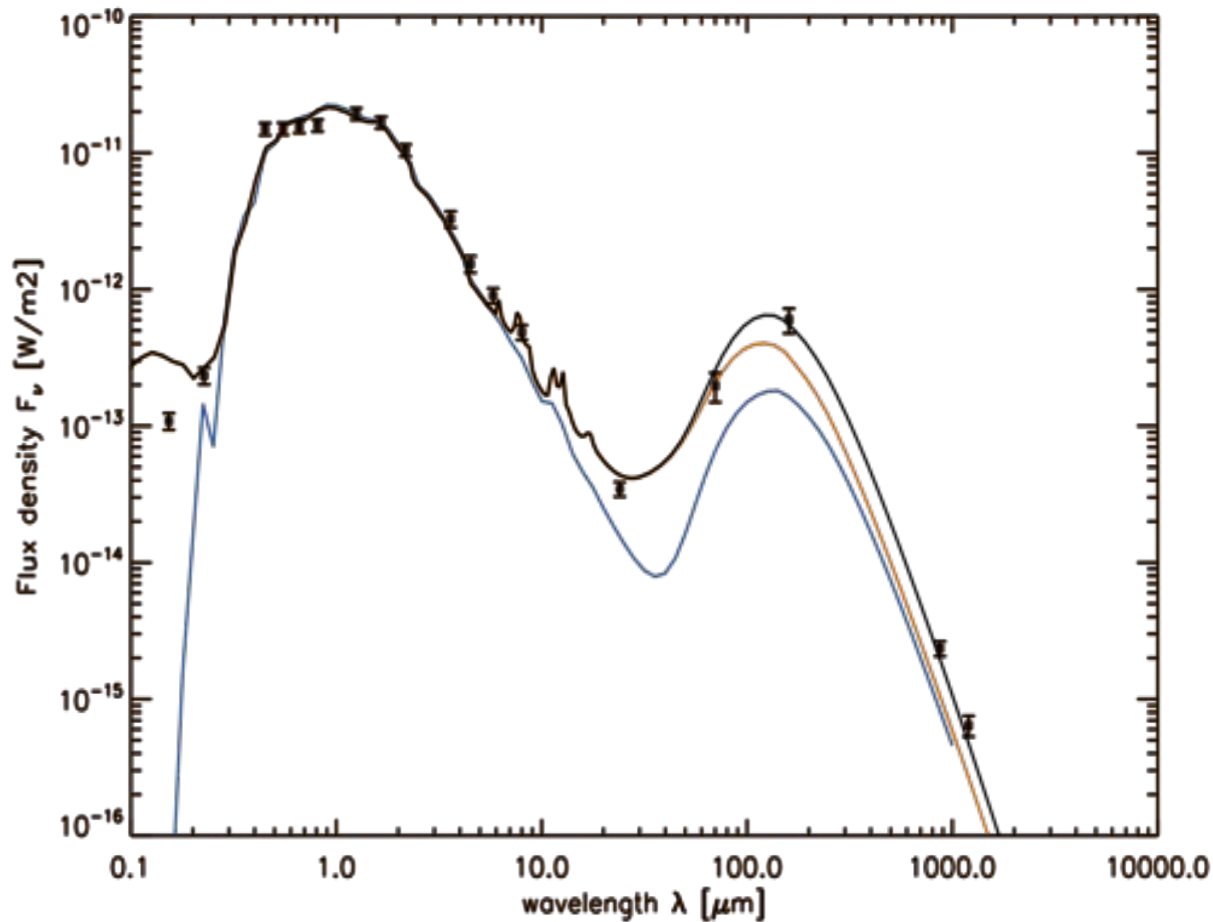


V-band model



*De Looze et al. 2012*

# Energy balance study for NGC 4594



*De Looze et al. 2012*

- Generate full SED from model
- Add young stars to match UV data
- We need an extra component of 17 K dust to explain the submm emission
- The dust seems to emit 3 times **more energy** than it absorbs

## Case study: NGC 4565

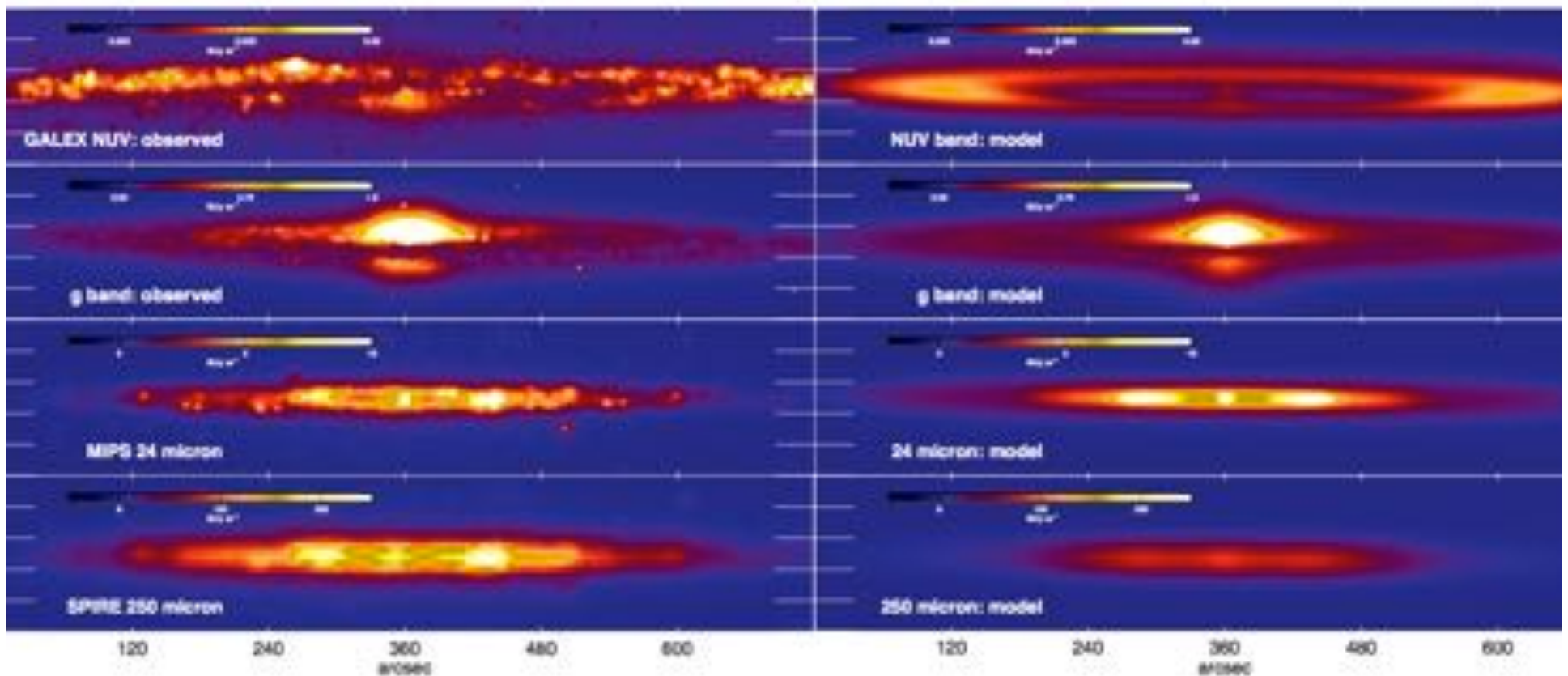




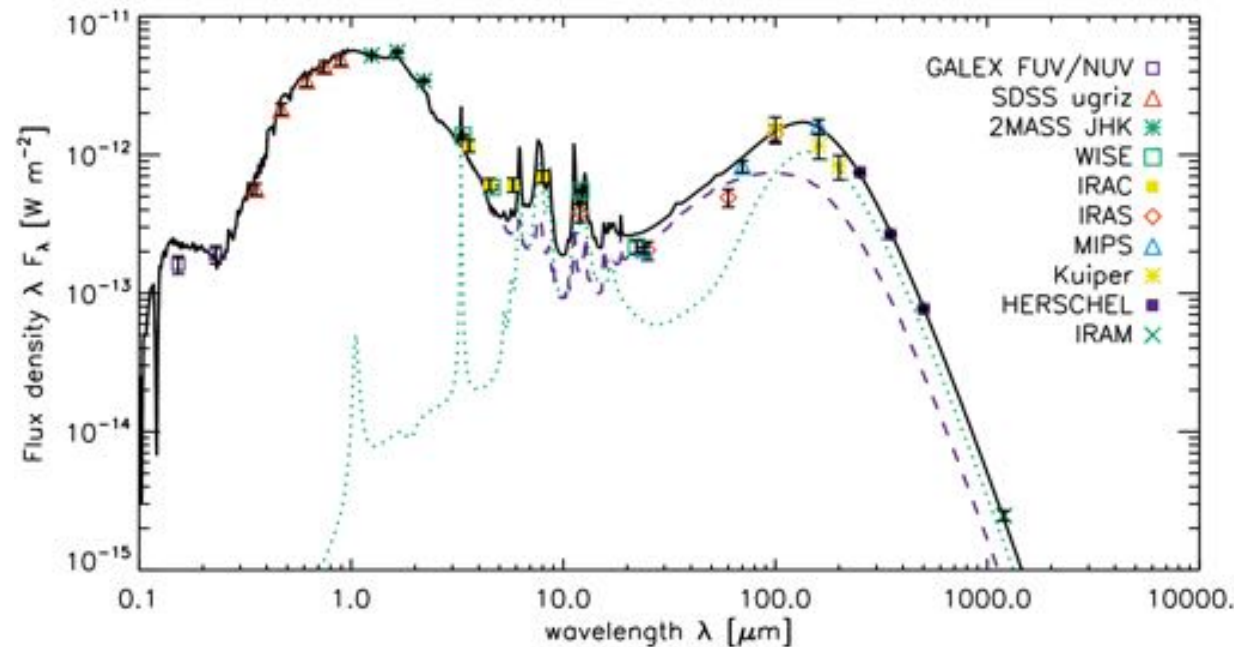
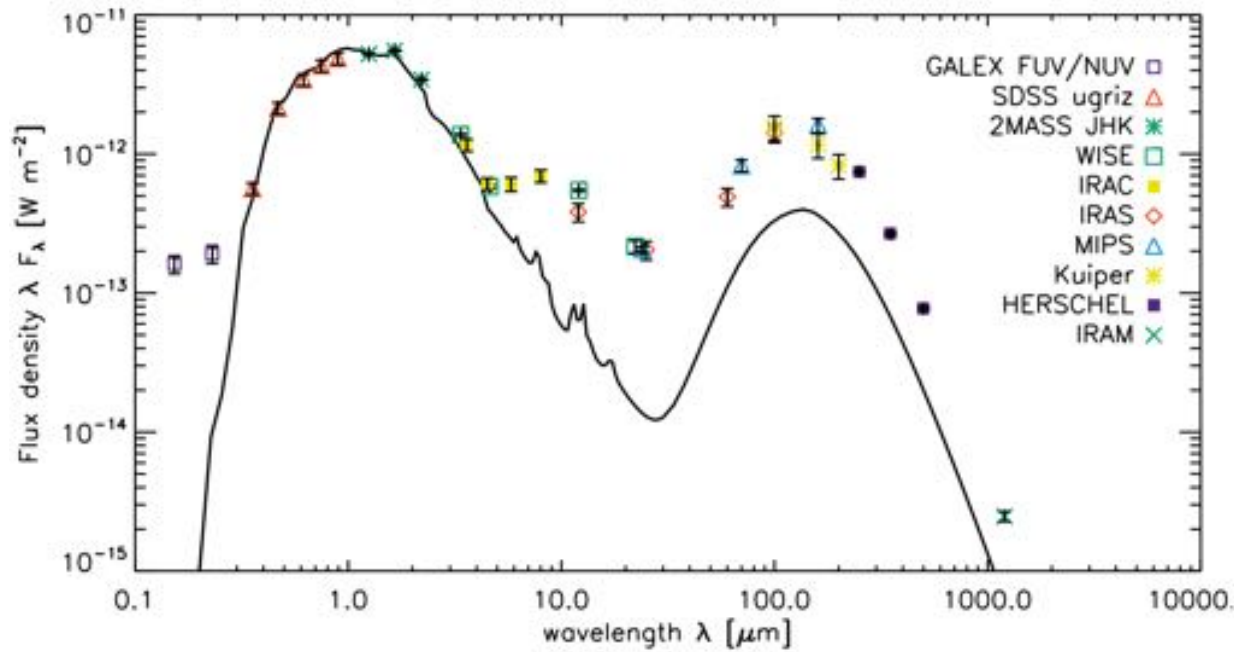
# Energy balance study for NGC 4565

Construct a model fitting  
images in **multiple bands**  
from UV to infrared

*De Looze et al. 2012*



# NGC 4565



- Generate full SED from model
- Discrepancy at UV/ FIR
- Add star formation constrained by NUV and MIR
- Still deficit of factor 3-4

*De Looze et al. 2012*

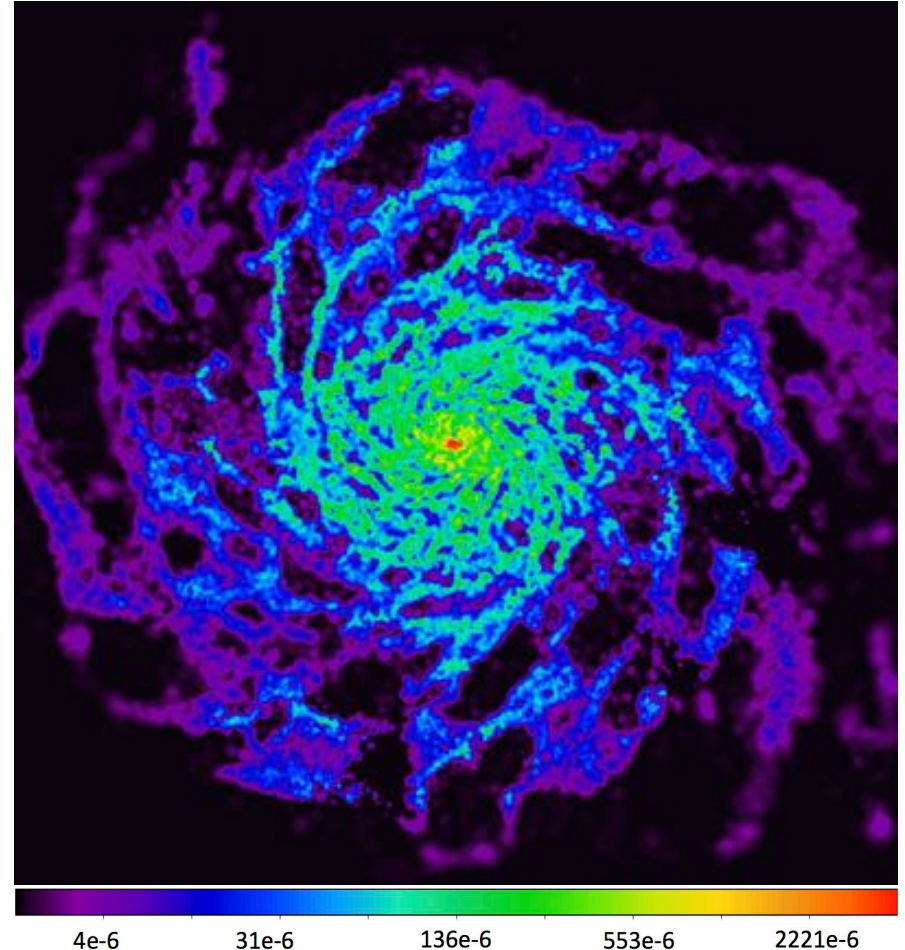
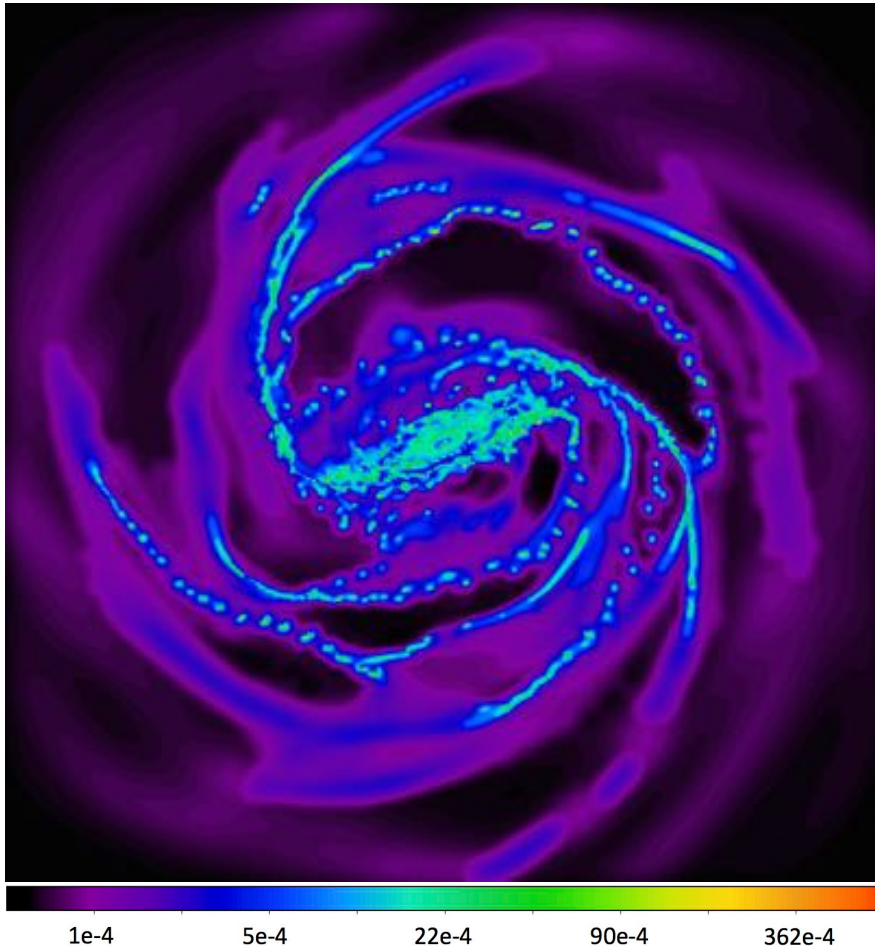
# The dust energy balance problem

- For some (not all) edge-on spiral galaxies
  - » the dust mass estimated from **extinction** is 3 or 4 times smaller
  - » than the dust mass estimated from **emission** in FIR/submm
- However, our models are smooth, unlike real galaxies
  - » Large-scale structure: bars, **spiral arms**
  - » Small-scale structure: granularity, filaments, star forming regions, compact dust **clumps**
- Better models?
  - » Models with large-scale structure (spiral arms, large clumps) fail to resolve the discrepancy (e.g. *Misioriotis et al. 2000, 2002*)
  - » What about **small-scale structure**? Test this hypothesis using galaxies created in hydrodynamical simulations...

# Input models from hydrodynamical simulations

R13 (*Renaud et al. 2013*)

Eris (*Guedes et al. 2011*)

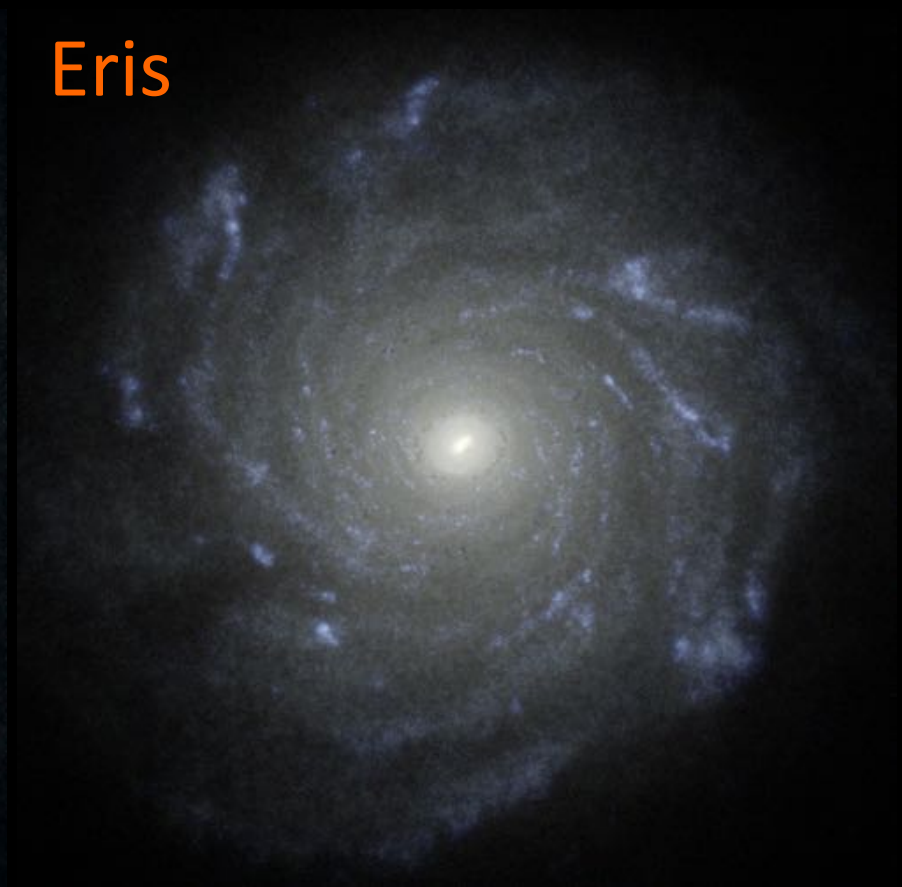


Cut through the dust density distribution in the equatorial plane of each galaxy

R13



Eris



# Fitting results

R13

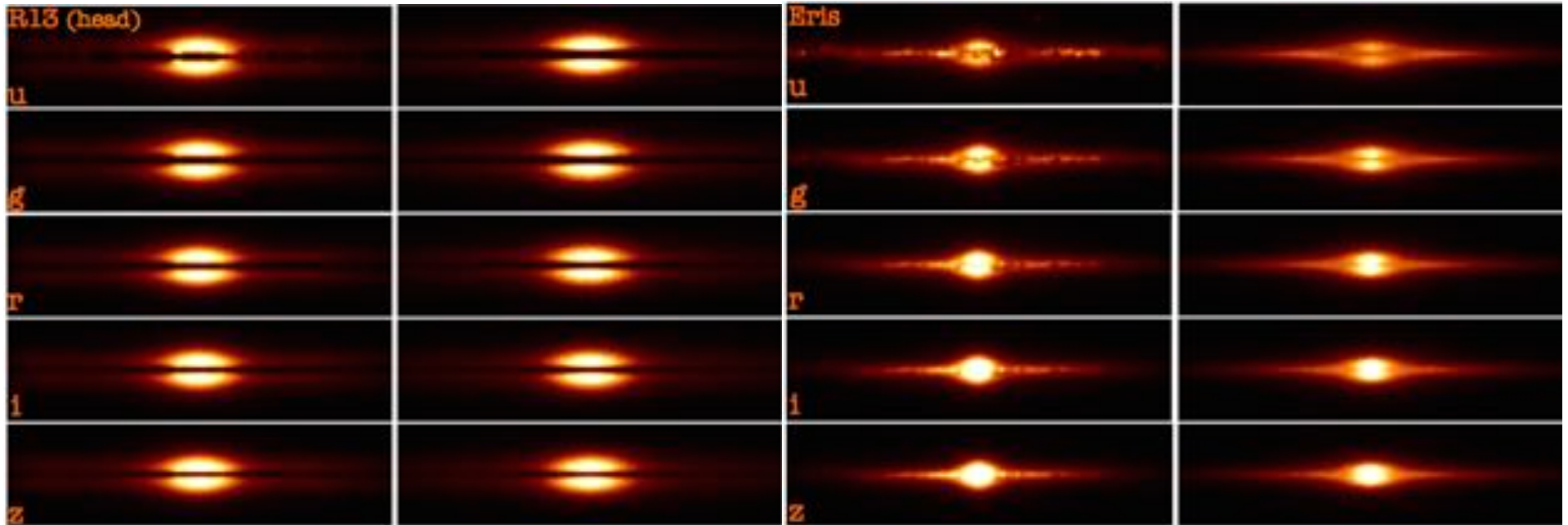
Eris

Reference images

Fitted images

Reference images

Fitted images



Par.	Units	R13 (head)	R13 (side)	Eris
$M_d$	$10^6 M_\odot$	$6.26 \pm 0.24$	$7.68 \pm 0.33$	$1.48 \pm 0.18$
			$18.1 \times 10^6 M_\odot$	$5.94 \times 10^6 M_\odot$

The RT model underestimates the "true" dust mass by a factor of: 2.9 and 2.4 for R13, and by a factor of 4 for Eris.

