













Rotational kinetic energy of pulsar

$$E_{\rm rot} = \frac{1}{2}I\omega^2$$

with

$$\omega = \frac{2\pi}{P_{\text{rot}}}$$
 and $I = \frac{2}{5}MR^2$

for a sphere of uniform density. Hence

$$E_{\rm rot} = \frac{4\pi^2 M R^2}{5 P_{\rm rot}^2}$$

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Hence
$$L = \frac{8}{5}\pi^2 M R^2 P_{\rm rot}^{-3} \left(\frac{dP_{\rm rot}}{dt}\right)$$

and rearranging gives

$$\frac{dP_{\rm rot}}{dt} = \frac{5}{8\pi^2} \left(\frac{LP_{\rm rot}^3}{MR^2}\right)$$

•For M = 1 M_{Sun}, R = 10km and, for the Crab nebula and pulsar, the observed values of L = 10^{31} W, P_{rot} = 0.03 s we obtain the observed slow-down rate.

$$\frac{dP_{\rm rot}}{dt} = 10^{-13} s s^{-1}$$

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So rotational kinetic energy is removed from the neutron star by the free electrons ejected from its magnetic polar regions at high speeds.

Electrons emit synchrotron radiation, but remain "tied" to the open field lines out to large distances- hence magnetic braking.

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