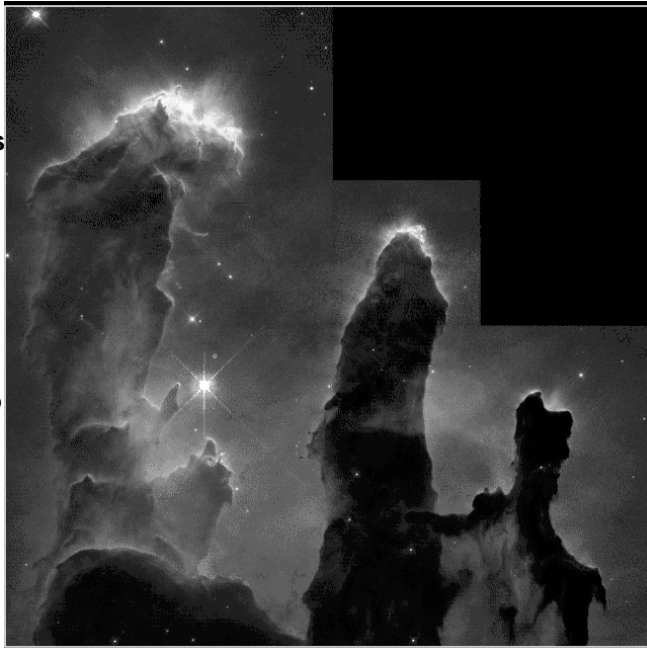


## 4. Star formation

- Galactic ISM: roughly uniform gas  $n \sim 5 \times 10^6 \text{ m}^{-3}$ .
- Stars form in molecular clouds.
- Dimensions  $\sim 10 \text{ pc}$ , density  $\sim 5 \times 10^9 \text{ m}^{-3}$ , temperature  $\sim 10 \text{ K}$ .
- Galactic magnetic field strongly tied to ionized plasma in ISM.
- Field lines run parallel to galactic plane.
- Local perturbations  
→ potential wells  
→ condensations.



**Gaseous Pillars · M16**

HST · WFPC2

PRC95-44a · ST ScI OPO · November 2, 1995  
J. Hester and P. Scowen (AZ State Univ.), NASA

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## 4.1 Jeans' criterion

- Contracting cloud must be compact enough to ensure that dispersive effects of internal pressure don't overwhelm gravity.
- Energetically, cloud becomes bound if:

$$E_{\text{grav}} + E_{\text{kin}} < 0.$$

- Spherical cloud, mass  $M$ , radius  $R$  has gravitational binding energy:

$$E_{\text{grav}} = \int_0^M \frac{Gm}{r} dm = -A \frac{GM^2}{R}$$

- where  $A$  depends on (and increases with) degree of central condensation of internal density distribution.
- $A=3/5$  for uniform density; we'll use  $A=1$ .

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## Conditions for collapse

- Total thermal (kinetic) energy of cloud is:

$$E_{\text{kin}} = \frac{3}{2} \frac{M}{\mu m_{\text{H}}} kT$$

Average mass  
of cloud particle

- Critical condition: for collapse of a cloud with radius R to occur, need either:

$$M_{\text{cloud}} > M_{\text{J}} = \frac{3kT}{2G\mu m_{\text{H}}} R$$

Jeans mass

- or

$$\rho_{\text{cloud}} > \rho_{\text{J}} = \frac{3}{4\pi M^2} \left[ \frac{3kT}{2G\mu m_{\text{H}}} \right]^3$$

Jeans density

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## 4.2 Onset of contraction

- Contraction of a massive gas-dust cloud will proceed if not opposed by increasing internal pressure.
- Release of  $E_{\text{grav}}$  tends to increase internal temperature but also excites  $\text{H}_2$  and other molecules into excited rotational levels.
- De-excitation emits photons mainly at IR and mm-wave frequencies where cloud is transparent.
- Hence photons escape, cooling the cloud and allowing contraction to proceed.