*Saftly et al. 2015*

# Conclusion

Fitting a smooth galaxy model to realistic input models from hydrodynamic simulations underestimates the total dust mass by a factor of about 3.

This **suggests** that the inhomogeneous **small-scale structure** of galaxies may be the **source** of the dust **energy balance problem**.

In other words, it suggests that the clumpy structure keeps a large amount of dust from being observed through extinction in the optical wavelength range.

Questions ?





# Automated galaxy modeling

Section A-4

# Automated inverse radiative transfer

## Objective

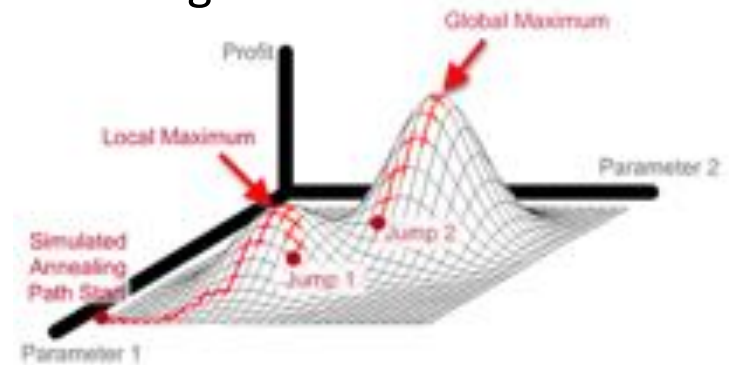
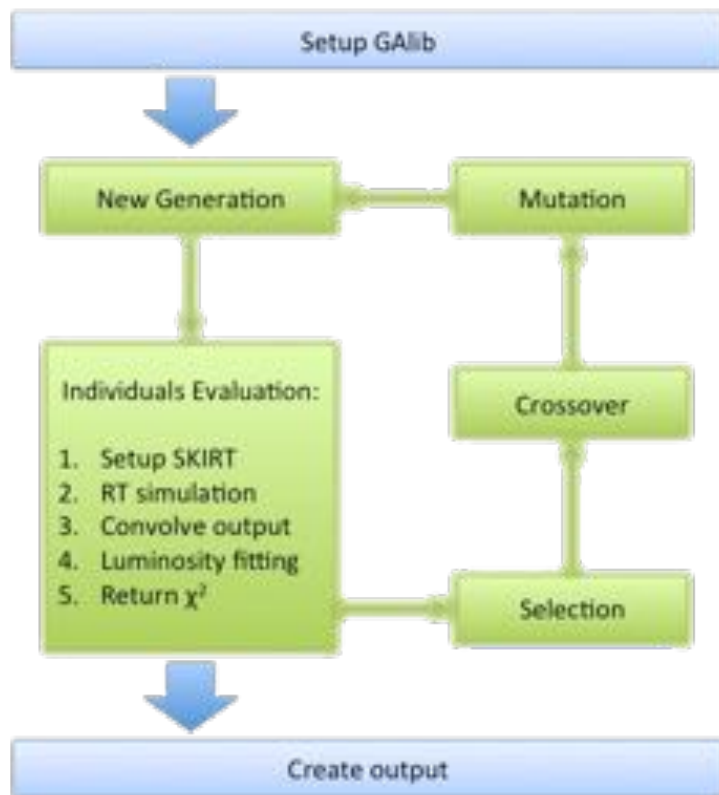
- Automatically find optimal model **parameters** by coupling a radiative transfer code to an **optimization** process

## Complications

- **Large number** of model parameters to be fitted
  - » Intrinsic star & dust geometry
  - » Orientation
  - » Dust properties
- **Run-time** for a single RT simulation (i.e. a single point in the multi-dimensional parameter space) is considerable
- Monte Carlo **noise** makes fitting more complicated

# Automated parameter fitting

Poisson **noise** on Monte Carlo simulations prevents standard fitting and complicates simulated annealing



Genetic algorithm:

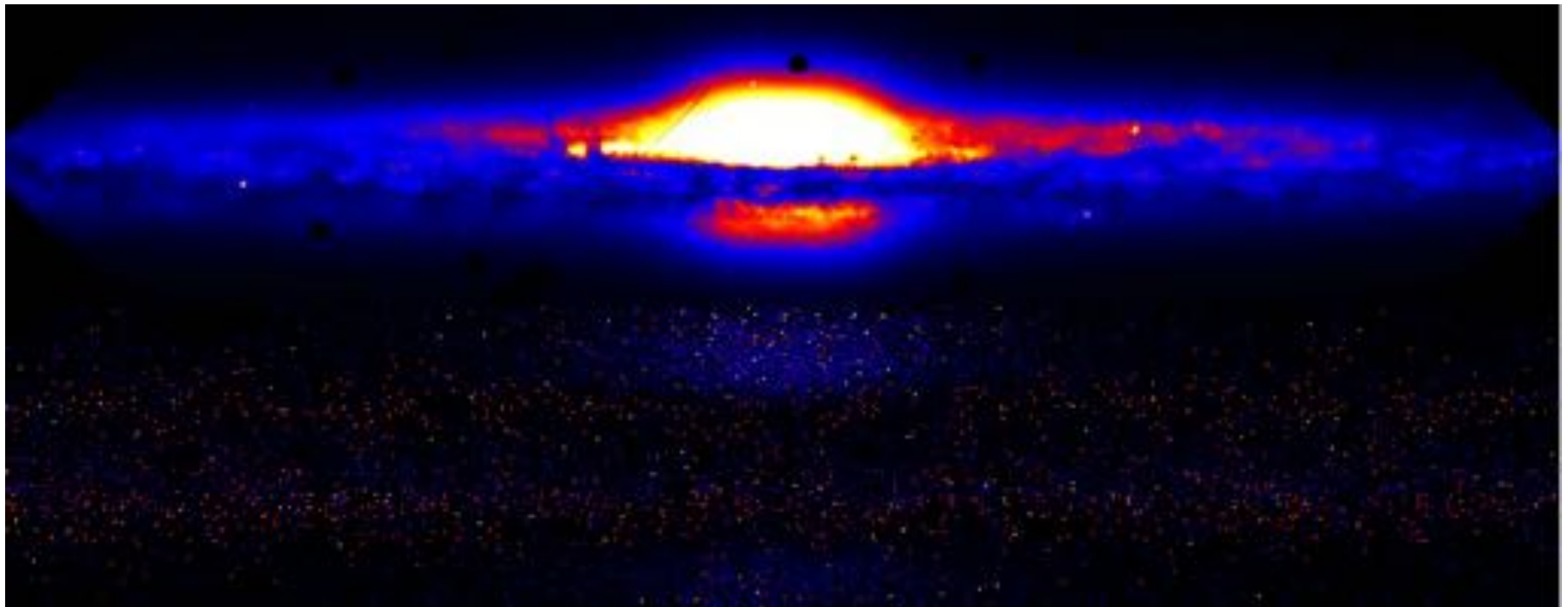
- Poisson noise **averages out** over population
- Uniformly samples parameter space
- More easily tests distant **global maximum**

*De Geyter et al. 2012*

# FitSKIRT

- Automatically fits parametric 3D models to a set of UV/optical/NIR images
- Searches the parameter space using a genetic algorithm
- Uses SKIRT to evaluate each individual against the data

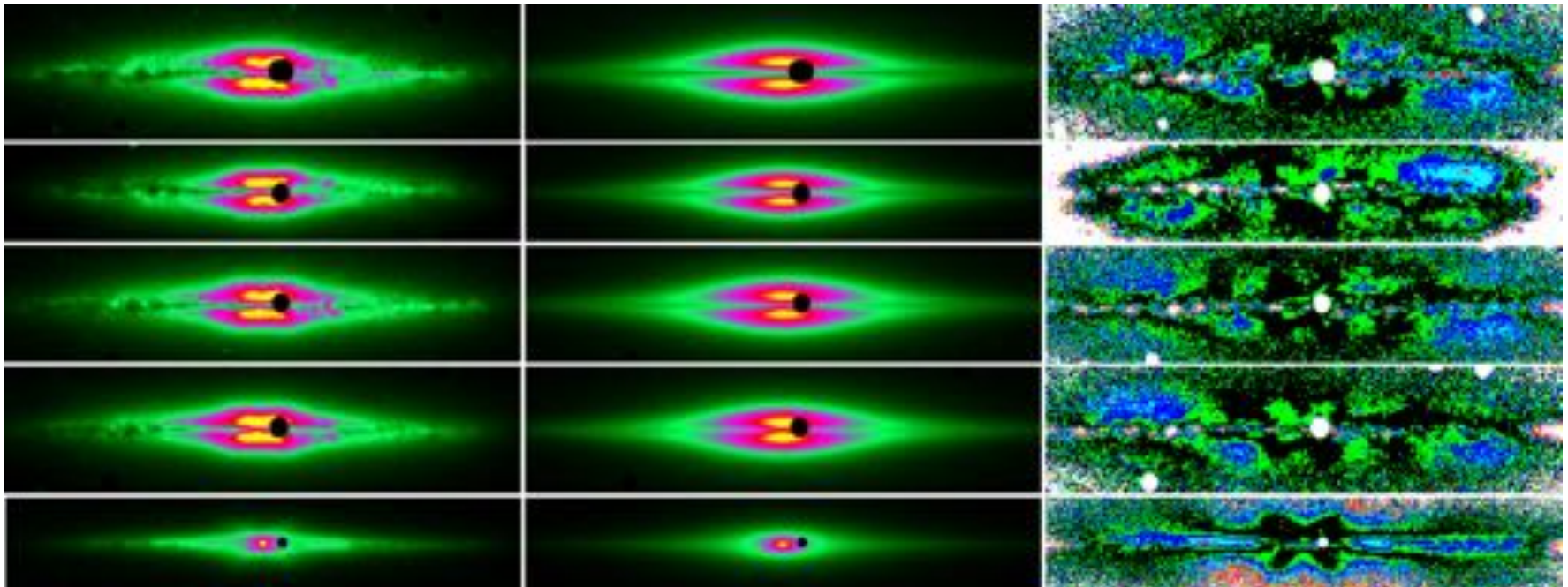
*De Geyter et al. 2012*

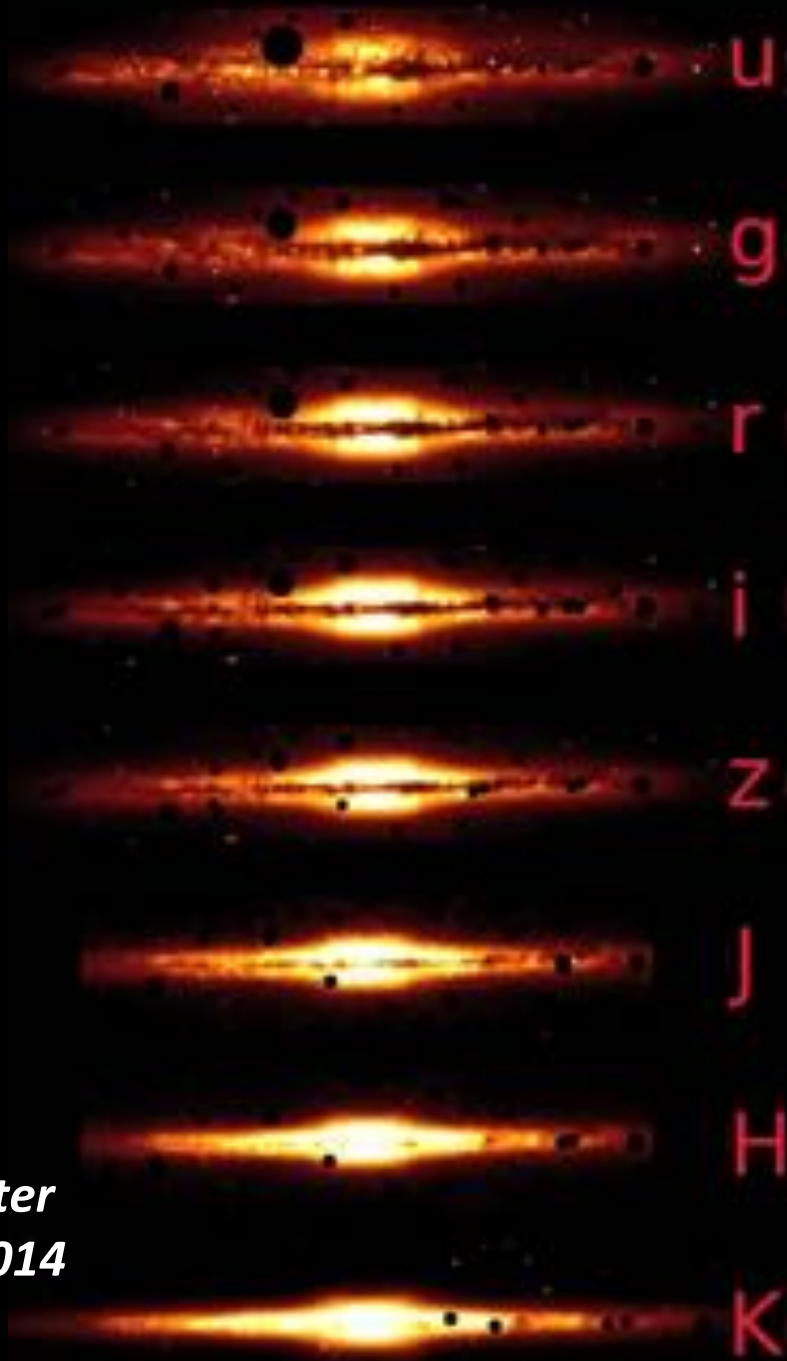


# Automated oligochromatic fit of NGC 4013

- Monochromatic fitting (single-wavelength) shows degeneracy in dust properties
- Improved by oligochromatic fitting (multiple wavelengths)
  - » Simultaneous fit in multiple bands (5 in this case)
  - » 11 parameters: stellar disk & bulge, dust disk

*De Geyter et al. 2013*





*De Geyter  
et al. 2014*

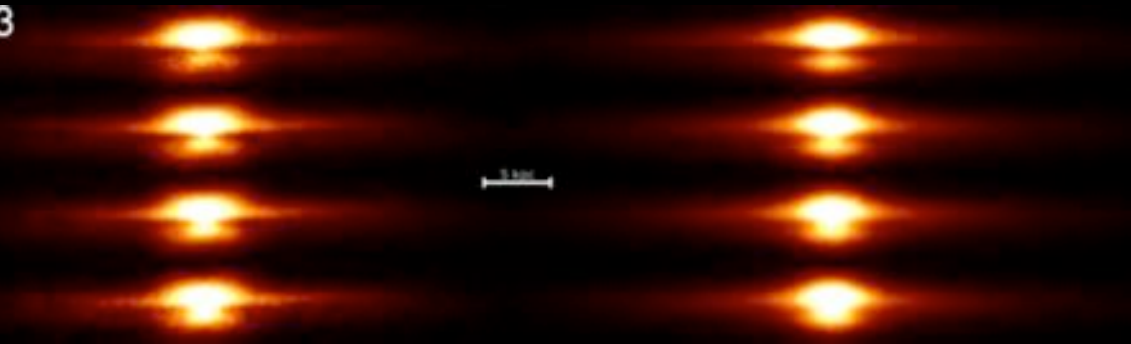
# Case study: CALIFA edge-on spiral galaxies



- 12 edge-on spiral galaxies selected from the CALIFA sample
- Oligochromatic g, r, i and z-band fitting
- Star and dust geometry?
- Face-on optical depth?

*De Geyter et al. 2014*

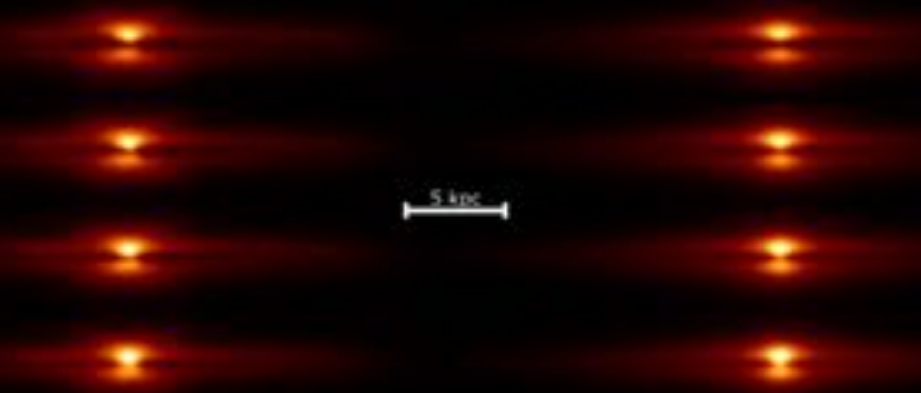
IC3203



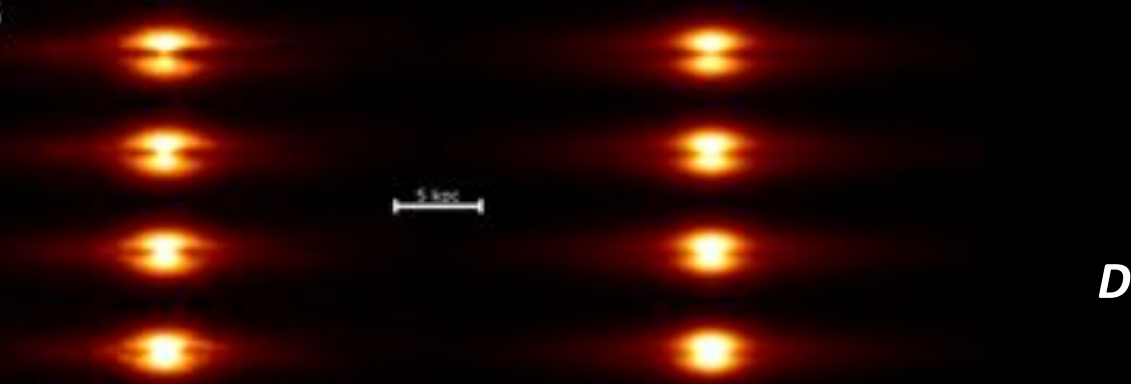
# CALIFA

Some  
fitting  
results

NGC3650



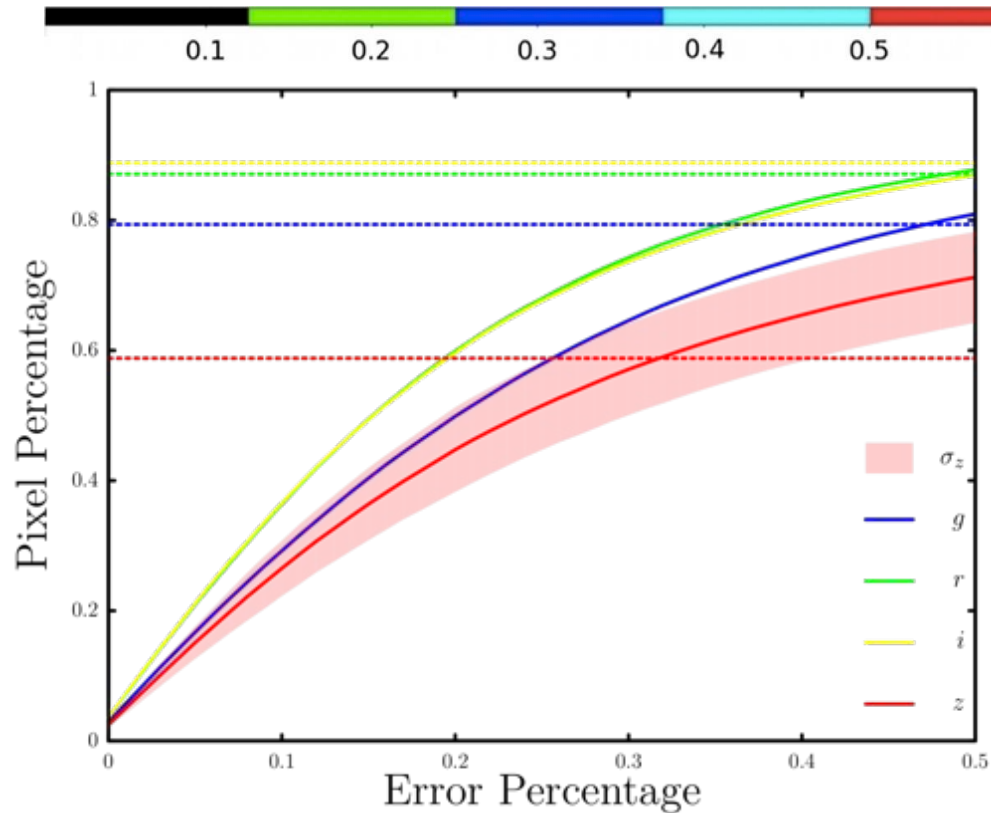
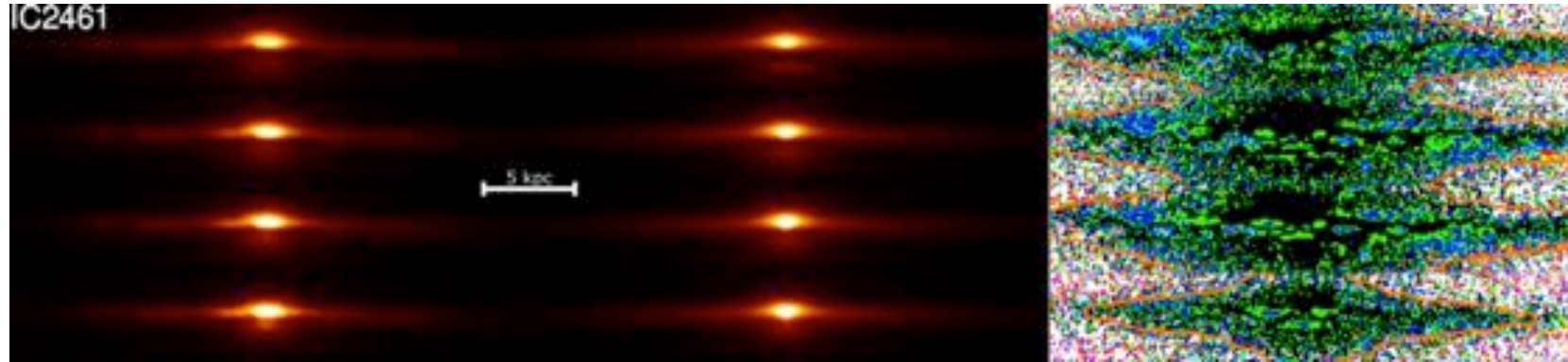
IC4225



*De Geyter et al. 2014*



# CALIFA - fitting accuracy



Parameter	unit	mean $\pm$ RMS	$1\sigma$ (%)
$h_{R,*}$	kpc	$4.23 \pm 1.23$	3
$h_{z,*}$	kpc	$0.51 \pm 0.27$	7
$R_{\text{eff}}$	kpc	$2.31 \pm 1.59$	11
$n$	—	$2.61 \pm 1.80$	14
$q$	—	$0.56 \pm 0.20$	6
$h_{R,d}$	kpc	$6.03 \pm 2.92$	19
$h_{z,d}$	kpc	$0.23 \pm 0.10$	13
$M_d$	$10^7 M_\odot$	$3.02 \pm 2.21$	23
$\tau_V^f$	—	$0.76 \pm 0.60$	28
$\tau_V^e$	—	$18.0 \pm 7.1$	15
$i$	deg	$86.7 \pm 2.5$	0.4
$L_g^{\text{Tot}}$	$10^9 L_\odot$	$2.70 \pm 2.40$	15
$L_r^{\text{Tot}}$	$10^9 L_\odot$	$4.12 \pm 3.54$	12
$L_i^{\text{Tot}}$	$10^9 L_\odot$	$5.64 \pm 4.50$	10
$L_z^{\text{Tot}}$	$10^9 L_\odot$	$7.35 \pm 5.72$	3
$B/T_g$	—	$0.41 \pm 0.11$	17
$B/T_r$	—	$0.45 \pm 0.11$	14
$B/T_i$	—	$0.46 \pm 0.11$	4
$B/T_z$	—	$0.46 \pm 0.08$	3

# CALIFA case study conclusions

- Sample of 12 edge-on spiral galaxies from CALIFA survey
- Reasonable accuracy on frame reproduction and parameter determination
- Values for stellar parameters and dust properties similar to those found by others
- **Dust disks** about 70% **more extended** than stellar disks, and about half as thick
- **Large spread** within sample for **face-on optical depth**, up to  $\tau=3$  i.e. fairly **opaque!**

Questions ?





# MCRT post-processing of hydrodynamic snapshots

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Saint Andrews Monte Carlo Summer School  
2015

# Overview

## **MCRT in galaxies with SKIRT**

- Dust in galaxies
- SKIRT features and code design
- Energy balance in galaxies
- Automated galaxy modeling

## **MCRT post-processing of hydrodynamic snapshots**

- Stochastic heating of dust grains
- Dust grids: regular, hierarchical, unstructured
- Importing hydro snapshots: AMR, SPH
- FIR properties of galaxies in a cosmological simulation

# Stochastic heating of dust grains

Section B-1

# Emission from a dust mixture

- Thermal emission depends **nonlinearly** on grain size  $a$ 
  - » For each dust type  $k$ , split the grain size range into  $b$  bins
- **Emissivity** when exposed to radiation field  $J(\lambda)$ :  
(according to Kirchhoff's law of thermal radiation)

$$\varepsilon(\lambda) = \sum_{k,b} S_{k,b}^{\text{abs}}(\lambda) \int_0^{\infty} P_{k,b,J}(T) B(\lambda, T) dT$$

Absorption cross section for representative grain in each bin

Planck function describing Black Body radiation

Probability of finding the representative grain of bin  $k,b$  at temperature  $T$  when exposed to field  $J(\lambda)$

## Emission in LTE conditions

$$\varepsilon(\lambda) = \sum_{k,b} \mathcal{S}_{k,b}^{\text{abs}}(\lambda) \int_0^{\infty} P_{k,b,J}(T) B(\lambda, T) dT$$

- If representative grain is in **local thermal equilibrium (LTE)** with the surrounding radiation, we have:

$$P_{k,b,J}(T) = \delta(T - T_{k,b,J}^{\text{eq}})$$

- where the equilibrium temperature is determined from the **energy balance** equation

$$\int_0^{\infty} \mathcal{S}_{k,b}^{\text{abs}}(\lambda) J(\lambda) d\lambda = \int_0^{\infty} \mathcal{S}_{k,b}^{\text{abs}}(\lambda) B(\lambda, T_{k,b,J}^{\text{eq}}) d\lambda$$

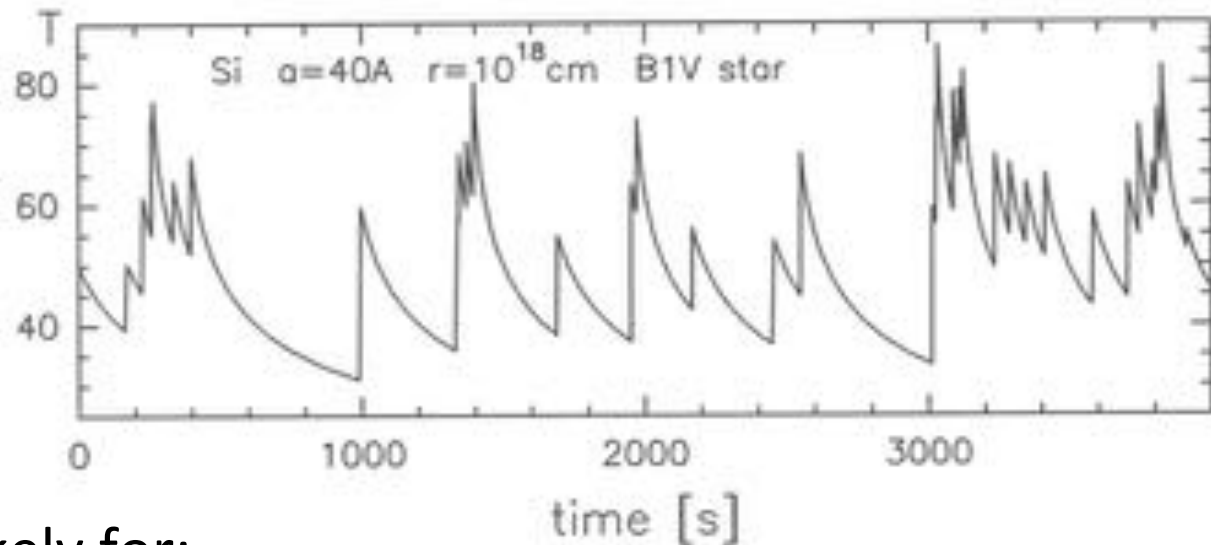
Absorbed energy

Emitted energy



# Non-LTE conditions

- If a **single photon** can significantly **change** the internal energy of a representative grain, the grain is **not** in local thermal equilibrium (LTE) with the surrounding radiation
  - » The grain is **stochastically heated**



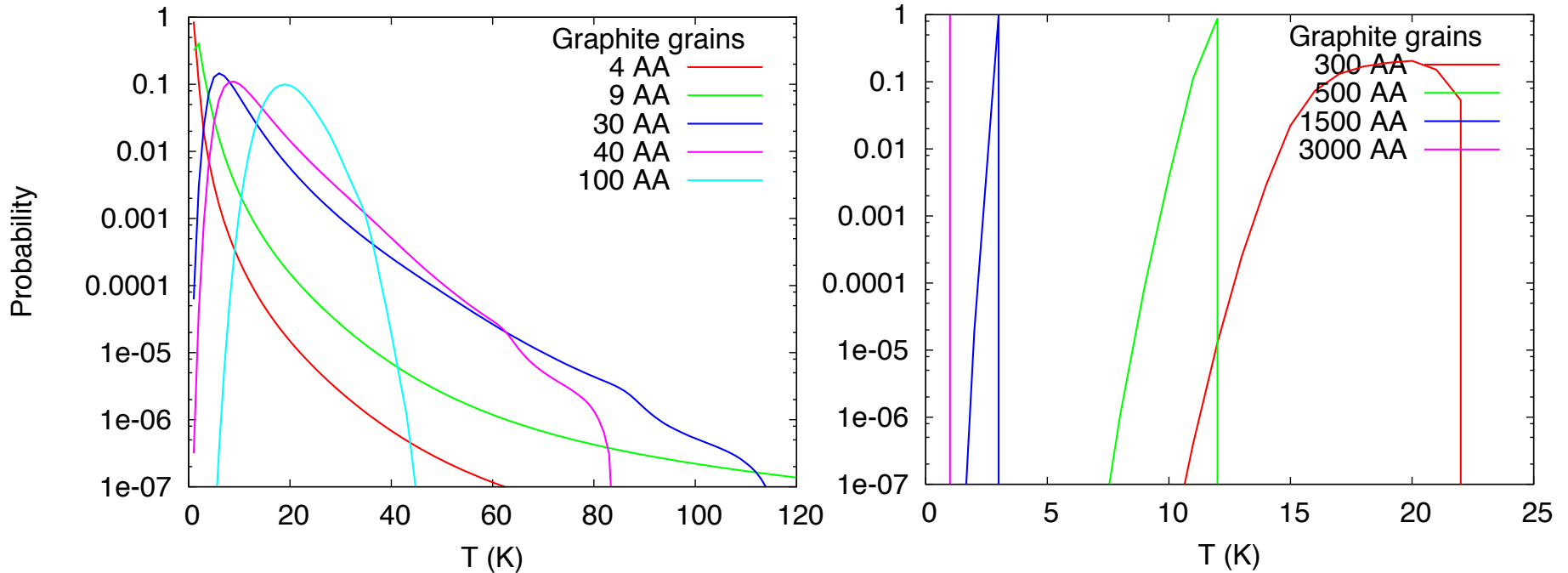
- This is more likely for:
  - » **Small** grains or molecules
  - » **Hard** radiation (high-energy photons)
  - » **Weak** fields (fewer photons)

# Emission in non-LTE conditions

$$\varepsilon(\lambda) = \sum_{k,b} \varsigma_{k,b}^{\text{abs}}(\lambda) \int_0^{\infty} P_{k,b,J}(T) B(\lambda, T) dT$$

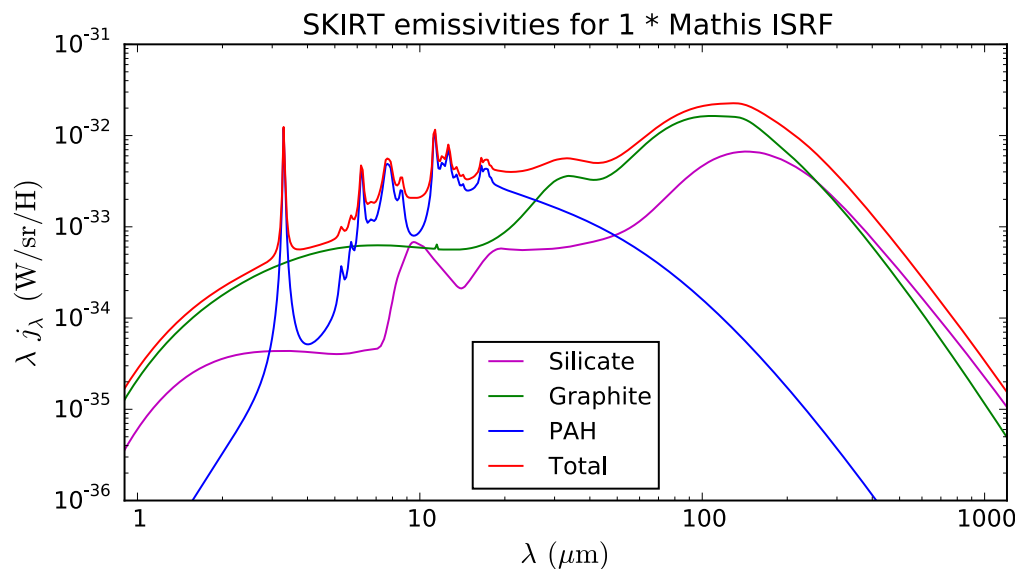
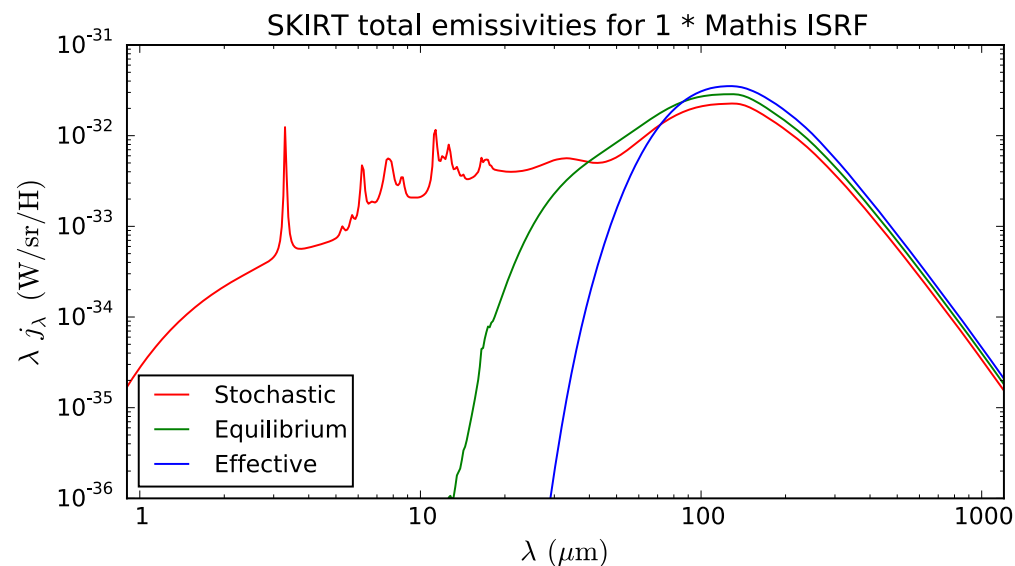
- We need to **solve** for the temperature probability distribution  $P_{k,b,J}(T)$ , which depends on the radiation field  $J(\lambda)$  in addition to the properties of the representative grain of bin  $k,b$
- This is computationally **very demanding**
  - » RT codes routinely need to calculate **many millions** of dust emission spectra so performing a full statistical treatment would be prohibitive
  - » We assume that a dust grain cools by radiating photons with an energy that is very small compared to the internal energy of the grain
  - » Using this **continuous cooling** assumption, the complexity can be reduced to  $O(N^2)$  where  $N$  is the number of temperature grid points
  - » Still challenging in **near-equilibrium** regimes where the probability distribution approaches a **delta function** (requiring a very fine grid)

# Temperature probability functions



- For large grains,  $P(T) \rightarrow \delta(T_{eq})$ , so calculation becomes **unstable**
- **Cutoff** point for switching to equilibrium calculation is subject to **debate**

# Dust emission in typical ISRF

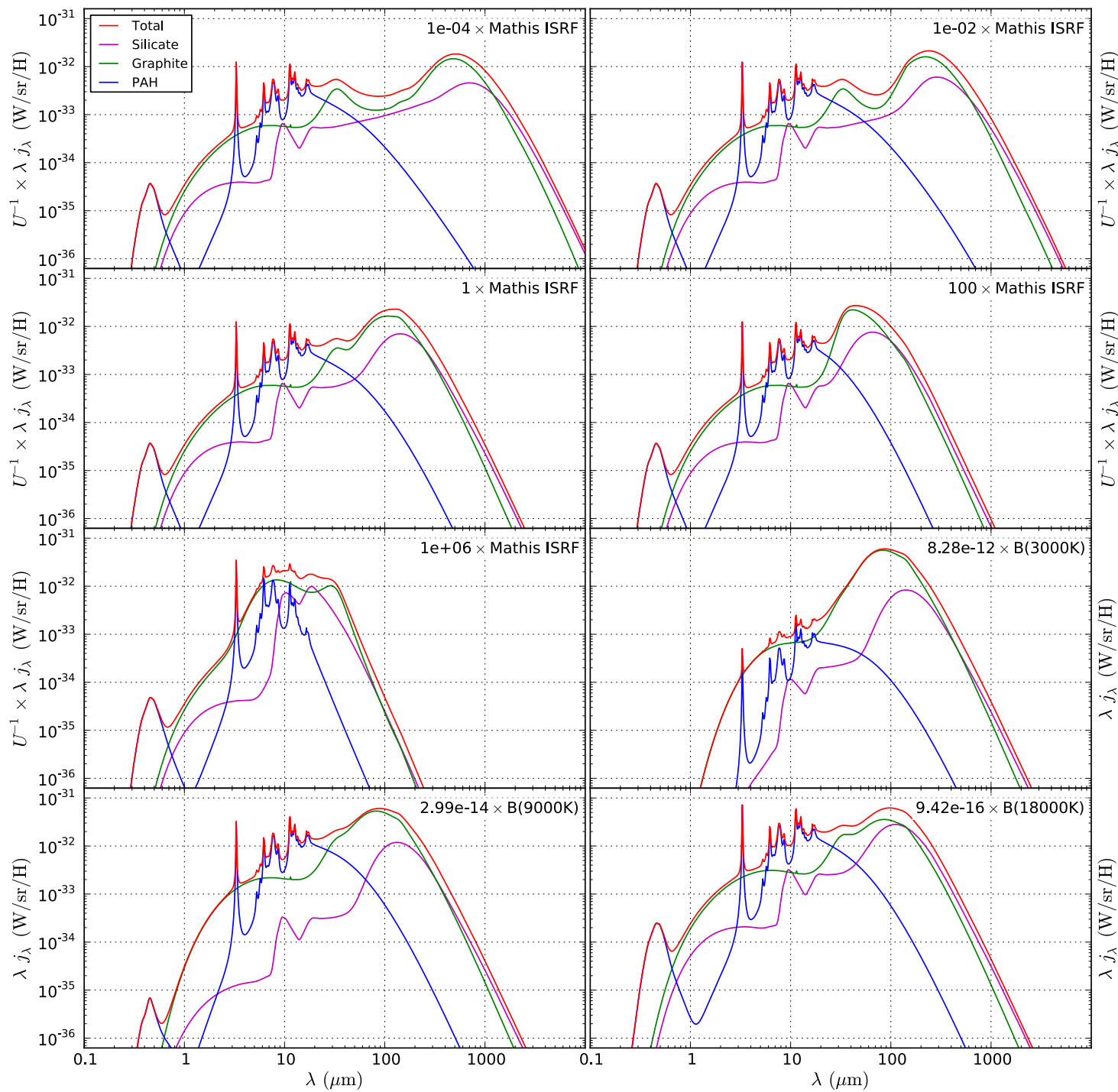


- Assumptions

- » Interstellar radiation field (ISRF) as observed in solar neighborhood (*Mathis et al. 1983*)
- » Simple dust model approximating Milky Way observations

- We see that

- » SHGs shift emission to shorter wavelengths (up to factor 10 or more)
- » PAH emission features sharp peaks in wavelength range 3-20  $\mu\text{m}$



# Dust emission for a range of embedding fields

- weak to strong
  - » continuum peak shifts
- soft to hard
  - » SHG emission increases

*Camps et al. 2015*

# Stochastically heated grains benchmark

- Compare SHG emission calculations in the context of RT
  - » Reference solution by non-RT code + 6 RT codes
  - » Precisely defined dust model
  - » 17 input fields ranging from weak to strong, soft to hard
- Explain differences and provide guidelines for implementation
  - » For all but the most extreme input fields, we find agreement within 10% across the important wavelength range  $3 \mu\text{m} \leq \lambda \leq 1000 \mu\text{m}$
  - » A lot of algorithmic and discretization details must be handled with care to achieve this level of accuracy with acceptable performance
    - » Transition from stochastic to equilibrium
    - » Grids for temperature, wavelength, grain size
  - » Can calculate several hundred spectra per second per core
    - a few hours for 5 million cells on a regular desktop computer

Questions ?



# Dust grids

Section B-2

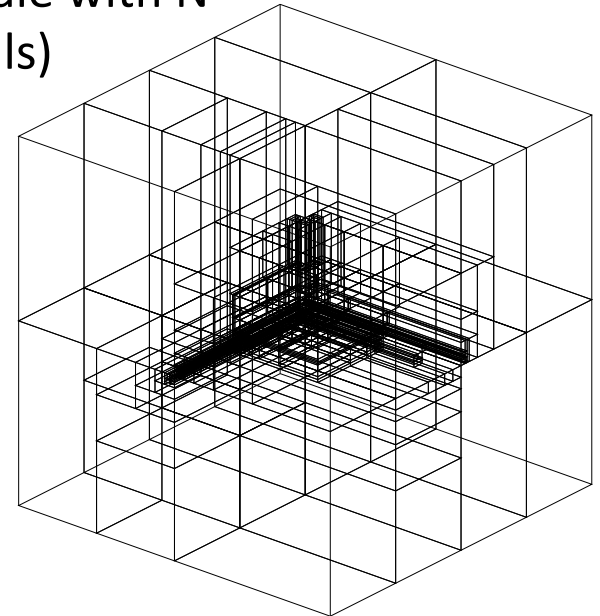


# Dust grids in (SKI)RT

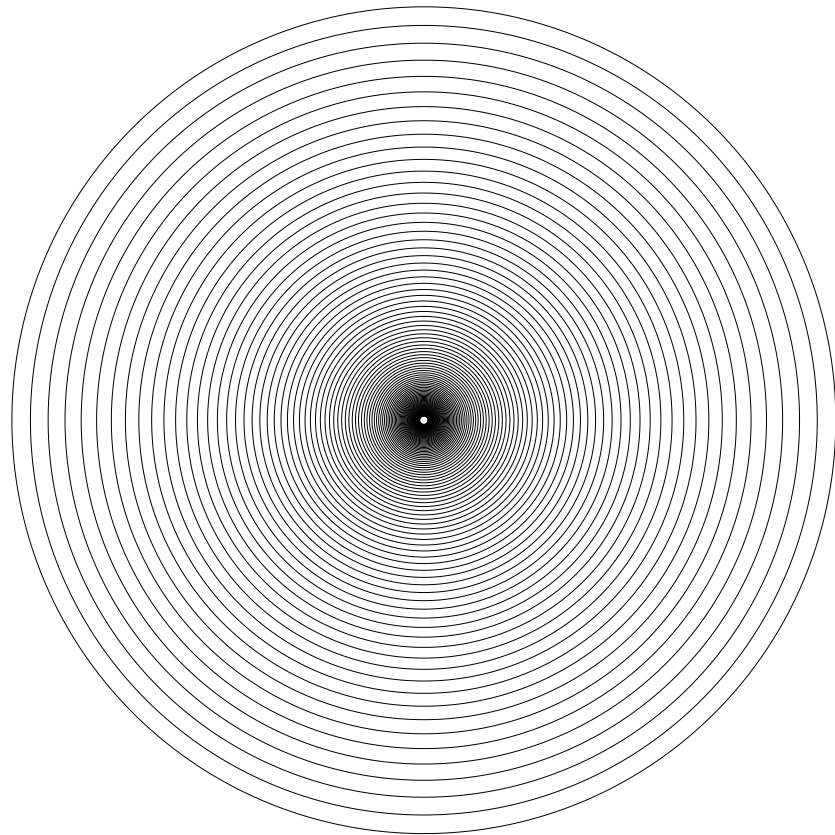
- Dust grid = spatial discretization of dust medium
- Physical quantities are assumed **constant** in each cell
  - » Radiation field
  - » Dust density, optical properties, temperature
- Need small cells to properly **resolve** the physics
- Number of cells  $N$  determines resource requirements
  - » **Memory** needs and execution **time** roughly scale with  $N$   
(need more photons to properly sample all cells)



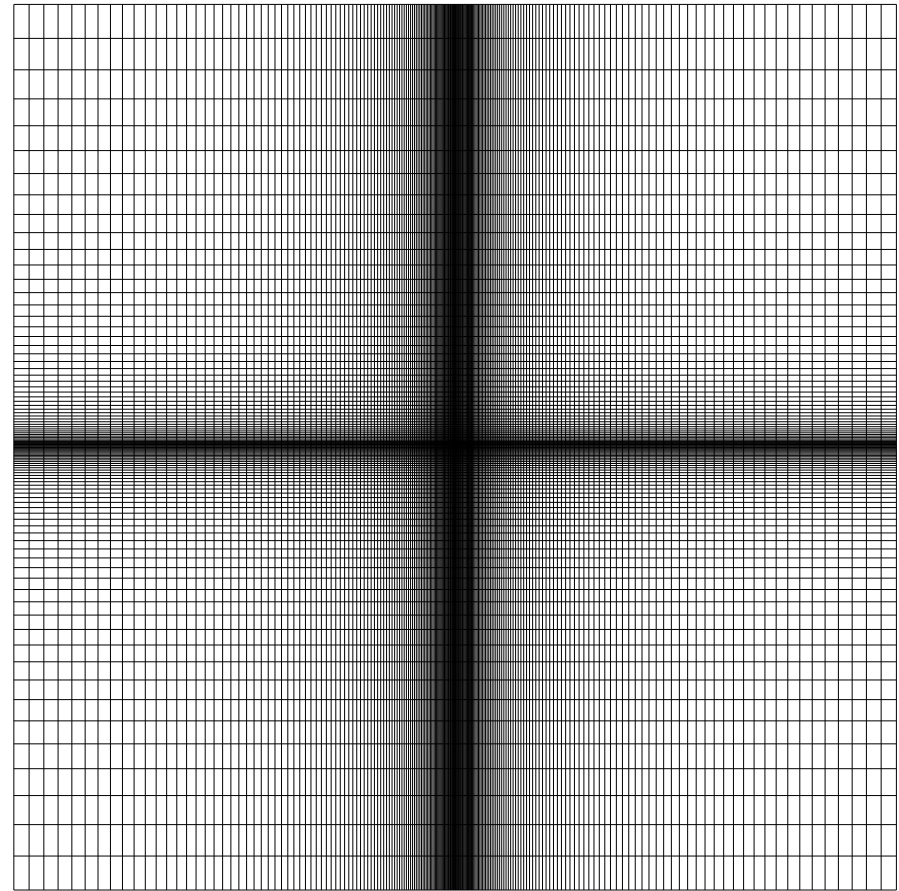
- Quest for schemes that place many small cells **where needed** and fewer large cells elsewhere