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## 4.3 Fragmentation and formation of protostars

- As main cloud contracts, smaller subregions will also reach the Jeans density
- Fragments will contract independently provided gravitational PE is not converted to internal KE.
- Energy released can be absorbed by:
  - Dissociation of  $H_2$  ( $\epsilon_D = 4.5$  eV)
  - ionisation of atomic H ( $\epsilon_I = 13.6$  eV)
- Amount of energy absorbed by this process is:

$$\frac{M}{2m_H} \epsilon_D + \frac{M}{m_H} \epsilon_I.$$

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## Radius of a protostar

- If we know the initial radius of the protostar we can calculate the final radius from:

$$GM \left( \frac{1}{R_2} - \frac{1}{R_1} \right) \approx \frac{1}{m_H} \left( \frac{\epsilon_D}{2} + \epsilon_I \right).$$

- Example: Radius of a protostar of 1 solar mass is  $\sim 10^{15}$  m with a Jeans density  $\sim 10^{-16}$  kg m<sup>-3</sup>.
- The dissociation + ionisation energy is  $3 \times 10^{39}$  J.
- The radius after gravitational contraction is  $R_2 \sim 10^{11}$  m.
- The timescale for this contraction is  $t_{\text{dyn}} \sim 20,000$  y.

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## 4.4 Approach to hydrostatic equilibrium

- **After H is all ionised:**
  - the internal pressure rises
  - contraction slows down
  - hydrostatic equilibrium is approached.
- **Can use the Virial theorem to estimate the average internal temperature at this point.**
- **Total thermal KE of protons and electrons is:**

$$E_{\text{kin}} \sim \frac{3kT}{2} \frac{M}{\mu m_{\text{H}}} = \frac{3kTM}{m_{\text{H}}}.$$

- **Gravitational energy at end of collapse is:**

$$E_{\text{grav}} \sim -\frac{GM^2}{R_2} \sim -\frac{M}{m_{\text{H}}} \left( \frac{\varepsilon_{\text{D}}}{2} + \varepsilon_{\text{I}} \right).$$

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## 4.5 Thermal contraction

- **Virial theorem:  $2E_{\text{kin}} + E_{\text{grav}} = 0$ , so protostar approaches equilibrium at an average temperature**

$$kT \sim \frac{(\varepsilon_{\text{D}} + 2\varepsilon_{\text{I}})}{12} \sim 2.6 \text{ eV},$$

- **Corresponds to  $T \sim 30,000 \text{ K}$ .**
- **Independent of mass of protostar.**
- **Subsequent contraction governed by opacity, which controls loss of radiation from surface.**
- **Hence gravitational energy is radiated away on a thermal (Kelvin) timescale,  $t_{\text{K}} \sim 10^7 - 10^8 \text{ y}$ .**
- **Star remains close to hydrostatic equilibrium so we can continue to use Virial theorem.**

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## 4.6 How far could contraction proceed without nuclear reactions?

- Classical mechanics breaks down when wavefunctions of neighbouring electrons begin to overlap significantly, i.e. at separation

$$r = \lambda_B = \frac{h}{m_e v} \quad \text{de Broglie wavelength}$$

- Since  $\frac{1}{2} m_e v^2 = \frac{3}{2} kT$ ,  $r = \frac{h}{(3m_e kT)^{1/2}}$

$$\Rightarrow \rho = \frac{\mu m_H}{(4/3)\pi r^3}$$

$$\Rightarrow \rho \approx \mu m_H \frac{(m_e kT)^{3/2}}{h^3}.$$

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## Minimum mass of a star

- At this point a further increase in density does not affect the temperature.
- Virial theorem gives average internal temperature:

$$kT \approx \frac{GM\mu m_H}{3R} \approx G\mu m_H M^{2/3} \rho^{1/3}$$

- Substitute to get maximum temperature:

$$kT_{\max} \approx \left[ \frac{G^2 \mu m_H^{8/3} m_e}{h^2} \right] M^{4/3} \Rightarrow T_{\max} \approx 10^7 \left( \frac{M}{M_{\text{Sun}}} \right)^{4/3}$$

- For  $M < 0.08 M_{\text{Sun}}$ ,  $T$  will not be high enough to trigger nuclear reactions.

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