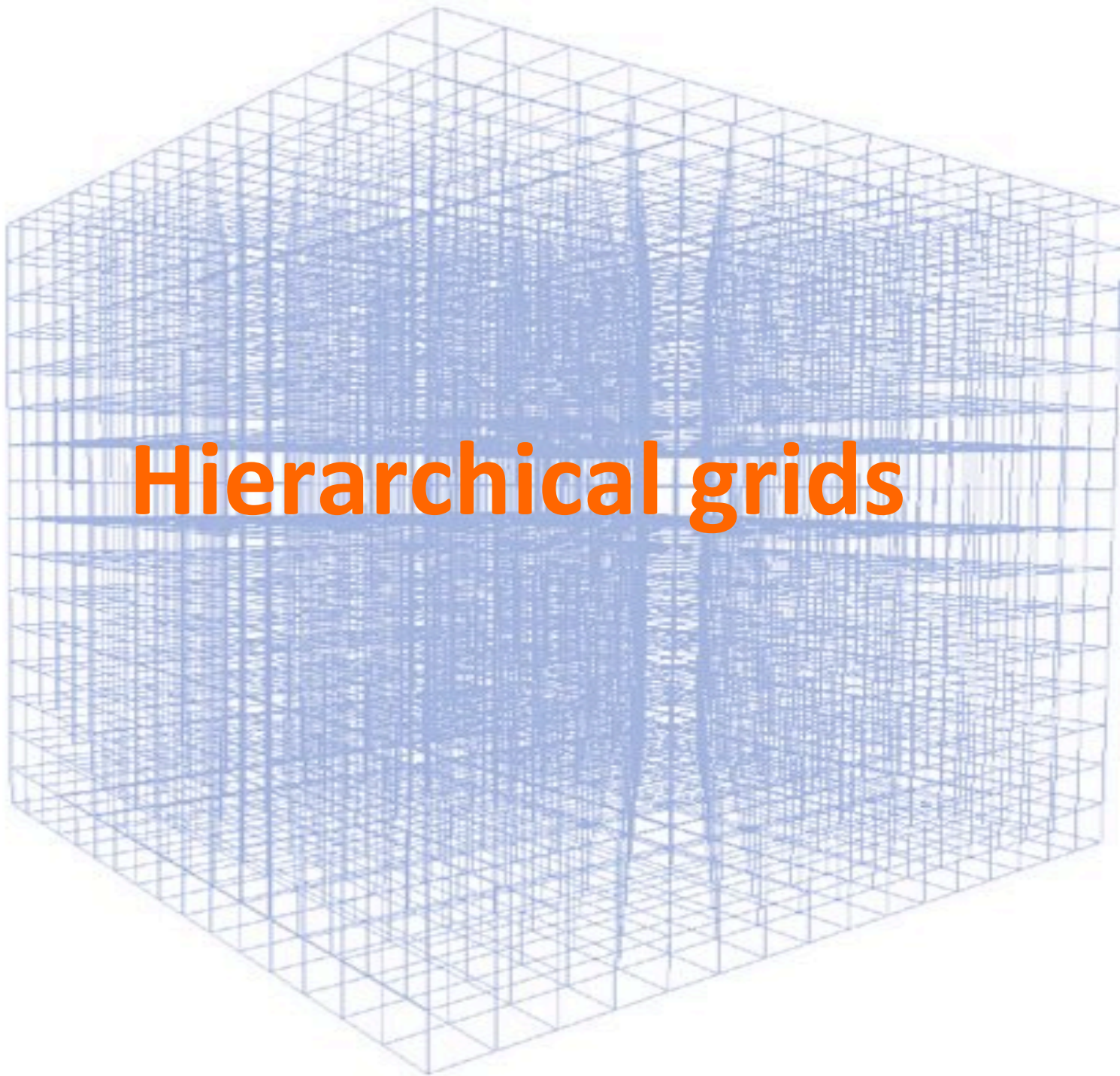


# Fixed dust grids

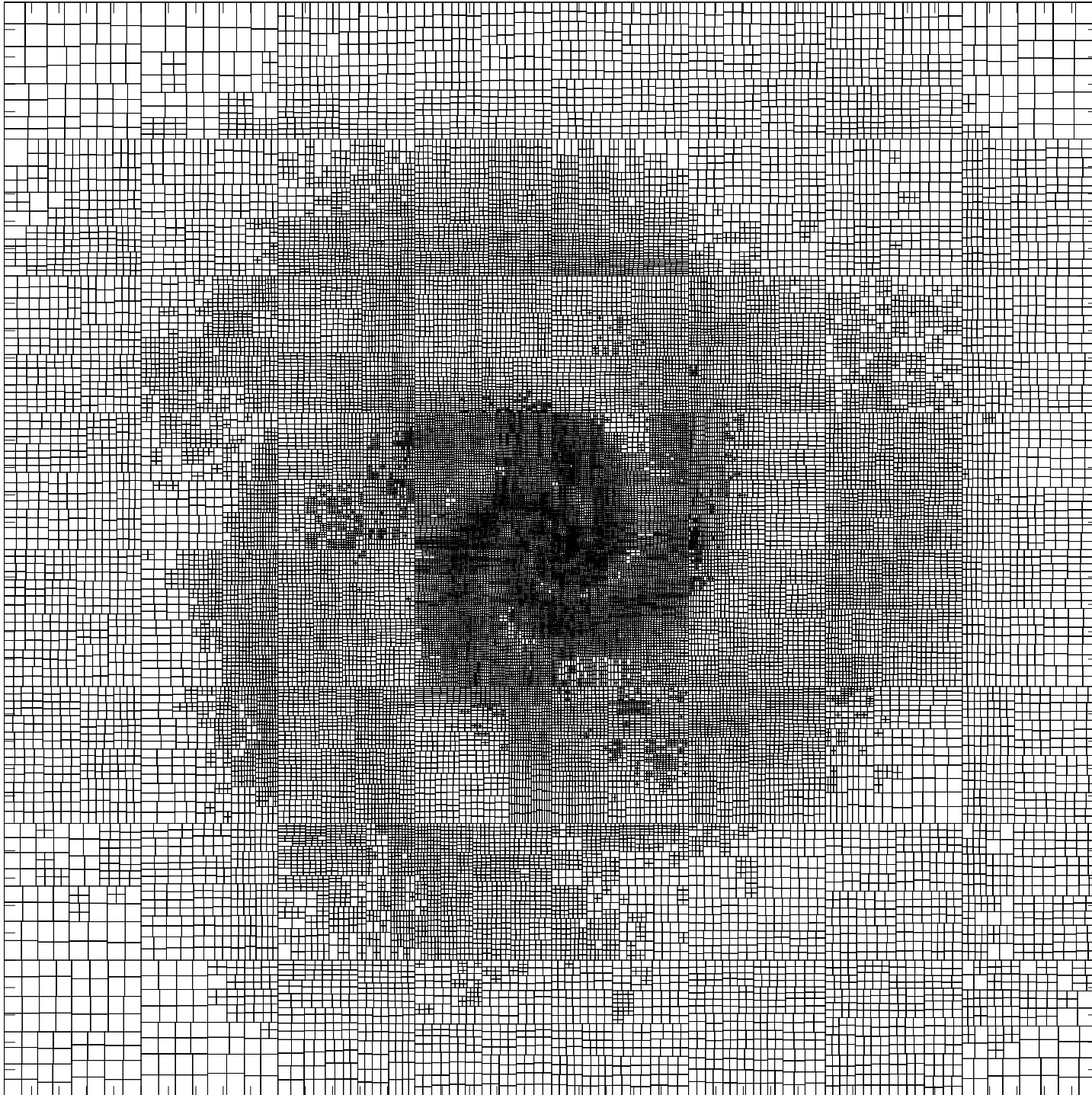


1D, 2D, 3D  
regular, log, power law





# Hierarchical grids



## Hierarchical dust grids

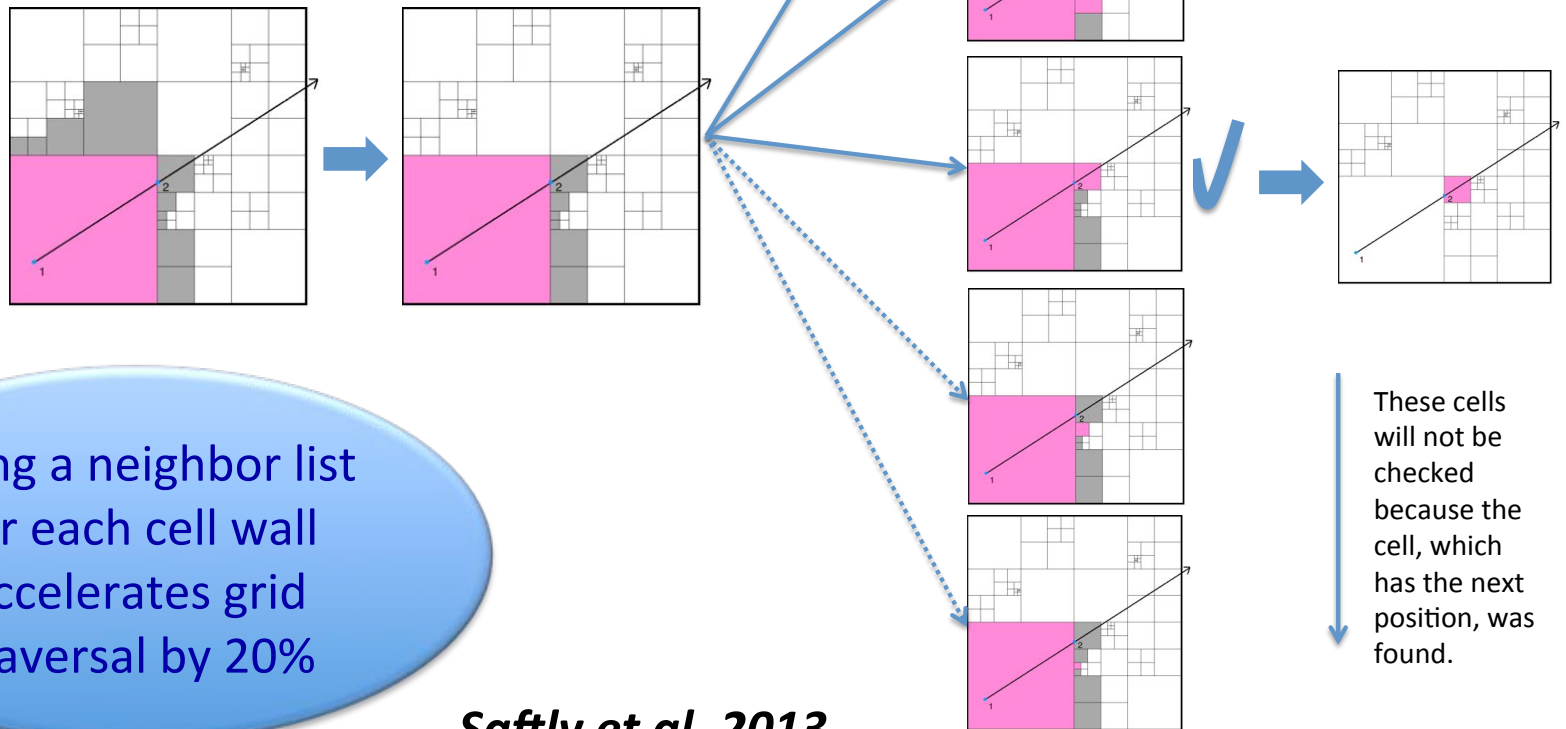
Cut through octree  
with **recursive**  
**barycentric**  
subdivision based  
on dust **density**  
distribution of a  
spiral galaxy

*Saftly et al. 2013*

# Grid traversal

For each cell:

1. Calculate the path to the boundary of the cell
2. Determine the **neighboring cell** at the exit position

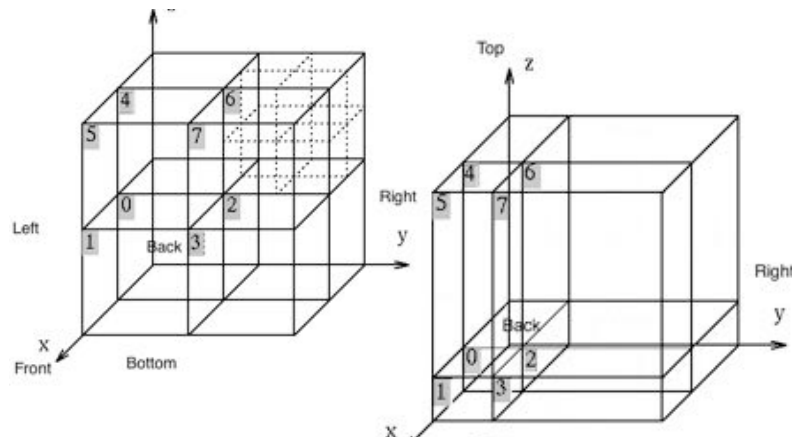


The cells are ordered by the area of overlap between the current cell and its neighbors.

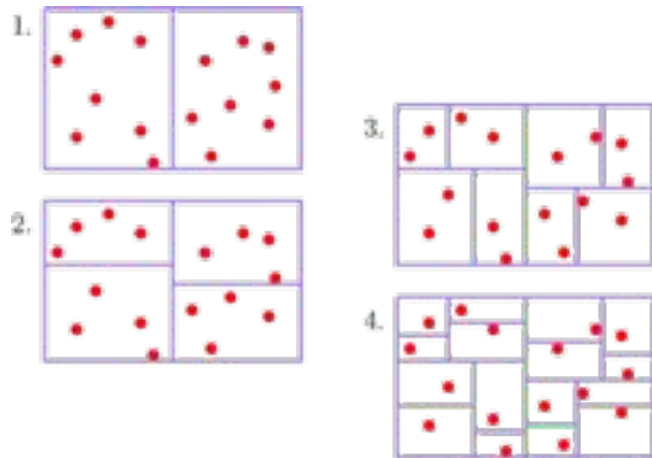
These cells will not be checked because the cell, which has the next position, was found.

*Saftly et al. 2013*

# Octree versus *k*-d tree



Octree subdivides a node into **eight** subnodes



*k*-d tree subdivides a node into **two** subnodes

Quality measure  
standard deviation of  
randomly sampled  
density error

*k*-d tree needs 20%  
fewer cells to  
achieve the same  
quality

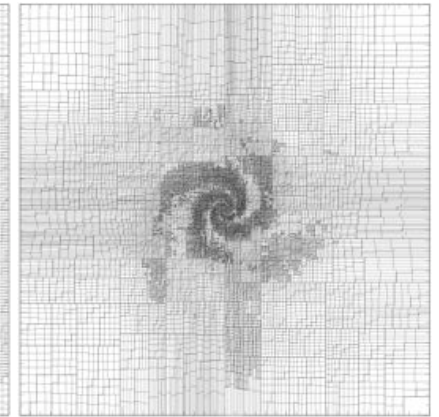
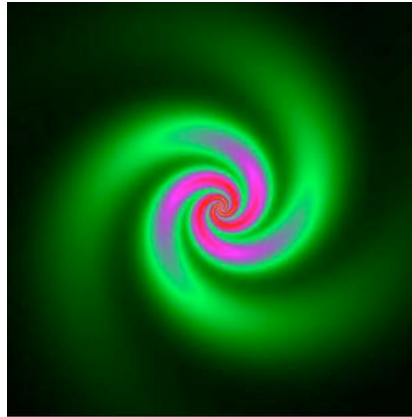
***Saftly et al. 2013***

# Subdivision point

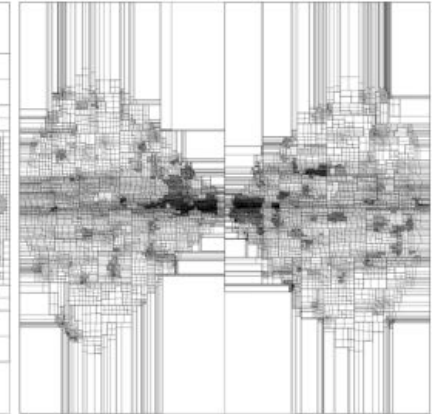
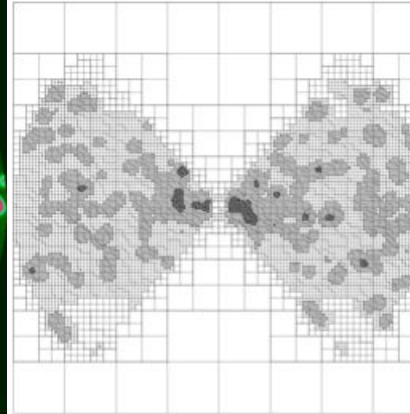
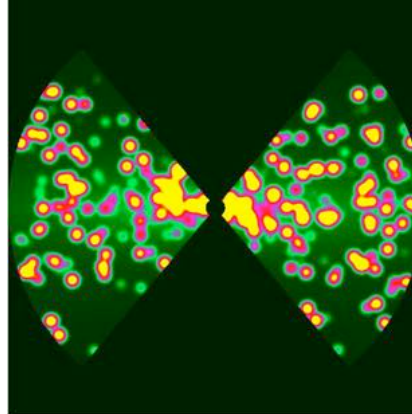
Geo-center

Barycenter

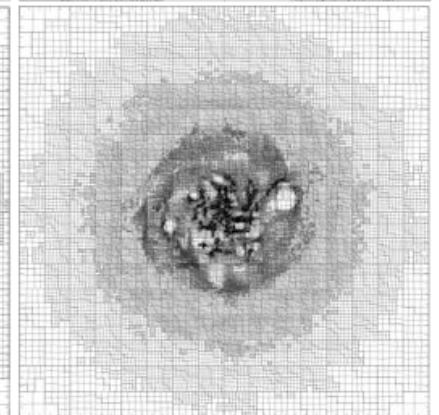
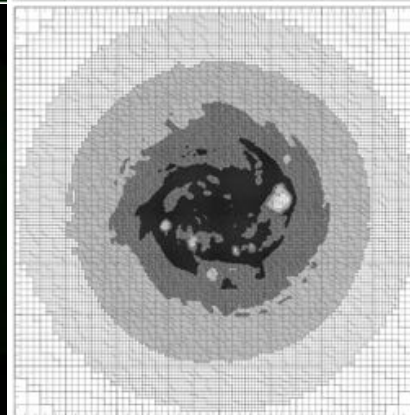
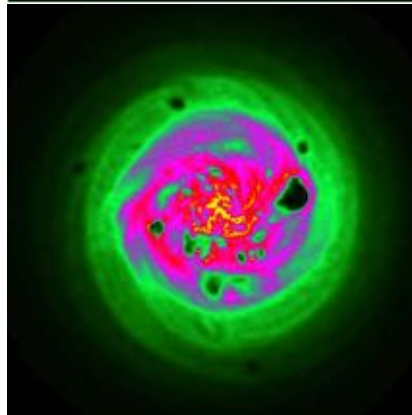
Spiral galaxy



AGN torus



SPH simulation



Geo-centric  
grids are more  
accurate and  
more efficient

*Saftly et al. 2013*

# Grid resolution criteria

## How to determine subdivision depth?

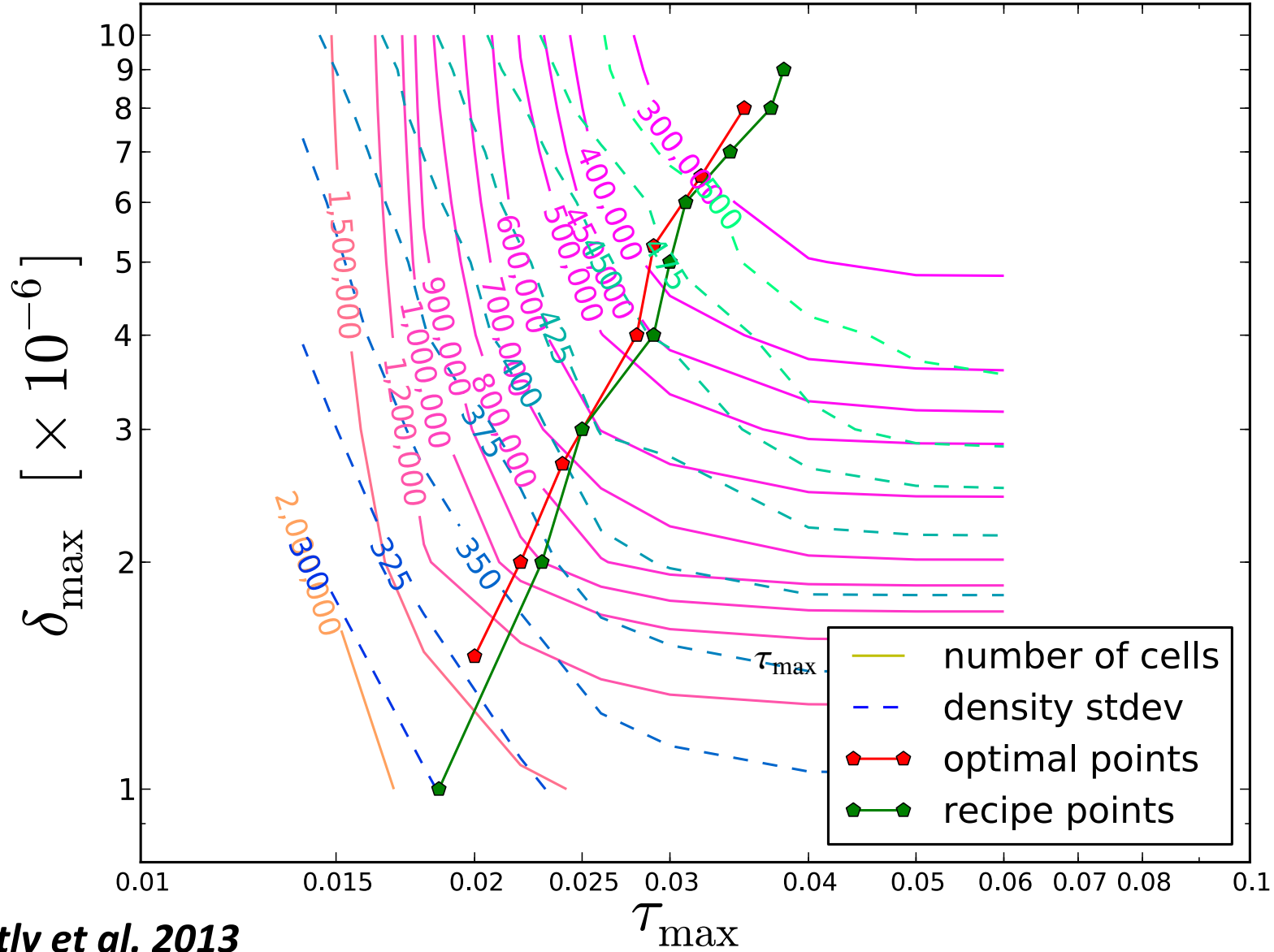
- The objective is to properly resolve the **radiation field**
- But... we don't know this until we run a RT simulation
- For now: criteria based on the **dust density** distribution
- Future: adjust grid during the simulation based on the radiation field calculated so far

## Criteria implemented in SKIRT

- Nesting level:  $L < L_{\max}$  (overrides other criteria)
- Dust mass fraction:  $M_{\text{cell}} / M_{\text{tot}} = \delta < \delta_{\max}$
- Optical depth:  $\tau_{\text{cell}} < \tau_{\max}$
- Density dispersion:  $(\rho_{\max} - \rho_{\min}) / \rho_{\max} = q < q_{\max}$



# Dust mass fraction and optical depth criteria



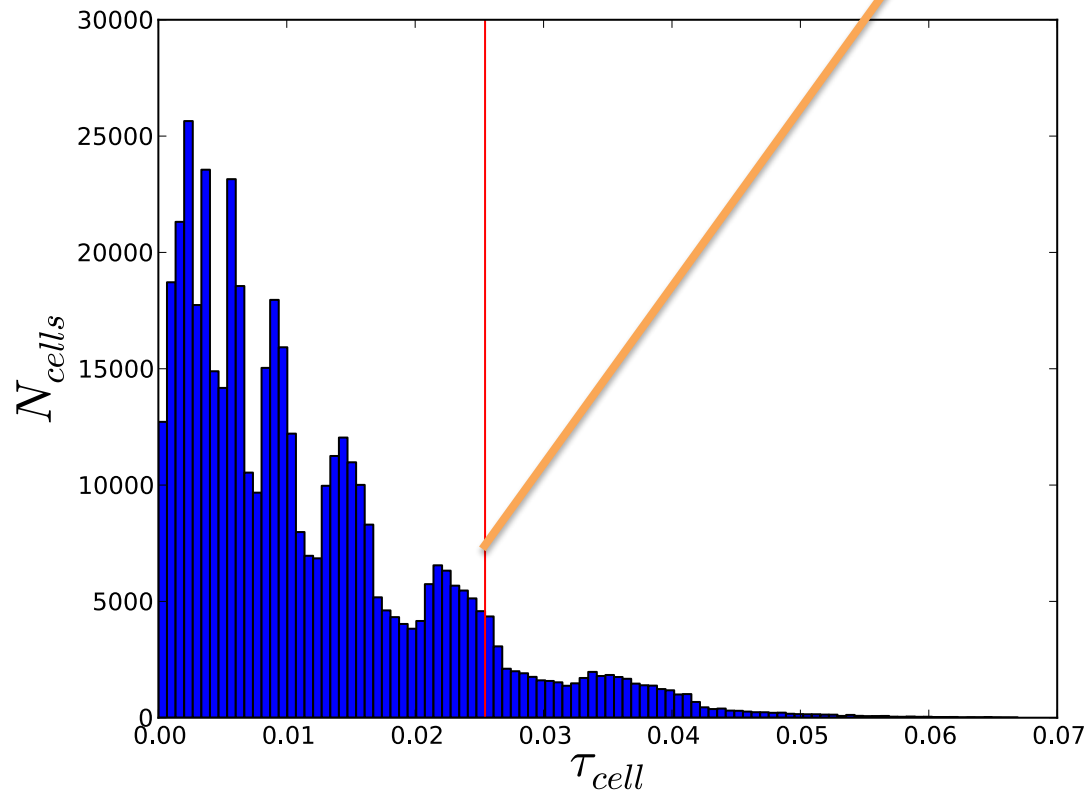
Saftly et al. 2013

# Optimal scheme combining $\delta_{\max}$ and $\tau_{\max}$

- Dust mass fraction:  $\delta < \delta_{\max}$
- Optical depth:  $\tau_{\text{cell}} < \tau_{\max} = \tau_{90}$

“sets number of cells”

“improves quality”

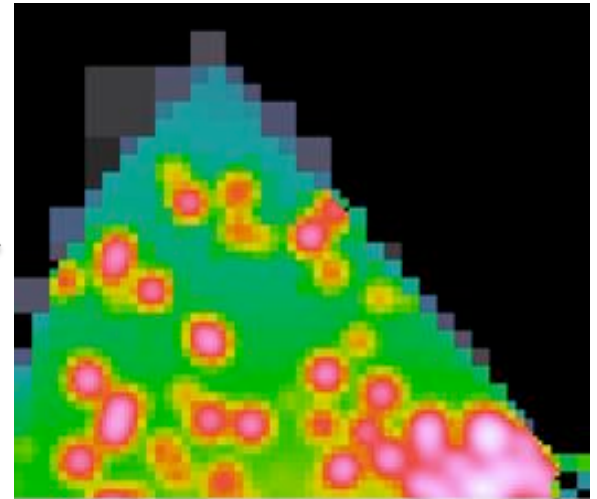


Using  $\tau_{90}$   
to cutoff the 10% tail  
of the  $\delta_{\max}$ -only result  
produces optimal grids

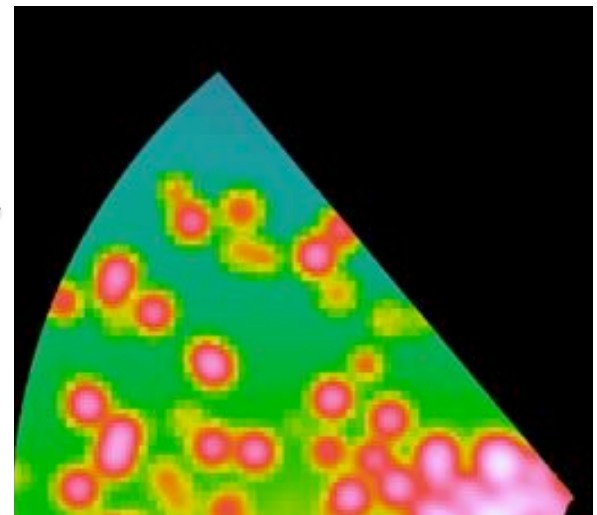
*Saftly et al. 2013*

# Strong gradients and sharp edges

- Using just the mass fraction criterion, sharp edges can still have large cells with a tiny and compact dusty corner



- The density dispersion criterion further subdivides these cells



The background of the slide is a complex, unstructured grid of irregular polygons. The colors of the polygons vary, with a central white and light yellow area, transitioning through yellow and orange to red and dark red at the edges. The polygons are of various shapes and sizes, creating a non-uniform, mesh-like appearance.

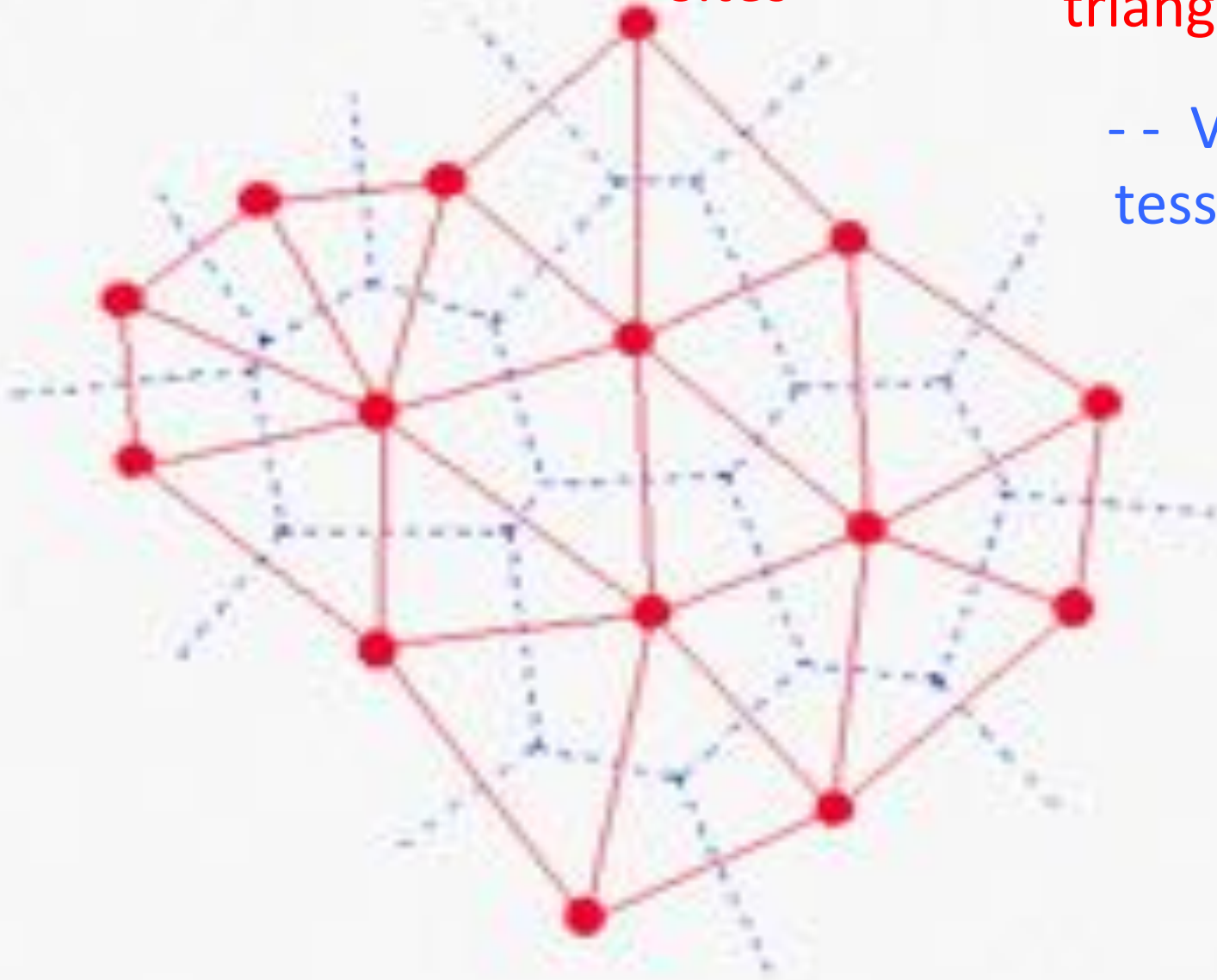
# Unstructured grids

# Voronoi cells in 2D

Sites

— Delaunay triangulation

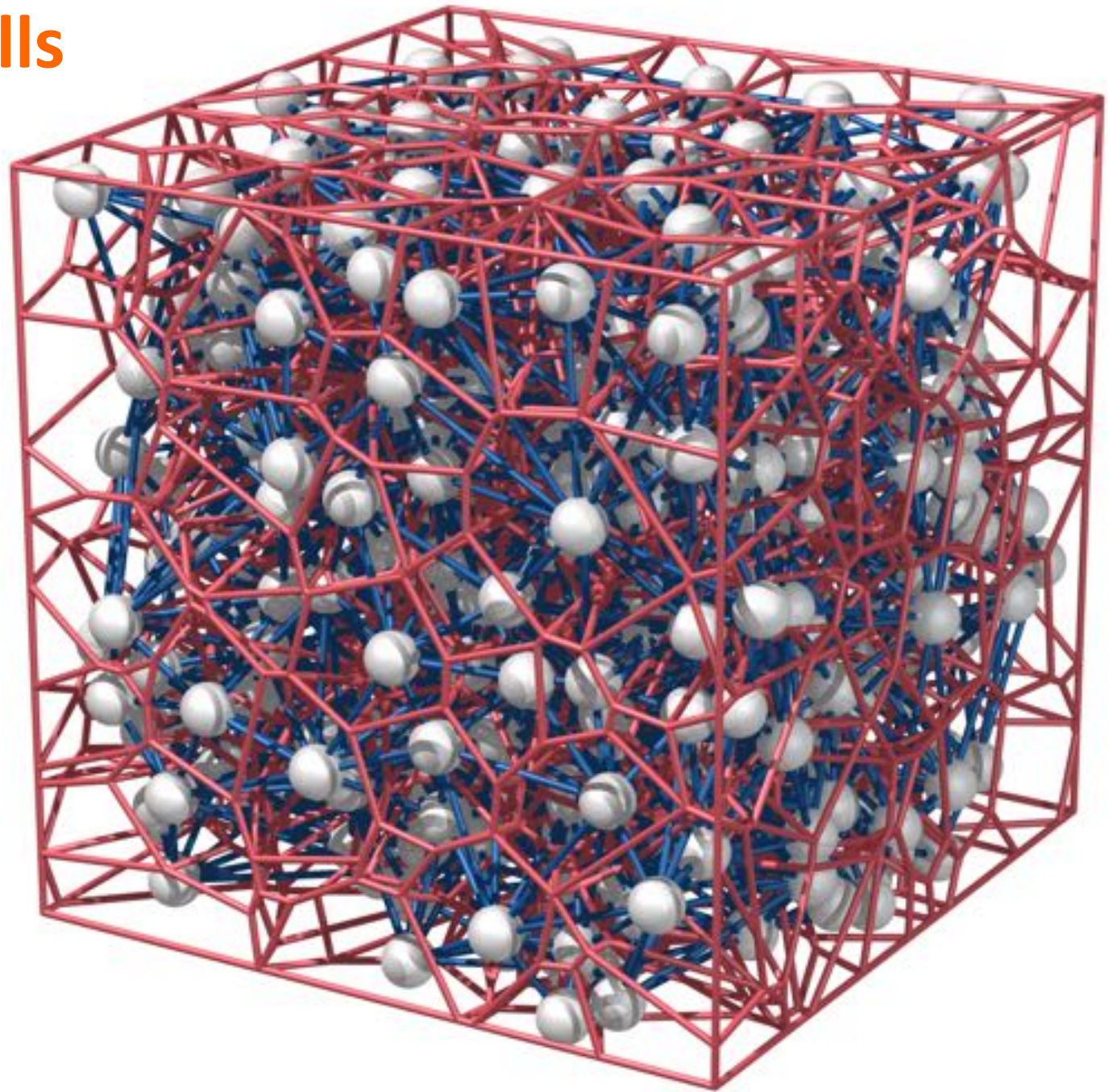
- - Voronoi tessellation



# Voronoi cells in 3D

— Delaunay  
edges

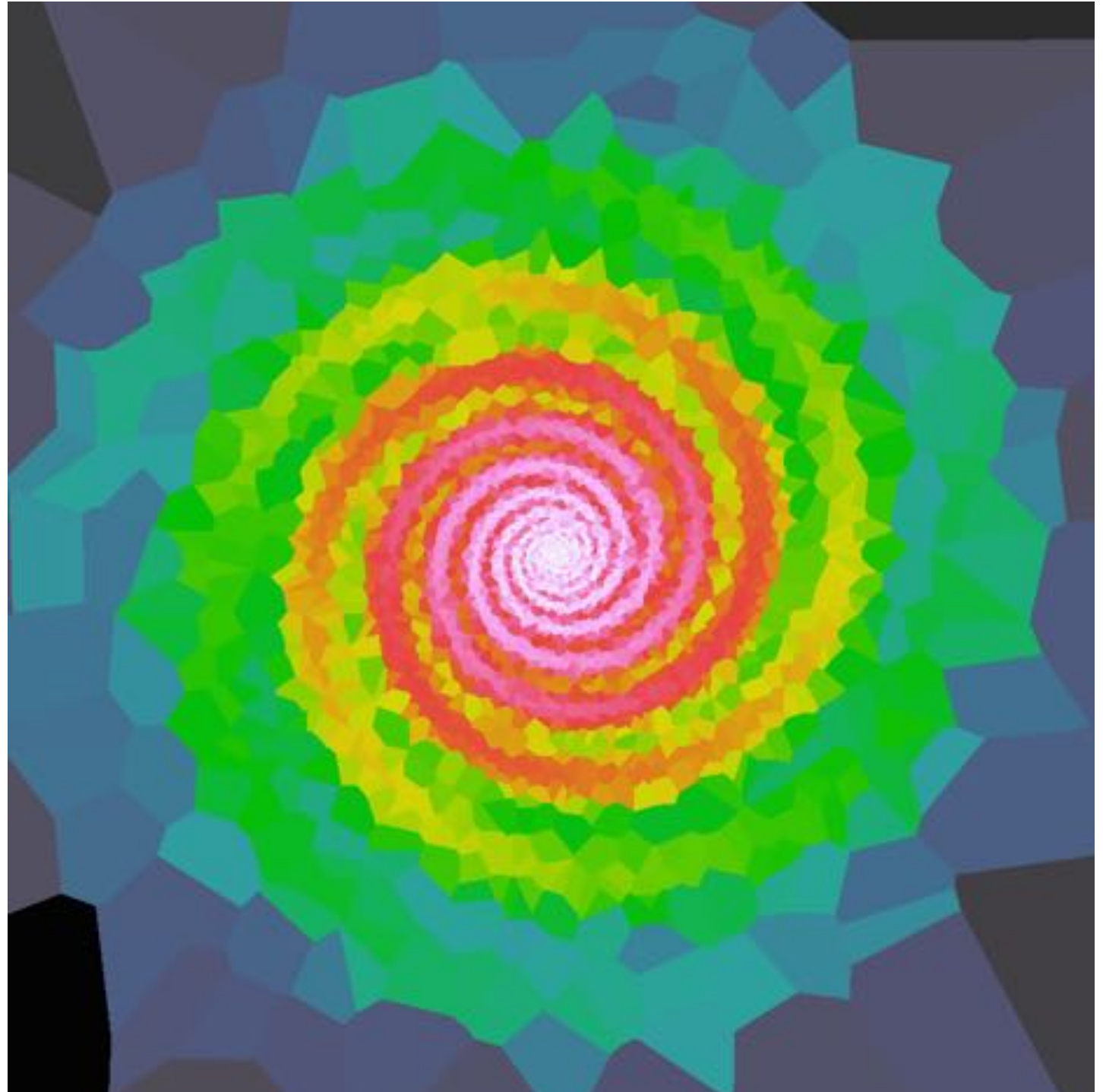
— Voronoi  
cell edges



(400 sites)

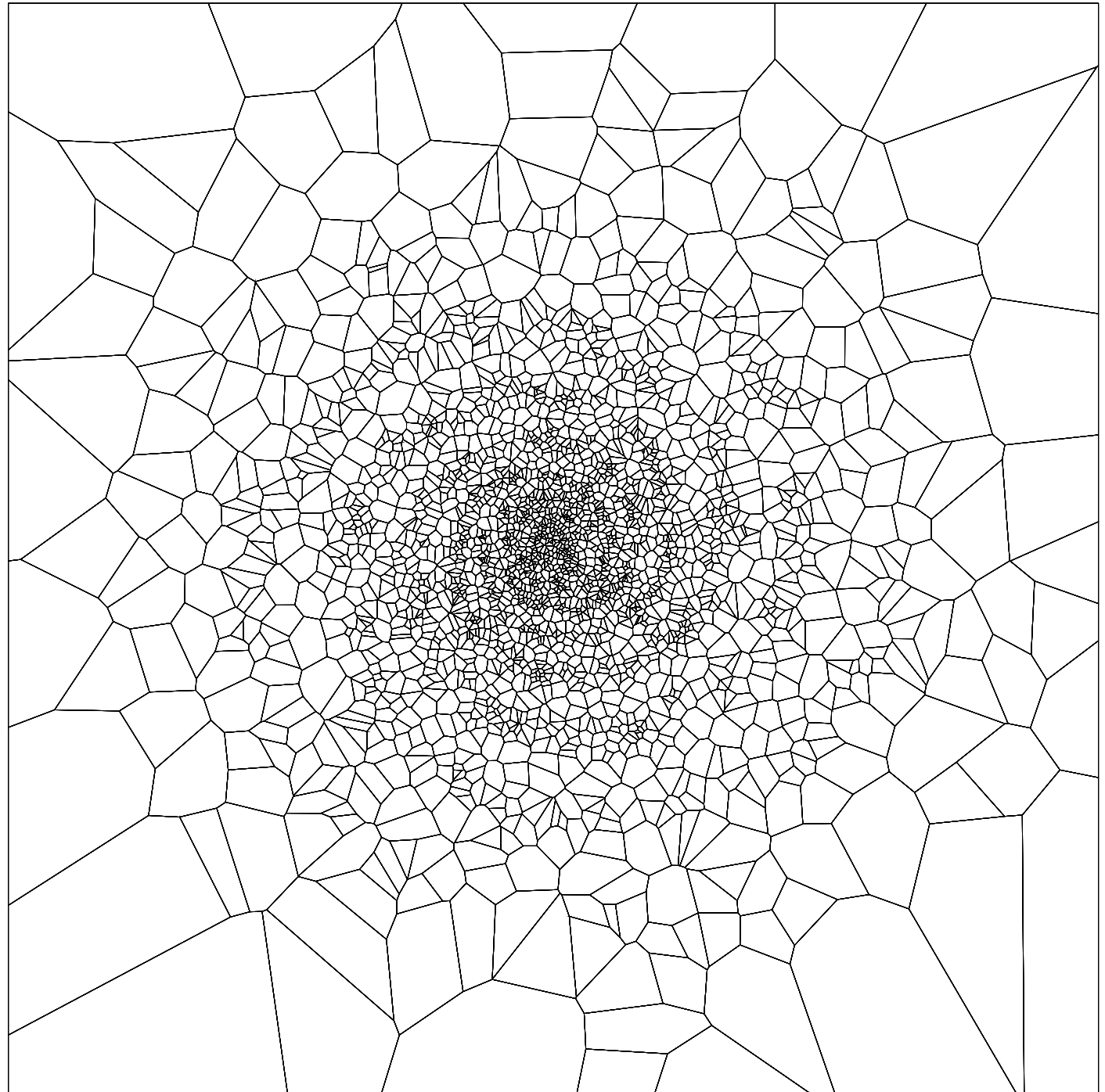
# Planar cut

Sites placed  
according to  
density  
distribution of  
dust in a spiral  
galaxy



# Planar cut

Sites placed  
according to  
density  
distribution of  
dust in a spiral  
galaxy



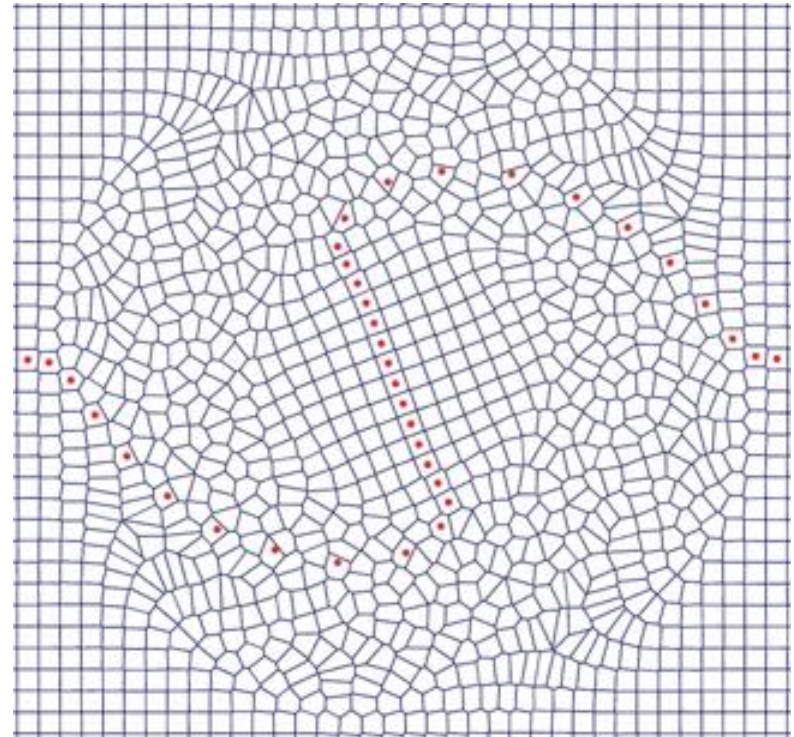
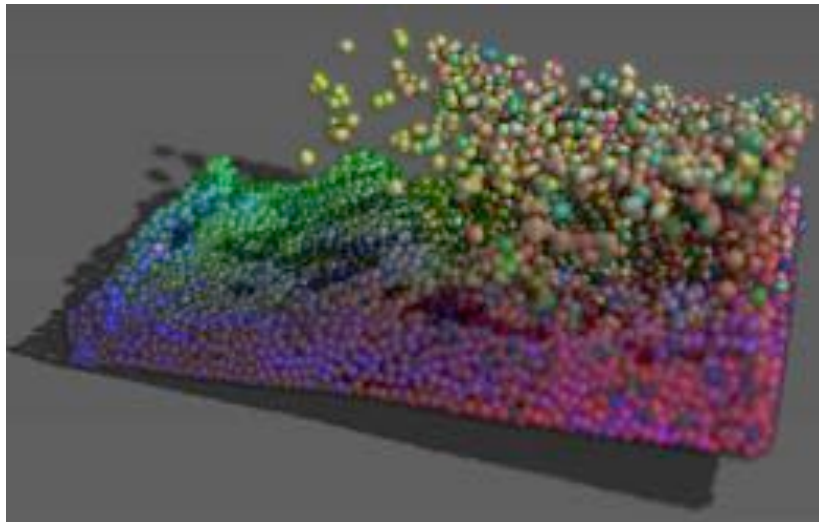


# Why consider Voronoi grids?

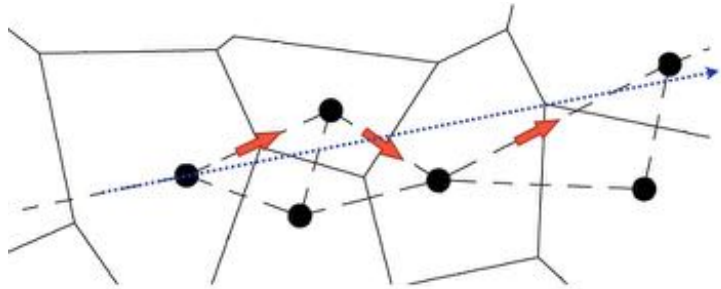
Minimize the **number of cells**

Place cell **boundaries** according to gradients

Natural grid for hydro **input models** (SPH, moving mesh)

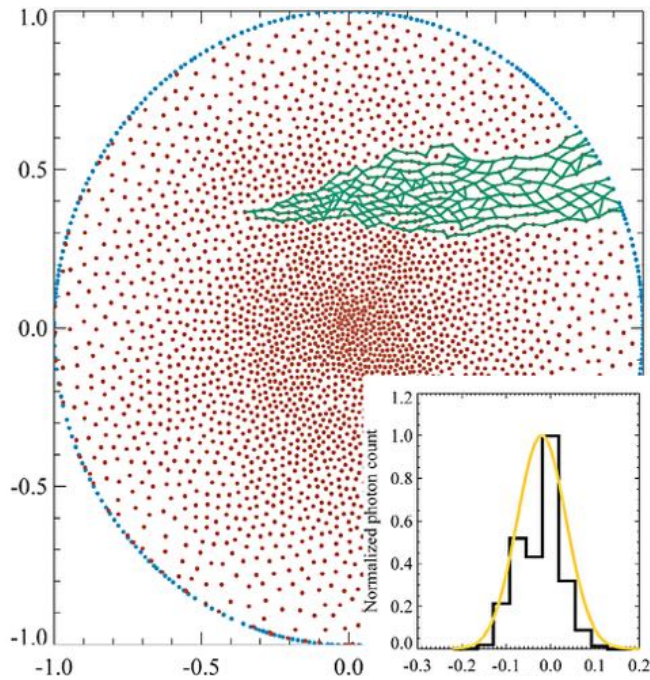


# Paths along Delaunay edges



SimpleX

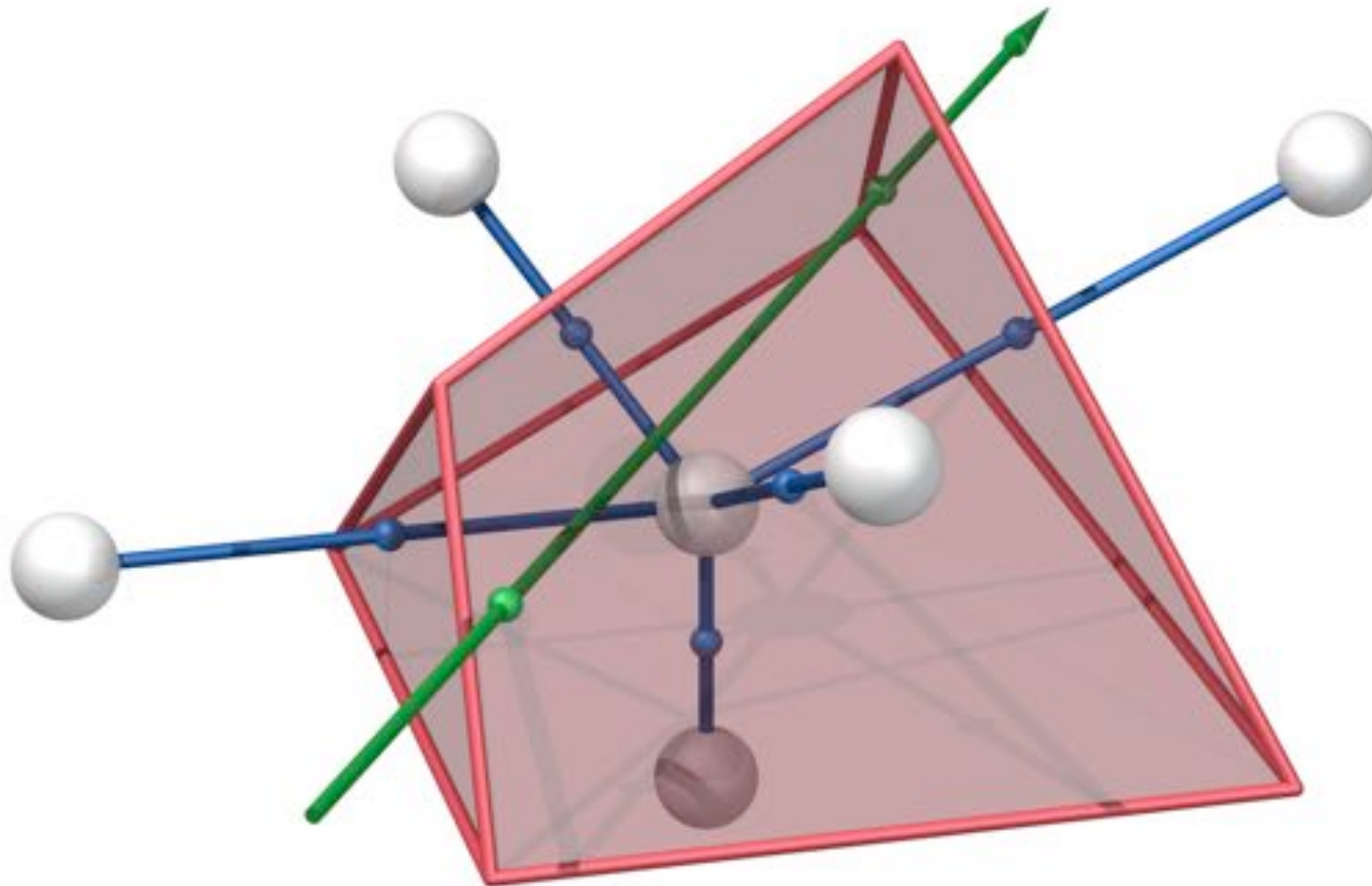
*Paardekooper et al 2010*



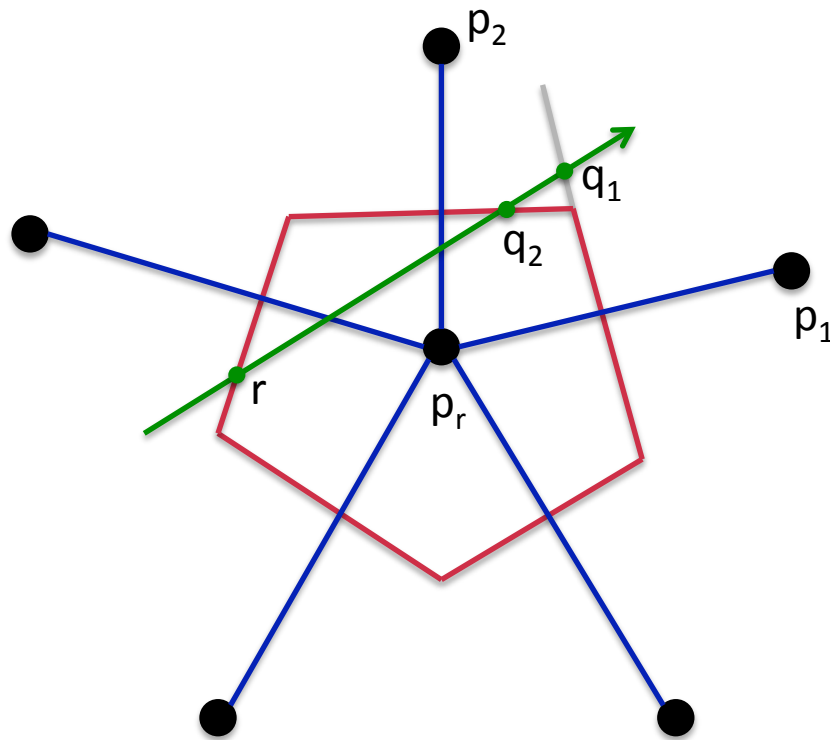
LIME

*Brinch & Hogerheijde 2010*

# Straight path through a Voronoi grid



# Straight path through a Voronoi grid



$$\mathbf{n} = \mathbf{p}_i - \mathbf{p}_r$$

$$\mathbf{p} = \frac{\mathbf{p}_i + \mathbf{p}_r}{2}$$

Equation of the plane

$$\mathbf{n} \cdot (\mathbf{x} - \mathbf{p}) = 0$$

Equation of the path

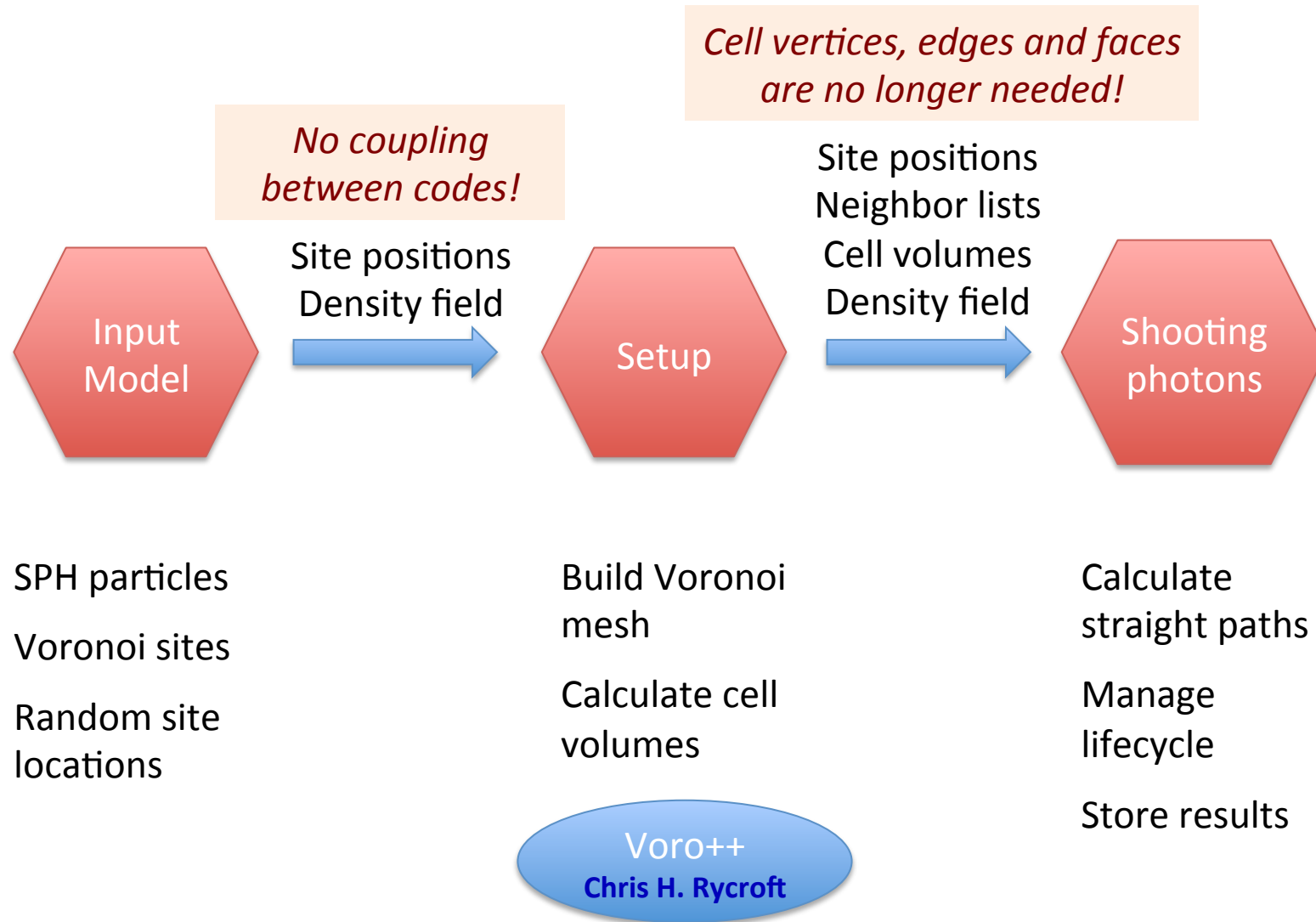
$$\mathbf{x} = \mathbf{r} + s \mathbf{k}$$

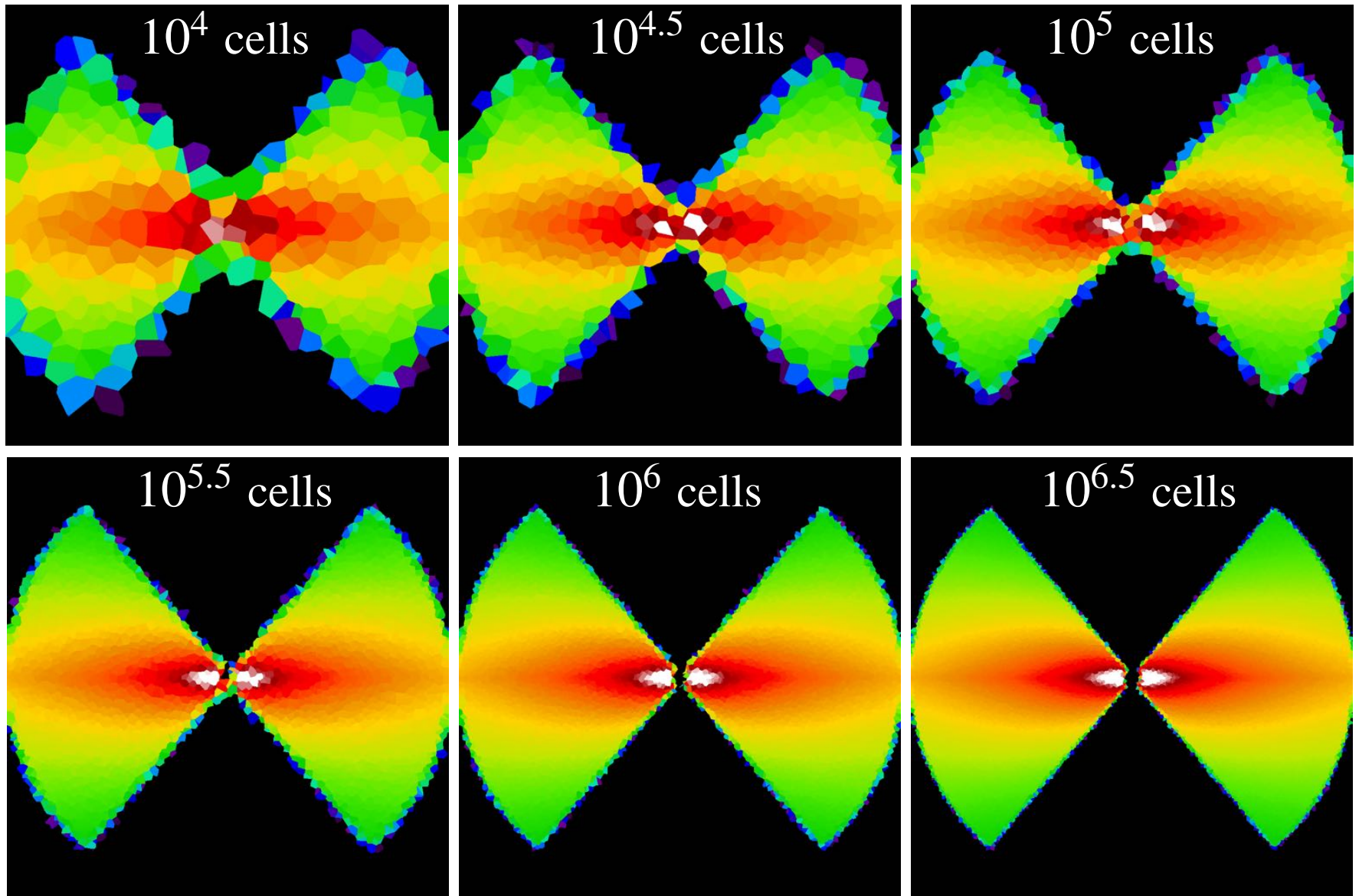
Intersection, solved for s

$$s = \frac{\mathbf{n} \cdot (\mathbf{p} - \mathbf{r})}{\mathbf{n} \cdot \mathbf{k}}$$

*Camps et al. 2013*

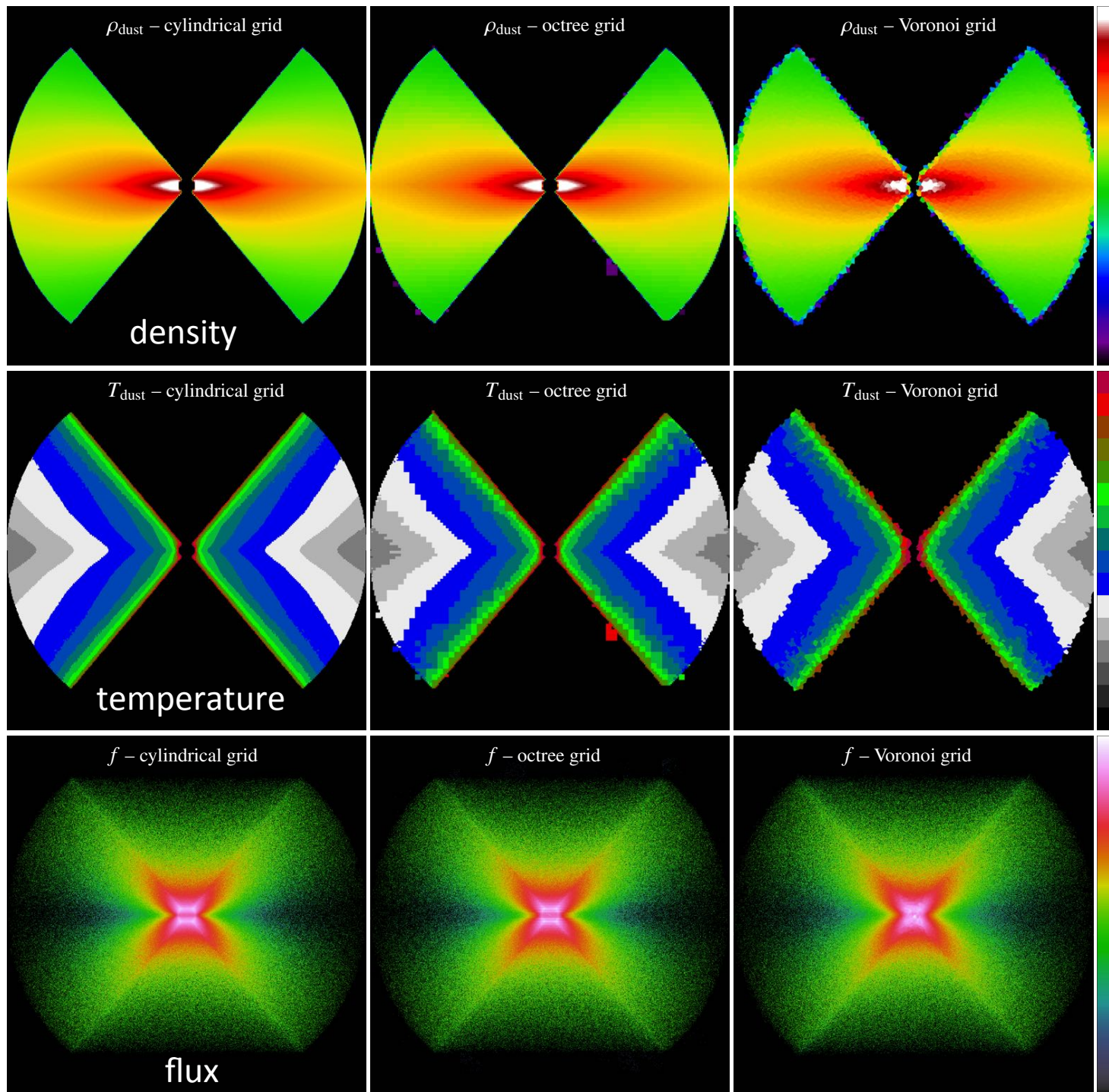
# Thin interfaces





**Cuts through grid with increasing number of cells**

# Torus model



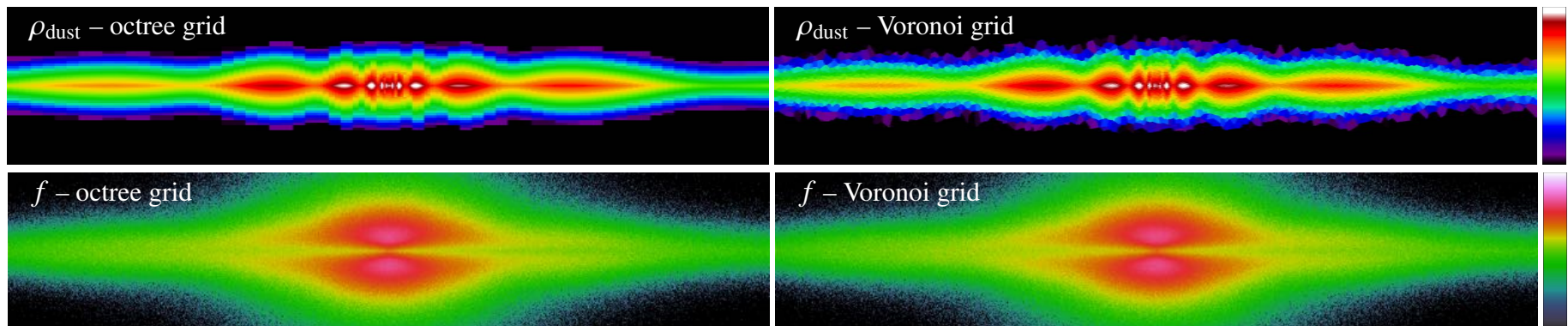
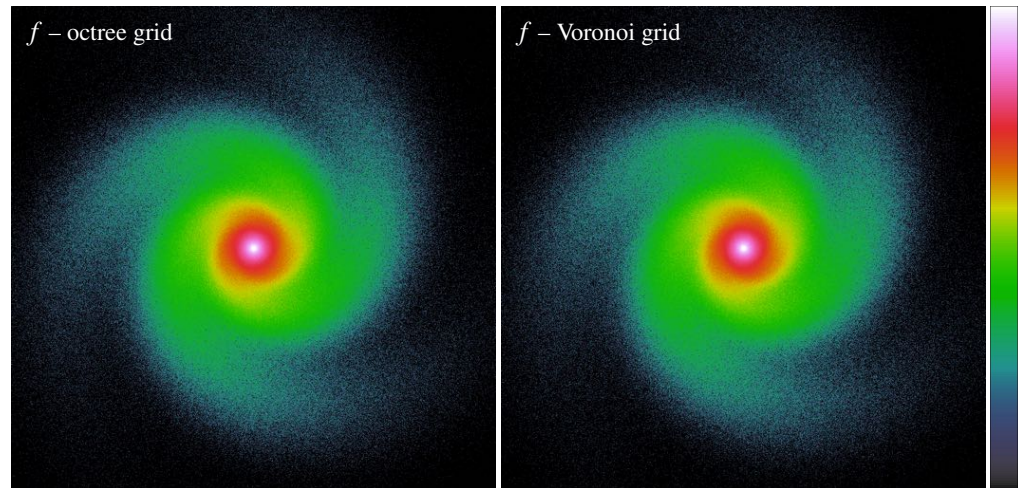
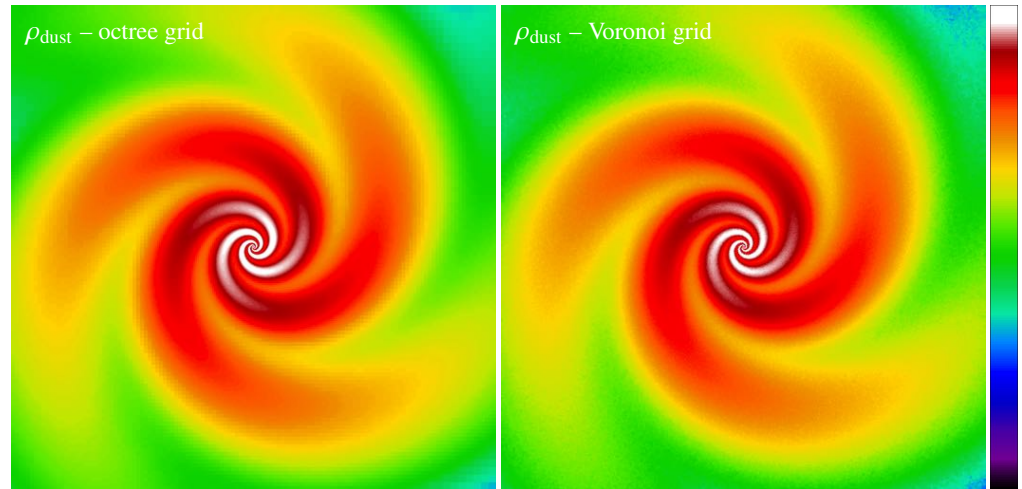
Octree & Voronoi grids have 950 000 cells

Voronoi sites are distributed uniformly

# Spiral model

Both grids have  
1 350 000 cells

Voronoi sites are  
distributed according  
to dust density





## Grid quality (std.dev. of $\rho_t - \rho_g$ )

Model	Cylindrical	Octree	Voronoi
Torus	0.82	1	1.75
Spiral	–	1	1.68

## Run time (including overhead)

Model	Simulation type	Time per cell crossing (ns)		
		Octree	Voronoi	Vor./Oct.
Torus	monochromatic	219	693	3.2
Torus	panchromatic	400	1006	2.5
Spiral	monochromatic	309	903	2.9
Spiral	panchromatic	442	1095	2.5

# Conclusions – 3D dust grids

## Hierarchical grids with cuboidal cells

- Use **neighbor** lists to traverse the grid
- **k-d tree** grids are about 20% “better” than octree grids
- Combination of **mass and optical depth** criteria is optimal

## Unstructured Voronoi grids

- Rather **straightforward** to implement in radiative transfer
- Only **3 times slower** per cell crossing
- Promise to have fewer and more **optimally placed cells** (to be confirmed)

Questions ?



# Importing hydro snapshots

Section B-3

# Observables for simulated galaxies

Properties deduced directly from simulation results:

- Size, mass, age, chemical composition
- Kinematics (central dispersion, rotation curve)
- Intrinsic 3D morphology (concentration, flattening, bulge to disk)
- Total bolometric luminosity

Properties calculated through dust radiative transfer:

- 2D morphologies from **various viewing angles**
- SEDs **from UV to FIR** wavelengths
- Luminosity in specific band, color



# Importing SPH and AMR data

*SPH = Smoothed Particle Hydrodynamics*

*AMR = Adaptive Mesh Refinement*

## Data format

- Read native snapshot data (in various formats), or define intermediate format containing just the required data

## Stars

- Assign **SED** based on particle/cell properties
- Launch random photons with appropriate distribution

## Dust

- Derive **dust** distribution from **gas** distribution (most hydro simulations do not trace the dust)
- **Sample** the dust **density** distribution defined by a large number of smoothed particles (can be very slow)
- Build **adaptive grid** that adjusts to dust density distribution

# The gas-to-dust relation

We use a (too) simple **heuristic** to determine the amount of dust contained in each gas particle/cell:

$$M_{\text{dust}} = \begin{cases} f_{\text{dust}} Z M & \text{if } T < T_{\text{max}} \\ 0 & \text{otherwise,} \end{cases}$$

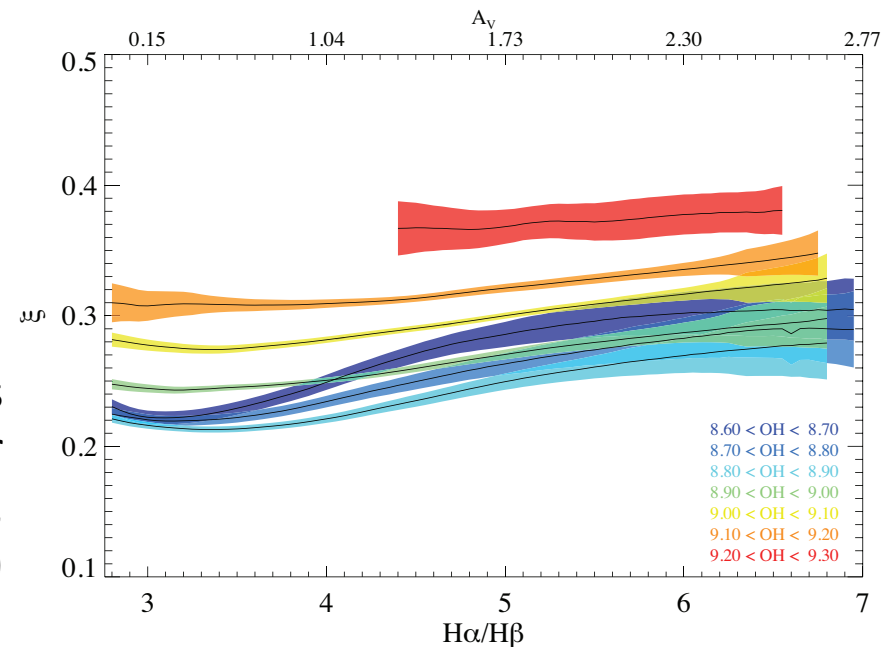
Gas properties:  
 $Z$ : **metallicity**  
 $T$ : **temperature**

Parameters:

$f_{\text{dust}}$ : fraction of metals locked in dust

$T_{\text{max}}$ : gas temperature above which  
all dust is destroyed

The **dust-to-metal ratio** as  
a function of the Balmer  
decrement (SDSS sample,  
**Brinchmann et al. 2013**)



# Density sampling on SPH particles

## Organize particles in a smart search grid

- List of particles that overlap each cell in a regular grid

## Optimize density interpolation on each particle

$$\rho(\mathbf{r}) = f_{\text{dust}} \sum_i Z_i M_i W(h_i, |\mathbf{r} - \mathbf{r}_i|)$$

standard spline kernel: 
$$W(h, r) = \frac{8}{\pi h^3} \times \begin{cases} 1 - 6u^2(1-u) & \text{for } 0 < u < \frac{1}{2}, \\ 2(1-u)^3 & \text{for } \frac{1}{2} < u < 1, \\ 0 & \text{else.} \end{cases}$$

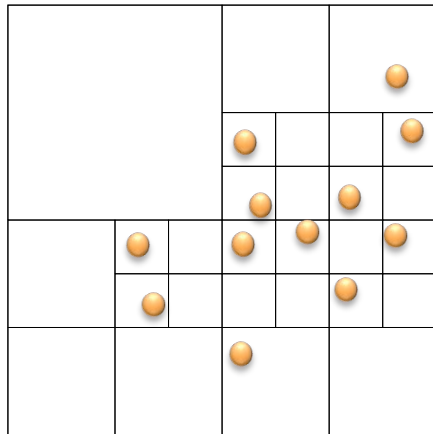
$$M_{\text{box}} = f_{\text{dust}} \sum_i Z_i M_i \int_{x_{\min}}^{x_{\max}} \int_{y_{\min}}^{y_{\max}} \int_{z_{\min}}^{z_{\max}} W(h_i, |\mathbf{r} - \mathbf{r}_i|) dx dy dz$$

scaled Gaussian kernel: 
$$W(h, r) = \frac{a^3}{\pi^{3/2} h^3} \exp\left(-\frac{a^2 r^2}{h^2}\right) \quad a = 2.42$$

6 error function evaluations per integral -> **tabulate** error function



# Specialty dust grids for hydro snapshots

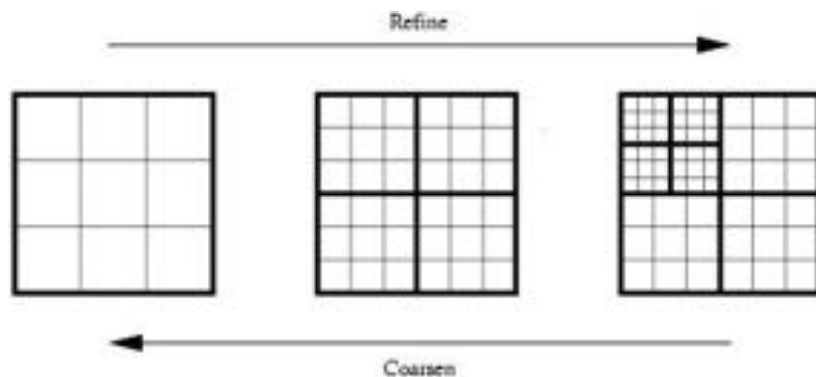
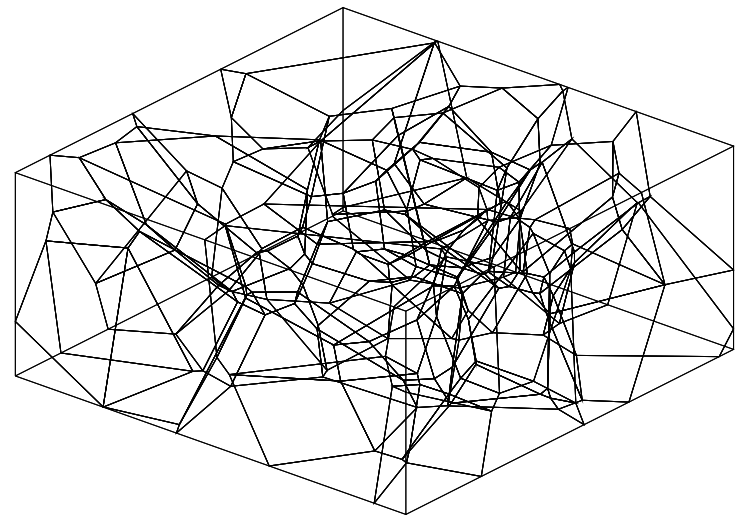


Octree or *k*-d tree

- Subdivide until there is at most **one particle** in each cell
- Then **subdivide further** with usual stopping criteria

Voronoi grid

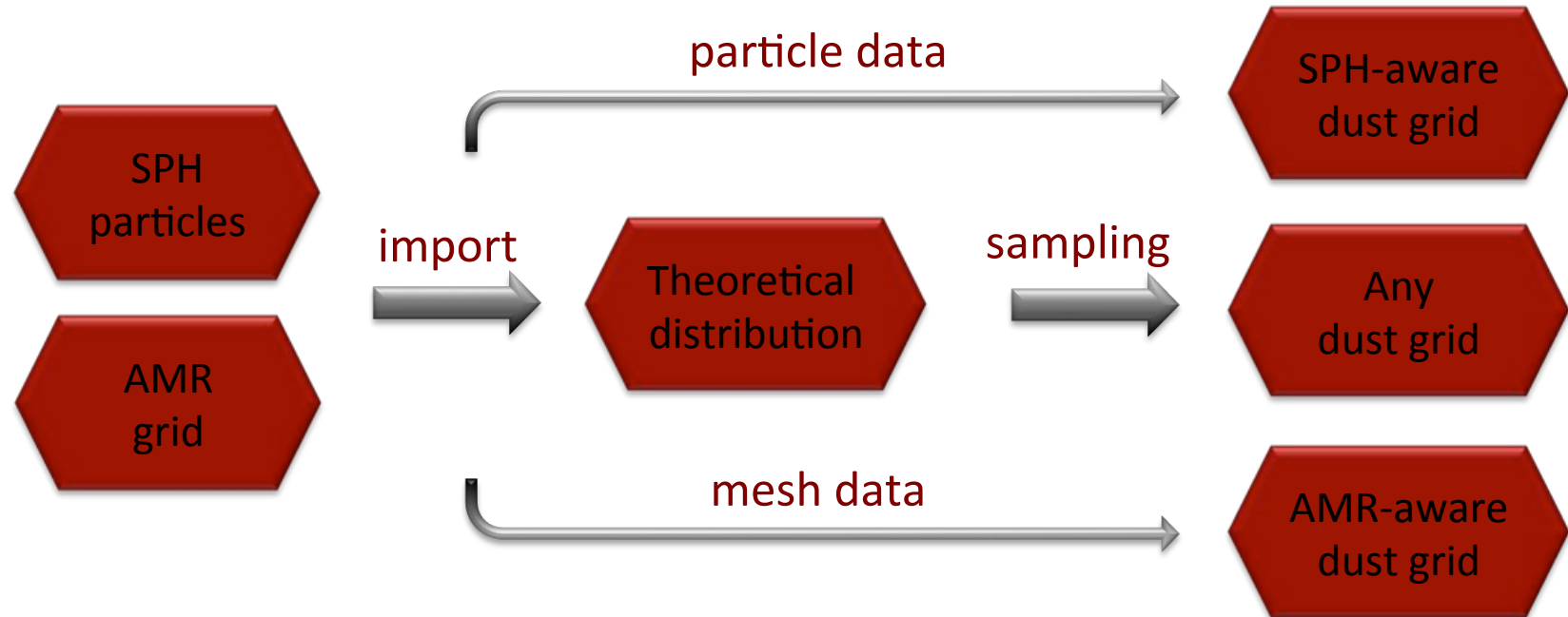
- Use particle positions as **seeds** (one cell per particle)



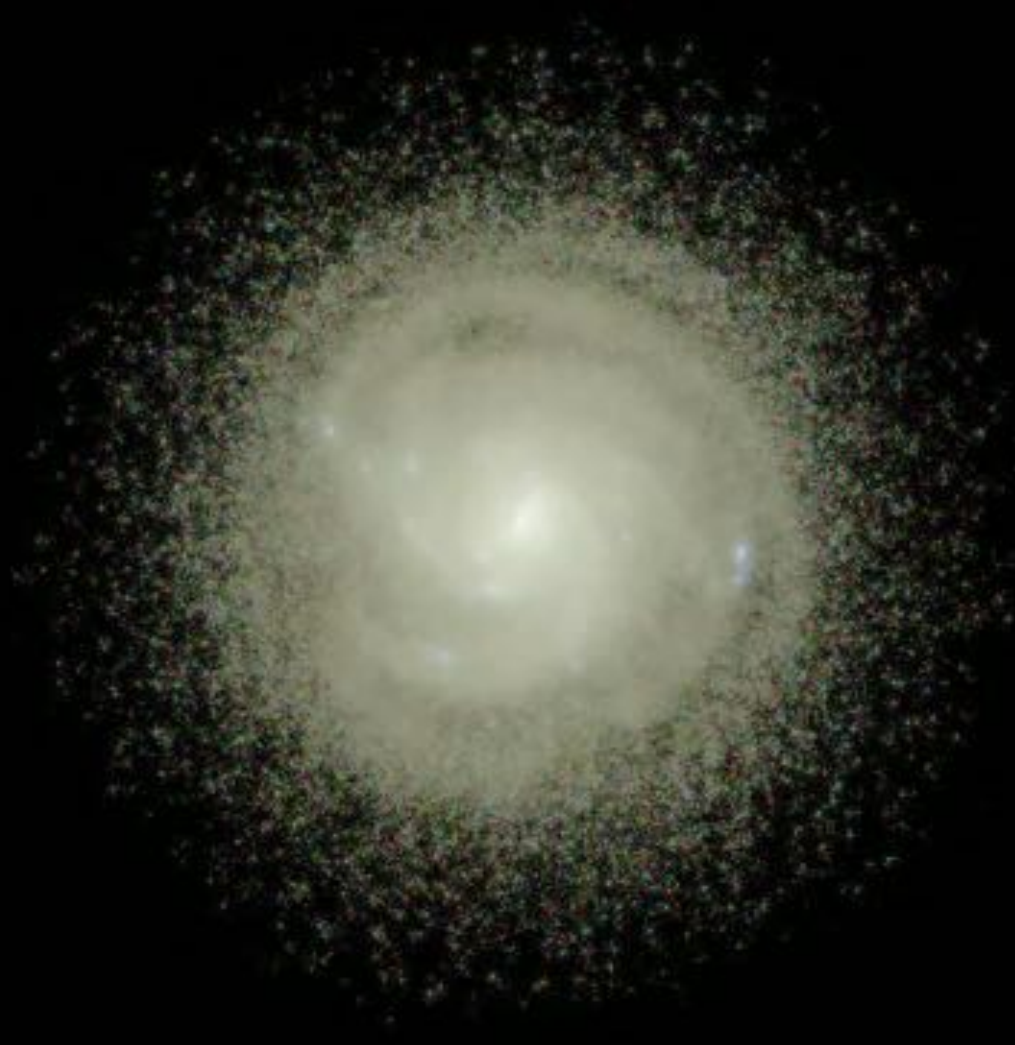
AMR grid

- Identical to **imported** grid

# Code structure in SKIRT



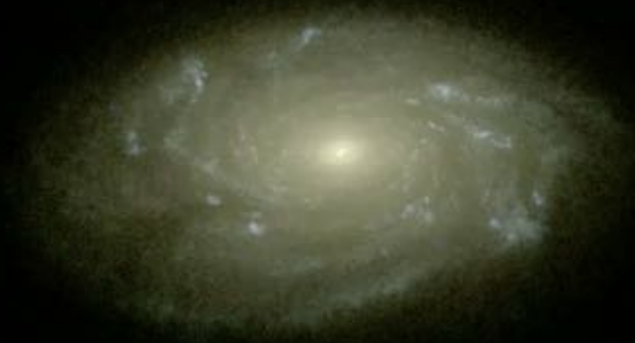
- Bypass interfaces operate only when **both parties** support it
- Input-format-aware dust grids can be **smarter**
  - Use particle **positions** or mesh cells to setup grid structure
  - Analytically calculate **density** in cuboid
- ➔ Faster import, and conceivably also **higher-quality** grid



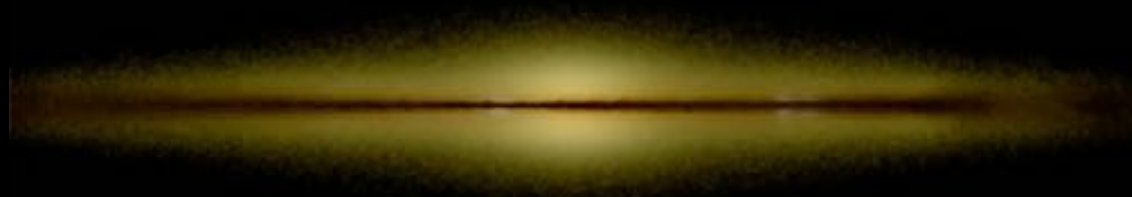
**SPH Data:**

***Rahimi & Kawata 2012***

Eris



R13



Questions ?



# **FIR properties of galaxies in a cosmological simulation**

**Section B-4**

# EAGLE

*Schaye et al. 2015*

Cosmological simulation(s)

100 Mpc box

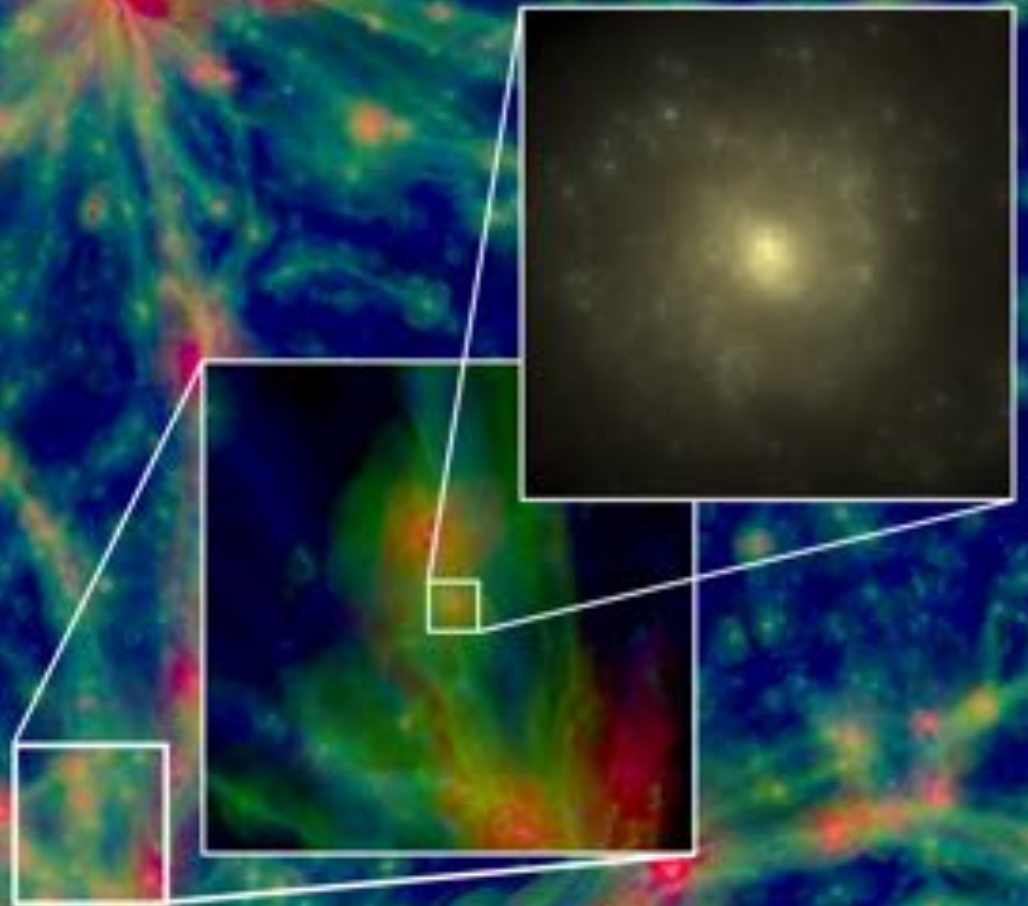
7 billion particles

Dark matter

Baryons

Star formation & feedback

Calibrated to reproduce present-day  
galaxy stellar mass function



# The Eagle Simulations

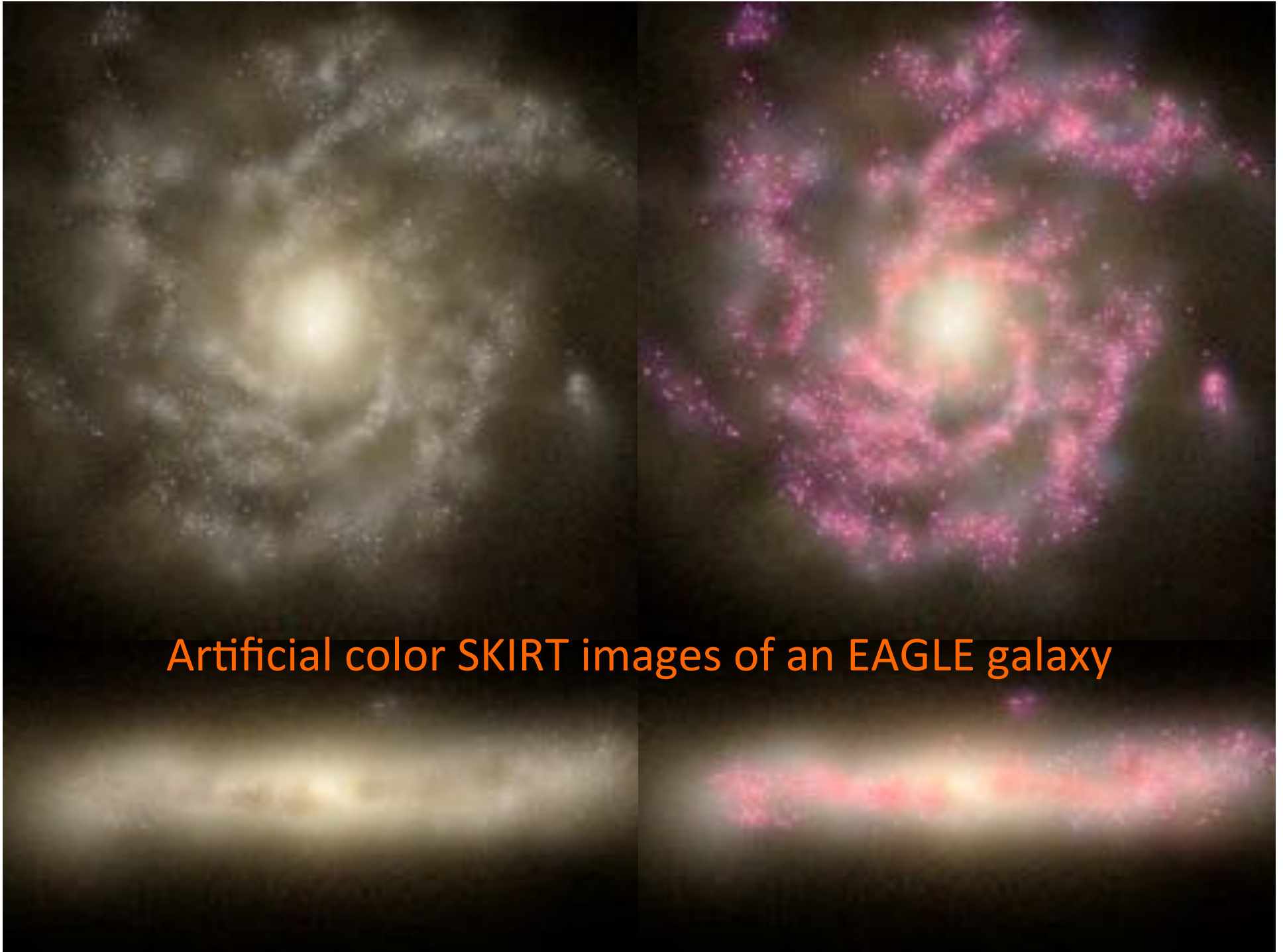
EVOLUTION AND ASSEMBLY OF GALAXIES AND THEIR ENVIRONMENTS

The Hubble Sequence realised in cosmological simulations

*Schaye et al. 2015*

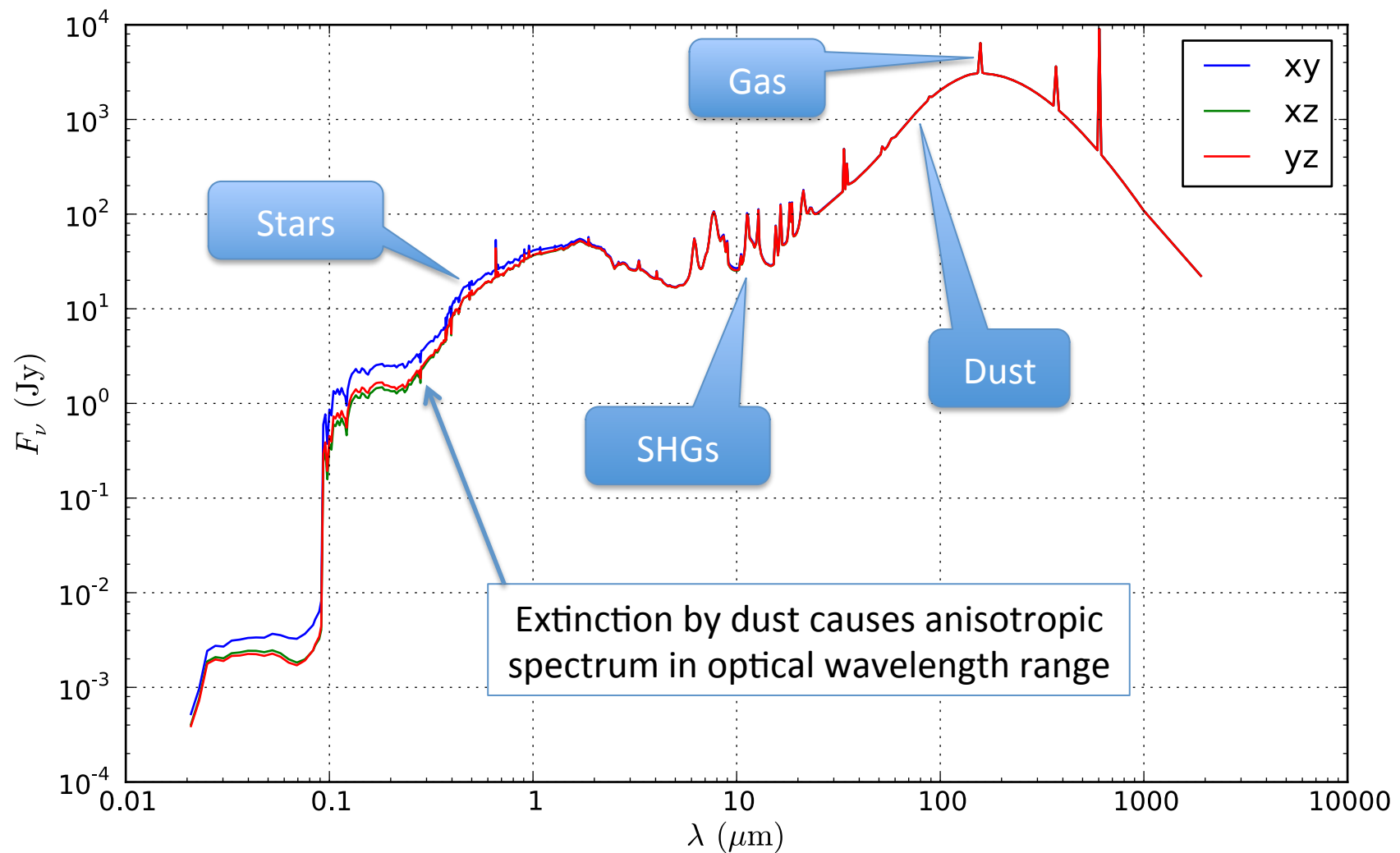


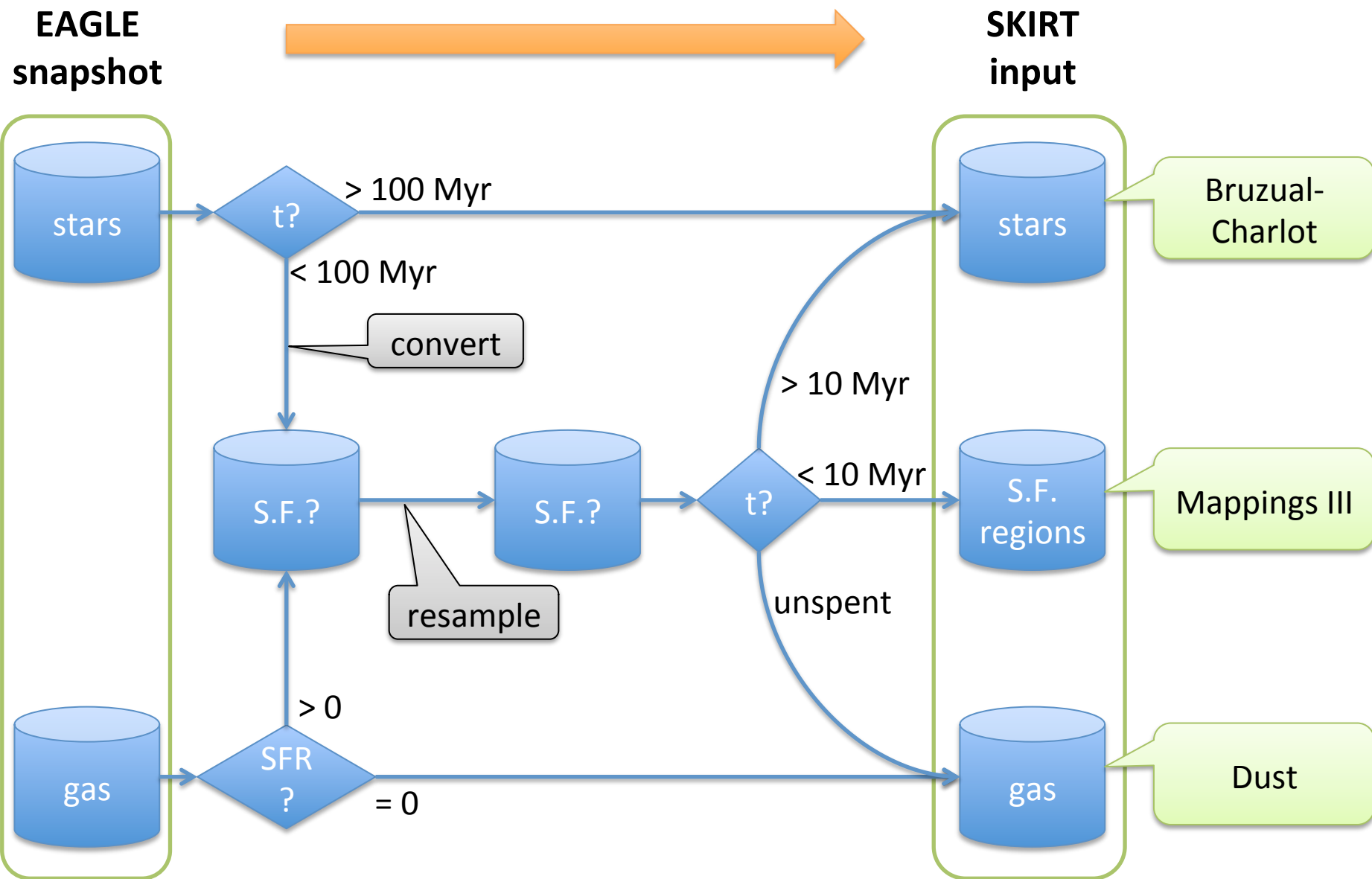




Artificial color SKIRT images of an EAGLE galaxy

# Full SED from UV to sub-mm produced by SKIRT



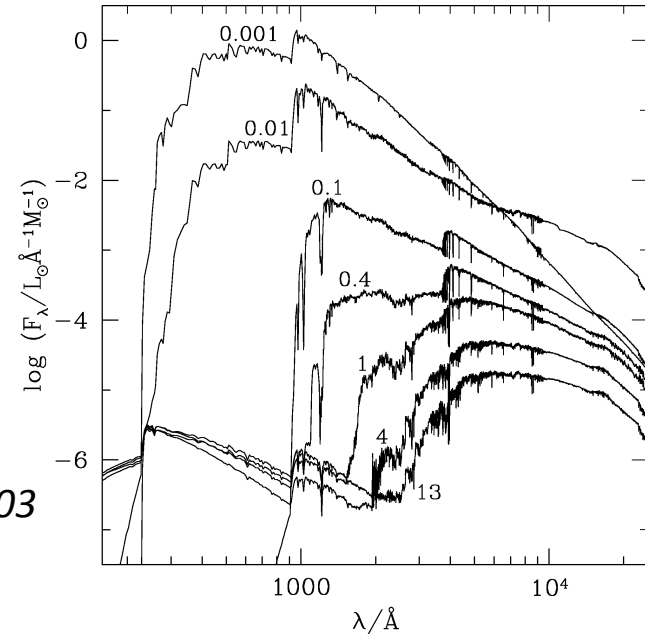


# SKIRT assigns SEDs to input particles

## Star

→ Bruzual-Charlot **stellar population** SED depending on age and metallicity

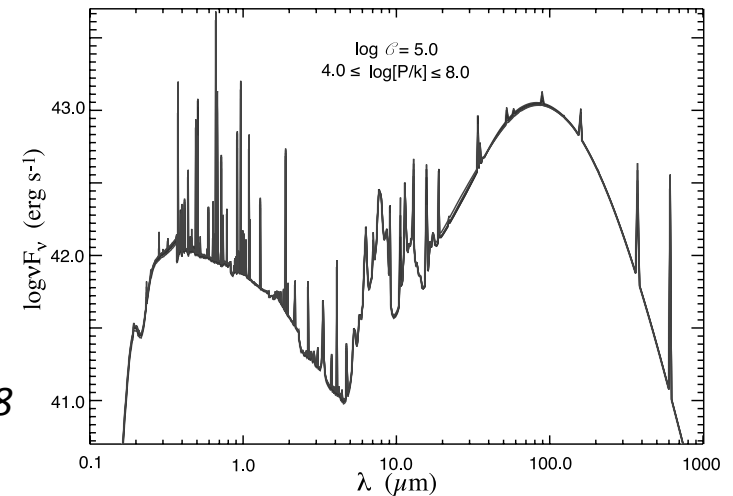
*Bruzual & Charlot 2003*



## Star forming region

→ MAPPINGS III starburst SED (HII region around cluster of young stars) depending on metallicity, compactness, pressure, PDR covering factor

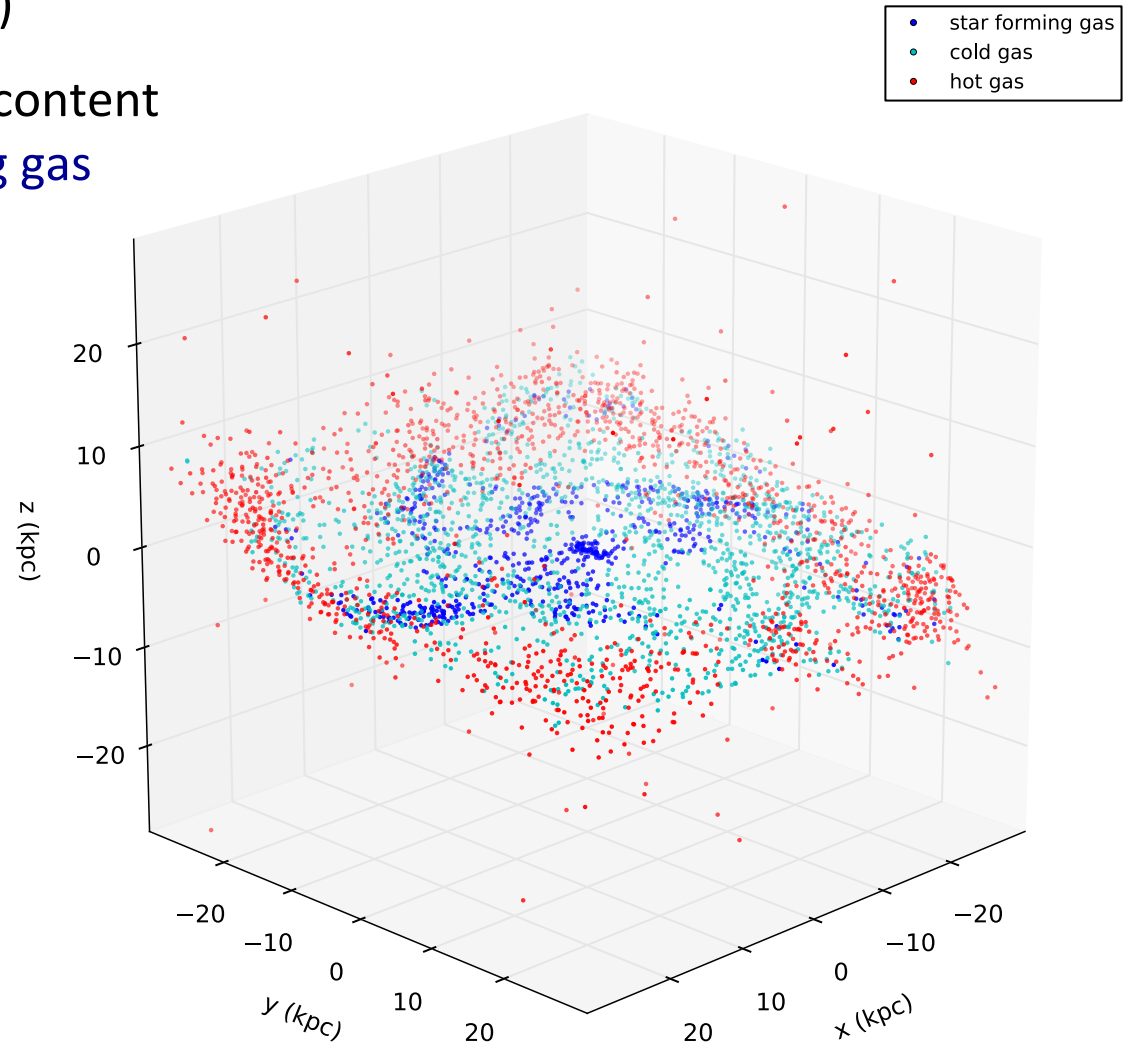
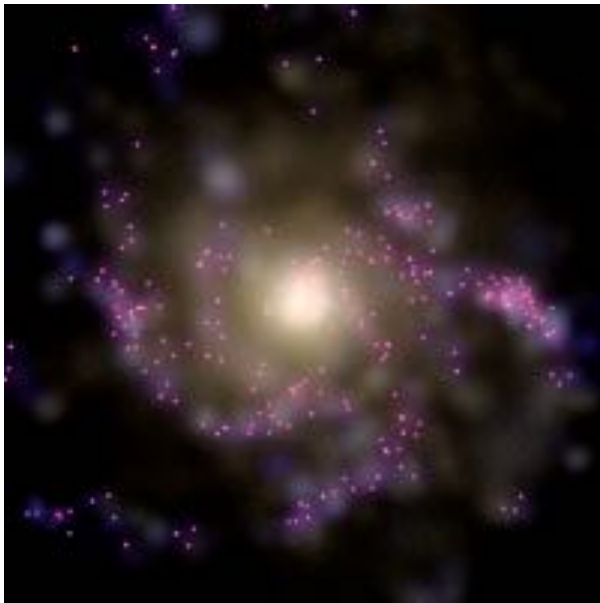
*Groves et al. 2008*



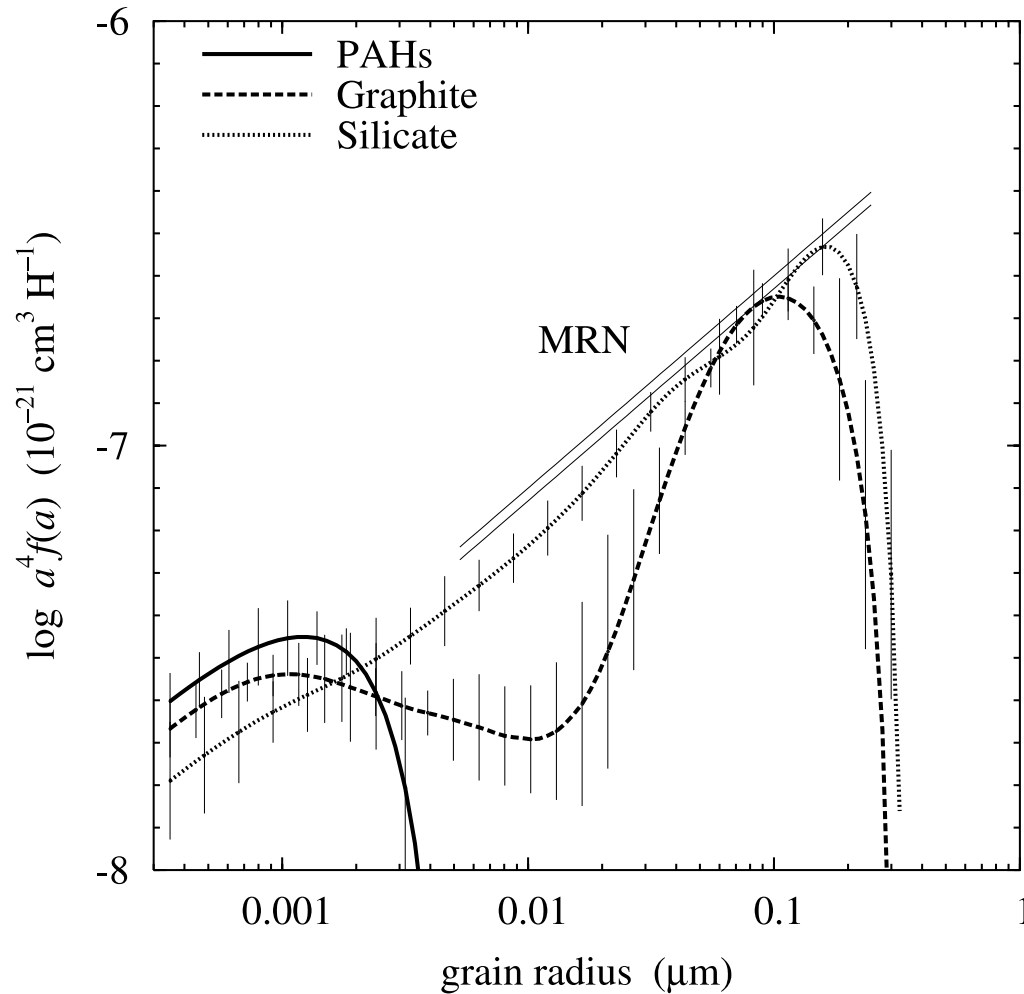
# SKIRT assigns dust content to input gas particles

No dust in hot gas ( $T > 8000$  K)

Fixed fraction (40%) of metal content in cold gas and in star-forming gas



## Dust model used for EAGLE galaxies



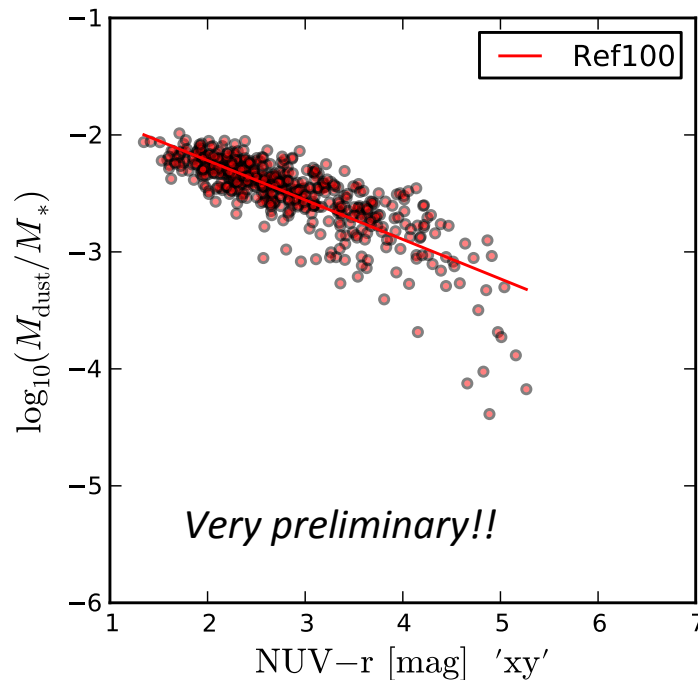
- Realistic mixture
  - » 33% graphite grains
  - » 62% silicate grains
  - » 5% neutral and ionized PAHs
- Fine-tuned to accurately reproduce the extinction, emission and abundance constraints on the Milky Way

Size distribution for BARE\_GR\_S model  
from *Zubko, Dwek & Arendt 2004*

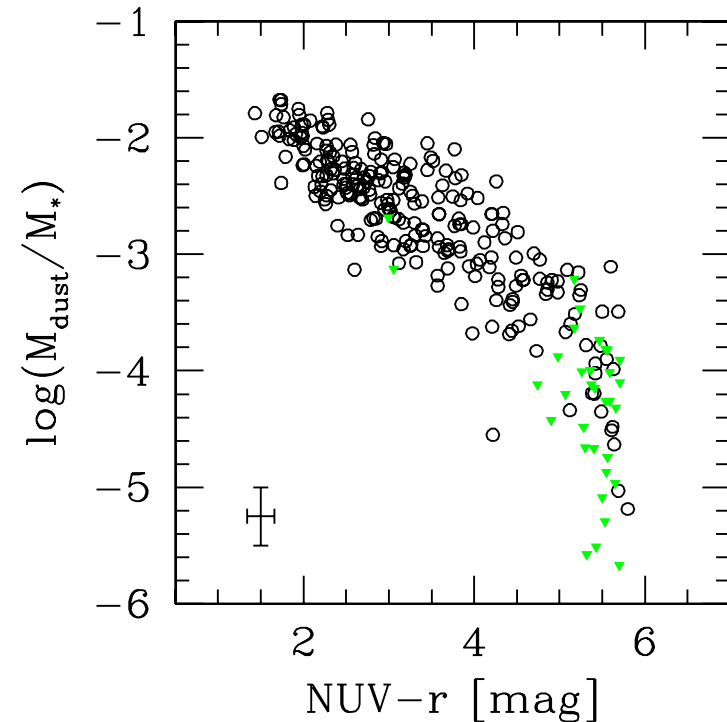
# Objective: compare far-infrared and dust properties of EAGLE galaxies to observations

Cortese et al. 2012

SKIRT results for EAGLE galaxies



Herschel Reference Survey



## TO DO

- mimic observational selection effect
- use mock observational quantities for  $M_{\text{dust}}$  en  $M_{\text{star}}$
- fine-tune parameters such as dust fraction, PDR coverage factor, ...







Questions ?

